

Statics and Dynamics of Complex Network Systems: Supply Chain Analysis and Financial Networks with Intermediation

Dissertation Defense

by

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June 21, 2004

- Complex network systems
 - ◆ Financial networks with intermediation
 - ◆ Supply chains
- In
 - ◆ Static setting
 - ◆ Dynamic setting

Dissertation Structure

- Introduction
 - ◆ Literature survey
 - ◆ Research motivation
- Methodologies
 - ◆ Variational inequality theory
 - ◆ Projected dynamical systems
- Multilevel network perspective for supply chain
- Financial networks with intermediation
 - ◆ Statics
 - ◆ Dynamics
 - ◆ Electronic transaction
 - ◆ Risk management with variable weights

Literature Survey for Supply Chain Analysis

- Interdisciplinary topic that received great attention
 - ◆ Theoretical challenges
 - ◆ Practical importance
- Conceptual in nature
 - ◆ Cohen and Huchzermeier (1997), Bramel and Simchi-Levi (1997), Poirier (1996, 1999), Miller (2001)
- Analytical study
 - ◆ Federgruen and Zipkin (1986), Federgruen (1993), Chan, Muriel and Simchi-Levi (1998), Ganeshan et al. (1998)

- Development of supply chain network models
 - ◆ Study of interactions among decision-makers
 - ◆ Compete within a tier
 - ◆ Cooperate between tiers
 - ◆ Nagurney, Dong, and Zhang (2002)
 - ◆ First multitiered model studying the supply chains in a unified manner in network equilibrium context
 - ◆ Nagurney and Dong (2002b)
 - ◆ For further background
 - ◆ Nagurney, Loo, Dong, and Zhang (2002)
 - ◆ Static models over a single network
 - ◆ Nagurney and Dong (2002a) and Nagurney, Dong, and Mokhtarian (2001, 2003)
 - ◆ Unified treatment of complex network systems
 - Teleshopping vs shopping
 - Telecommuting vs commuting

Research Motivation for Supply Chain Analysis

- To capture distinct flows
 - ◆ Logistical
 - ◆ Informational
 - ◆ Financialwithin the *same* supply chain network system
- Observe *evolution* of
 - ◆ Prices
 - ◆ Commodity shipmentsthrough a discrete-time process

Novelty of My Research

- Nagurney, Ke, Cruz, Hancock and Southworth (2002)
 - ◆ *Environment and Planning B*
 - ◆ First proposed the multilevel (Logistical/Informational/Financial) network perspective to study the supply chain problem in network equilibrium context.
 - ◆ In the supply chain model, the financial and informational networks are made explicit.
 - ◆ The multilevel network was widely used thereafter and inspired the idea of supernetworks (<http://supernet.som.umass.edu/>).

Literature Survey for Financial Networks with Intermediation

- Intermediation
 - ◆ Banks, savings institutions, investment and insurance companies
- Quesnay (1758)
 - ◆ Origin use of networks to represent financial system
 - ◆ Depict the circular flow of funds
- Thore (1969, 1980)
 - ◆ Study systems of linked portfolios in credit networks
 - ◆ Decentralization/decomposition theory
 - ◆ Basic intertemporal models

Literature Survey for Financial Networks with Intermediation

- Nagurney, Dong, and Hughes (1992)
 - ◆ Multi-sector, multi-instrument
- Dong, Zhang, and Nagurney (1996)
 - ◆ Dynamic model
- Nagurney and Dong (1995, 1996a, b)
 - ◆ Inclusion of transaction costs

Literature Survey for Electronic Finance

- A growing area of study
 - ◆ Increasing impact on
 - ◆ Financial markets
 - ◆ Financial intermediation
 - ◆ Related regulatory issues and governance
 - ◆ Claessens, Glaessner, and Klingebiel (2000, 2001), Long (2000), Banks (2001), Turner (2001)
- Particular emphasis
 - ◆ Conceptualization
 - ◆ Role of networks in the transformations
 - ◆ McAndrews and Stefanidis (2000), Allen, Hawkins, and Seto (2001), Economides (2001), and Nagurney and Dong (2002)

Literature Survey for Risk Management with Variable Weights

- Behavior of investors
 - ◆ Maximize the expected return
 - ◆ Minimize the risk
- Markowitz (1952, 1959)
 - ◆ Mean and variance
- Numerous extension (Sharpe (1971), Stone (1973), Young (1998))
 - ◆ Equal trade-off between two criteria
- Dong and Nagurney (2001) and Nagurney, Dong, and Mokhtarian (2002)
 - ◆ Variable weights

Research Motivation for Financial Networks with Intermediation

- The financial economy explicitly includes
 - ◆ Financial intermediaries
 - ◆ Source agents
 - ◆ Uses of financial funds
- Advances of telecommunications have enormous effect
 - ◆ Financial services
 - ◆ Options available for financial transactions
 - ◆ Distribution channels
 - ◆ New types of products
 - ◆ Role of financial intermediaries
- Construction of a unified, quantifiable framework
- Variable weights to catch the risk attitudes of investors

Novelty of My Research

- Nagurney and Ke (2001a)
 - ◆ Published in *Quantitative Finance*
 - ◆ First publication that modeled the financial network with intermediation quantifiably.
- Nagurney and Ke (2001b)
 - ◆ Disequilibrium dynamics
 - ◆ Foundation for further study
- Nagurney and Ke (2003)
 - ◆ Published in *Quantitative Finance*
 - ◆ First considered the impact of electronic transaction
 - ◆ Capture competition within a tier of nodes and cooperation between tiers.
- Nagurney and Ke (2004)
 - ◆ First studied the bicriteria decision-making problem in multitiered financial networks.

Chapter 2: Overview of Methodologies

- Introduction
- Methodologies
 - ◆ Variational inequality theory
 - ◆ Projected dynamical systems
- Multilevel network perspective for supply chain
- Financial networks with intermediation
- Conclusion

- Definition of variational inequality problem:

To determine a vector $X^* \in \mathcal{K} \subset \mathcal{R}^n$ such that

$$F(X^*)^T \cdot (X - X^*) \geq 0, \quad \forall X \in \mathcal{K}$$

- Qualitative properties
 - ◆ Existence
 - ◆ Monotonicity
 - ◆ Lipschitz continuity
 - ◆ Uniqueness

Chapter 2: Overview of Methodologies

- Introduction
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- Conclusion

■ Algorithms

- ◆ Projection method
 - ◆ Initialization
 - ◆ Computation

$$[X^\tau + \alpha G^{-1} F(X^{\tau-1}) - X^{\tau-1}]^T$$

$$\cdot [X - X^\tau] \geq 0, \quad \forall X \in \mathcal{K}$$

- ◆ Convergence verification

Chapter 2: Overview of Methodologies

- Introduction
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- ◆ Modified projection method
 - ◆ Initialization
 - ◆ Computation

$$[\bar{X}^\tau + \alpha F(X^{\tau-1}) - X^{\tau-1}]^T$$

$$\cdot [X - \bar{X}^\tau] \geq 0, \quad \forall X \in \mathcal{K}.$$

- ◆ Adaptation

$$[X^\tau + \alpha F(\bar{X}^\tau) - X^{\tau-1}]^T$$

$$\cdot [X - X^\tau] \geq 0, \quad \forall X \in \mathcal{K}$$

- ◆ Convergence verification

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■ Definition of Projected Dynamical Systems

Given $X \in \mathcal{K}$ and $v \in F^n$, define the projection of v at X (with respect to K) by

$$\pi_{\mathcal{K}}(X, v) = \lim_{\delta \rightarrow 0} \frac{P_{\mathcal{K}}(X + \delta v) - X}{\delta}$$

And $P_{\mathcal{K}}(X) = \operatorname{argmin}_{X' \in \mathcal{K}} \|X' - X\|$.

Definition: *The projected dynamical system (PDS) is defined as map: $\Phi: \mathcal{K} \times \mathcal{R} \mapsto \mathcal{K}$ where: $\Phi(X, t) = \phi_X(t)$ solves the initial value problem:*

$$\dot{\phi}_X(t) = \pi_{\mathcal{K}}(\phi_X(t), -F(\phi_X(t))),$$

$$\phi_X(0) = X$$

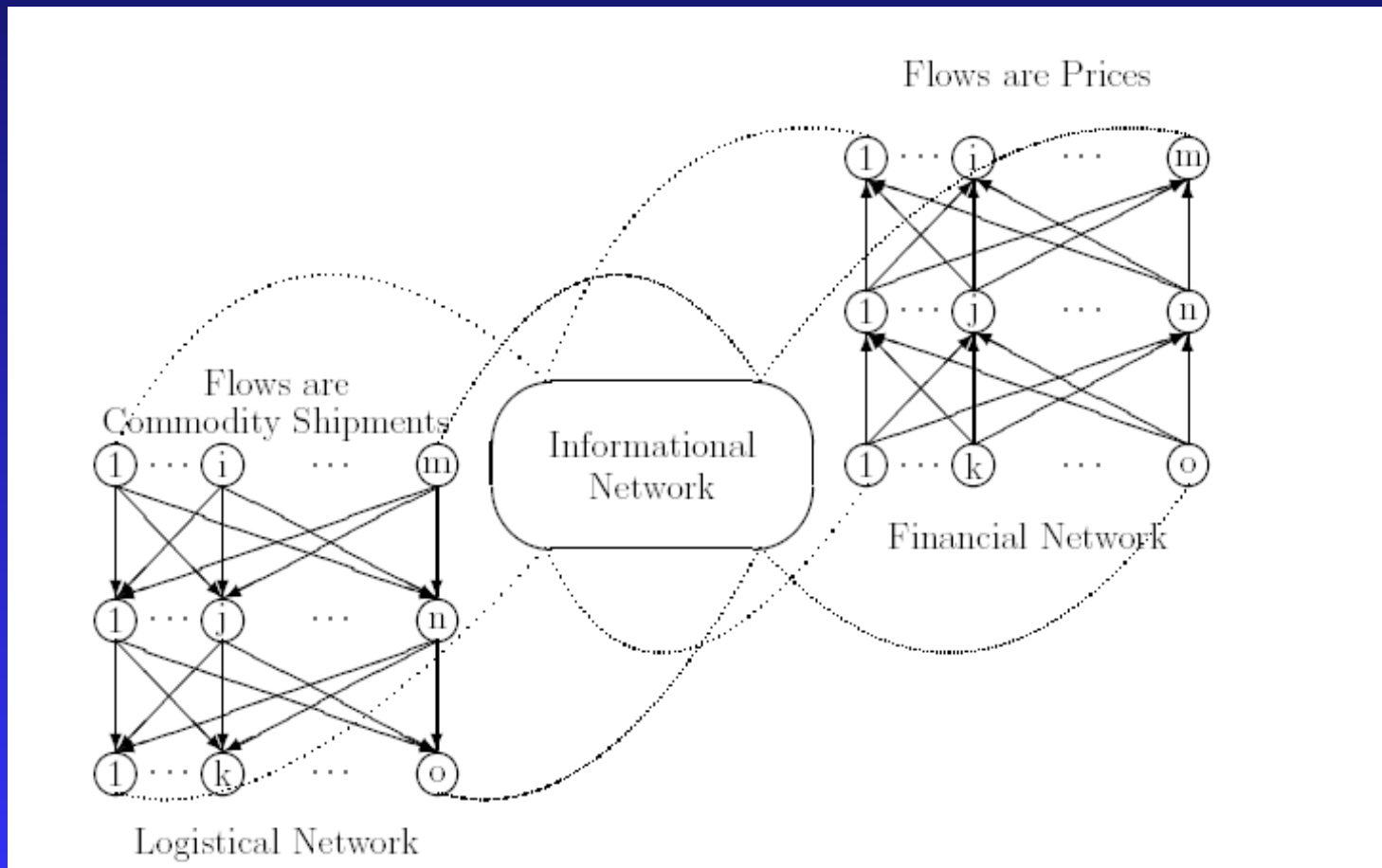
Chapter 2: Overview of Methodologies

- Introduction
- Methodologies
 - ◆ Variational inequality theory
 - ◆ Projected dynamical systems
- Multilevel network perspective for supply chain
- Financial networks with intermediation
- Conclusion
- Qualitative properties
 - ◆ Existence, uniqueness, and continuous dependence (Theorem 2.8)
 - ◆ Lipschitz continuity (Theorem 2.9)
 - ◆ Stability analysis

Chapter 2: Overview of Methodologies

- Introduction
- Methodologies
 - ◆ Variational inequality theory
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- Conclusion
- Algorithm (the Euler method)
 - ◆ Initialization
 - ◆ Set the sequence $\{\alpha_\tau\}$
 - ◆ Computation
$$X^\tau = P_{\mathcal{K}}(X^{\tau-1} - \alpha_{\tau-1}F(X^{\tau-1}))$$
 - ◆ Convergence verification

Chapter 3: Dynamics of Supply Chains: A Multilevel Network Perspective



Notable Features

- Within the same network:
- Logistical network
 - ◆ Depict the physical flows of products
 - ◆ Examine the relationships of various individual entities
- Informational network
 - ◆ Processing information
 - ◆ Demand forecasting information
 - ◆ Management information
 - ◆ Price information
- Financial network
 - ◆ Prices

The Dynamics

- The quantity flows over logistical network
 - ◆ The firms adjust commodity shipment
 - ◆ The consumers adjust consumption based on prices
 - ◆ The retailers operating between them
- The prices over financial network

The Projected Dynamical System

- The equilibrium point (the variational inequality formulation)
- Qualitative properties
 - ◆ Monotonicity
 - ◆ Lipschitz continuity
 - ◆ Existence and uniqueness
 - ◆ Stability of the system
- A discrete-time adjustment process
 - ◆ The Euler method
 - ◆ Computation of the commodity shipments at each iteration
 - ◆ Computation of the prices at each iteration

Numerical Examples

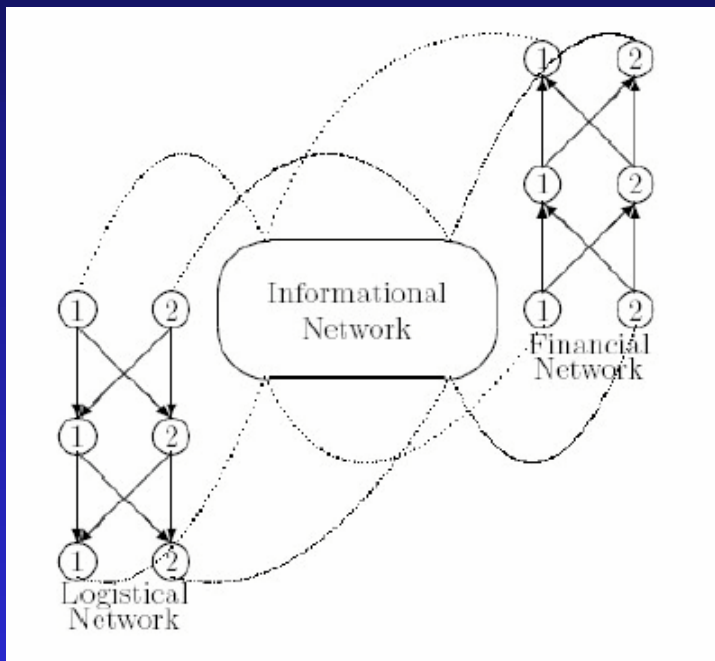


Figure 3.2: Multilevel Network for Examples 3.1 and 3.2

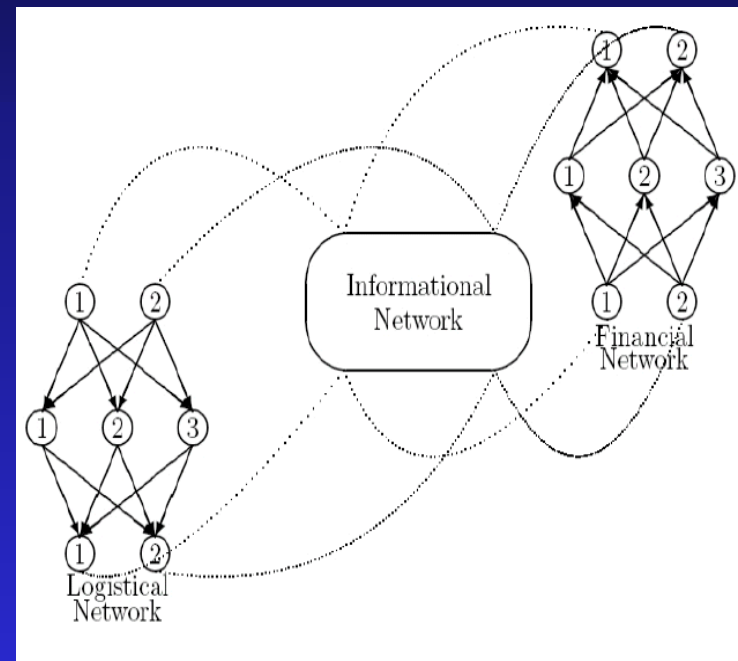


Figure 3.3: Multilevel Network for Example 3.3

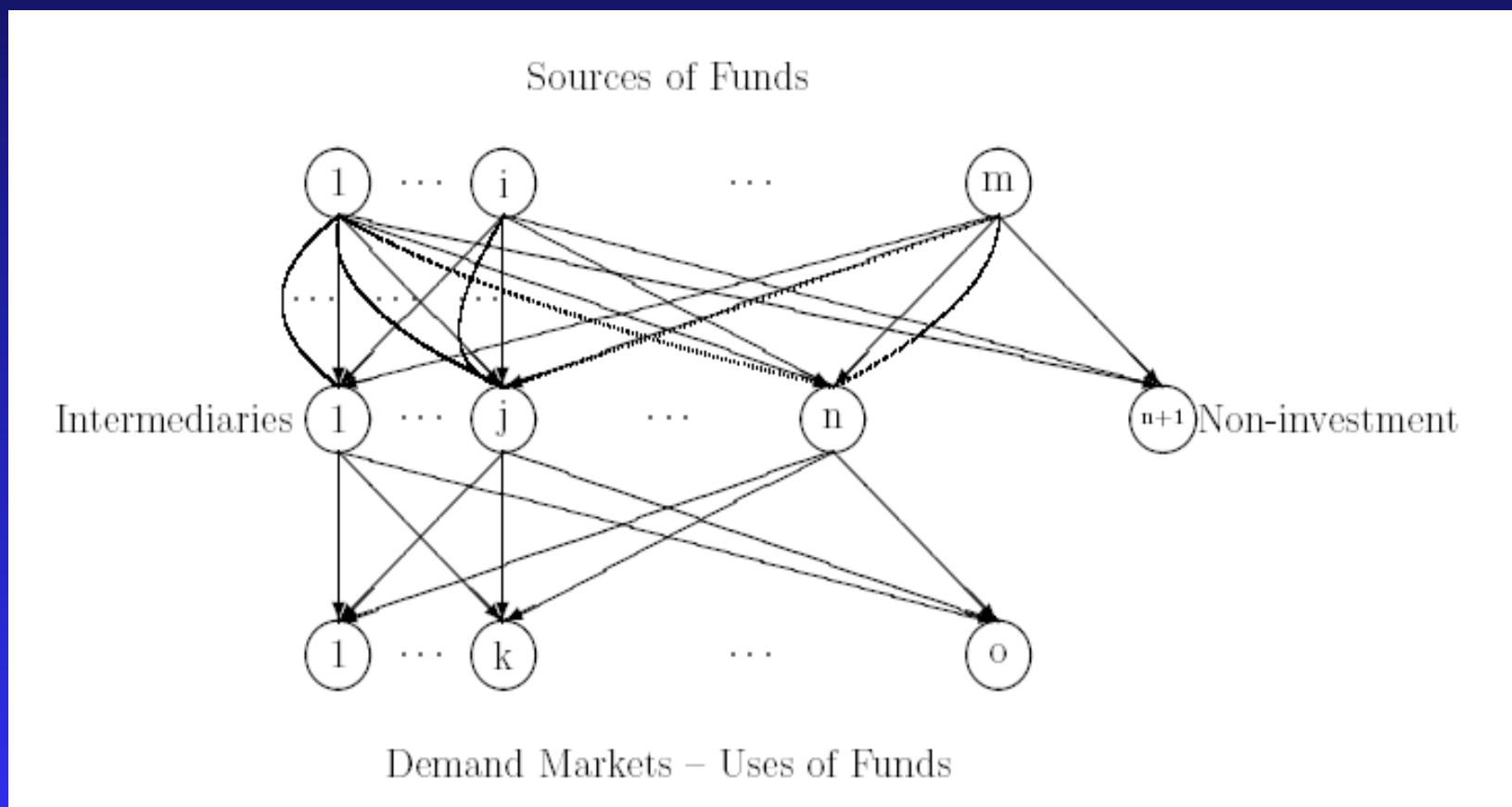
Input Data for Examples

<p>The production cost functions of the manufacturers</p>	<p>Example 3.1: $f_i(q) = 2.5q_i^2 + q_1q_2 + 2q_i$ Example 3.2: $f_1(q) = 2.5q_1^2 + q_1q_2 + 12q_1$ Example 3.3: $f_2(q) = 2.5q_2^2 + q_1q_2 + 12q_2$</p>
<p>The transaction cost functions faced by the manufacturers and associated with retailers</p>	<p>Example 3.1: $c_{ij}(Q^1) = .5q_{ij}^2 + 3.5q_{ij}^1$ Example 3.2: $c_{1j}(Q^1) = q_{1j}^2 + 3.5q_{1j}^1$ Example 3.3: $c_{i3}(Q^1) = .5q_{i3}^2 + 5q_{i3}^1$</p>
<p>The handling costs of the retailers</p>	$c_j(Q^1) = .5 \left(\sum_{i=1}^2 q_{ij}^1 \right)^2$
<p>The demand functions</p>	$d_1(\rho^3) = -2\rho_1^3 - 1.5\rho_2^3 + 1000$ $d_2(\rho^3) = -2\rho_2^3 - 1.5\rho_1^3 + 1000$
<p>The transaction costs between the retailers and the consumers</p>	$c_{jk}(Q^2) = q_{jk}^2 + 5$

Equilibrium Patterns of the Numerical Examples

			Example 3.1	Example 3.2	Example 3.3	
Flows Q^*	Q^{1*} (q_{ij}^{1*})	q_{11}^{1*}	16.608	14.507	9.243	
		q_{12}^{1*}	16.608	14.507	9.243	
		q_{21}^{1*}	16.608	17.230	13.567	
		q_{22}^{1*}	16.608	17.230	13.567	
		q_{13}^{1*}			14.645	
		q_{23}^{1*}			9.726	
		Q^{2*} (q_{jk}^{2*})	q_{11}^{2*}	16.608	15.869	11.404
	q_{12}^{2*}		16.608	15.869	11.404	
	q_{21}^{2*}		16.608	15.869	11.404	
	q_{22}^{2*}		16.608	15.869	11.404	
	q_{31}^{2*}				12.184	
	q_{32}^{2*}				12.184	
	prices ρ^{3*}		ρ_k^{3*}	ρ_1^{3*}	276.224	276.646
		ρ_2^{3*}		276.224	276.646	275.717

Chapter 4: Financial Networks with Intermediation



Notable Features

- Financial systems in disequilibrium or in equilibrium
- Interactions
 - ◆ Among individual sectors
 - ◆ Each facing own objective function
- Emphasize the advantage of network modeling and computation
- Allowing non-investment
- Consideration of transaction costs

- The behavior and optimality conditions

- ◆ Agents with sources of funds

$$\text{Maximize } U^i(q_i^1) = \sum_{j=1}^n \sum_{l=1}^L \rho_{ijl}^1 q_{ijl}^1 - \sum_{j=1}^n \sum_{l=1}^L c_{ijl}(q_{ijl}^1) - q_i^{1T} V^i q_i^1$$

$$\sum_{j=1}^n \sum_{l=1}^L q_{ijl}^1 \leq S^i$$

- ◆ Intermediaries

$$\text{Maximize } U^j(q_j^2) = \sum_{k=1}^o (\rho_{jk}^2 q_{jk}^2 - c_{jk}(q_{jk}^2)) - c_j(Q^1) - \sum_{i=1}^m \sum_{l=1}^L (\hat{c}_{ijl}(q_{ijl}^1) + \rho_{ijl}^1 q_{ijl}^1) - q_j^{2T} V^j q_j^2$$

Subject to:

$$\sum_{k=1}^o q_{jk}^2 \leq \sum_{i=1}^m \sum_{l=1}^L q_{ijl}^1$$

- ◆ Demand markets

$$\rho_{jk}^{2*} + \hat{c}_{jk}(Q^{2*}) \begin{cases} = \rho_k^{3*}, & \text{if } q_{jk}^{2*} > 0 \\ \geq \rho_k^{3*}, & \text{if } q_{jk}^{2*} = 0 \end{cases}$$

$$d_k(\rho^{3*}) \begin{cases} = \sum_{j=1}^n q_{jk}^{2*}, & \text{if } \rho_k^{3*} > 0 \\ \leq \sum_{j=1}^n q_{jk}^{2*}, & \text{if } \rho_k^{3*} = 0 \end{cases}$$

- Variational inequality formulation

$$\begin{aligned}
 & \sum_{i=1}^m \sum_{j=1}^n \sum_{l=1}^L \left[2V_{z_{jl}}^i \cdot q_i^{1*} + 2V_{z_{il}}^j \cdot q_j^{2*} + \frac{\partial c_{ijl}(q_{ijl}^{1*})}{\partial q_{ijl}^1} + \frac{\partial c_j(Q^{1*})}{\partial q_{ijl}^1} \right. \\
 & \qquad \qquad \qquad \left. + \frac{\partial \hat{c}_{ijl}(q_{ijl}^{1*})}{\partial q_{ijl}^1} - \gamma_j^* \right] \times [q_{ijl}^1 - q_{ijl}^{1*}] \\
 & + \sum_{j=1}^n \sum_{k=1}^o \left[2V_{z_{mL+k}}^j \cdot q_j^{2*} + \frac{\partial c_{jk}(q_{jk}^{2*})}{\partial q_{jk}^2} + \hat{c}_{jk}(Q^{2*}) + \gamma_j^* - \rho_k^{3*} \right] \times [q_{jk}^2 - q_{jk}^{2*}] \\
 & \qquad \qquad \qquad + \sum_{j=1}^n \left[\sum_{i=1}^m \sum_{l=1}^L q_{ijl}^{1*} - \sum_{k=1}^o q_{jk}^{2*} \right] \times [\gamma_j - \gamma_j^*] \\
 & + \sum_{k=1}^o \left[\sum_{j=1}^n q_{jk}^{2*} - d_k(\rho^{3*}) \right] \times [\rho_k^3 - \rho_k^{3*}] \geq 0, \quad \forall (Q^1, Q^2, \gamma, \rho^3) \in \mathcal{K},
 \end{aligned}$$

- Qualitative properties

- ◆ Uniqueness
- ◆ Existence

- The algorithm

- ◆ Modified projection method
- ◆ Computation of financial flow of products and prices

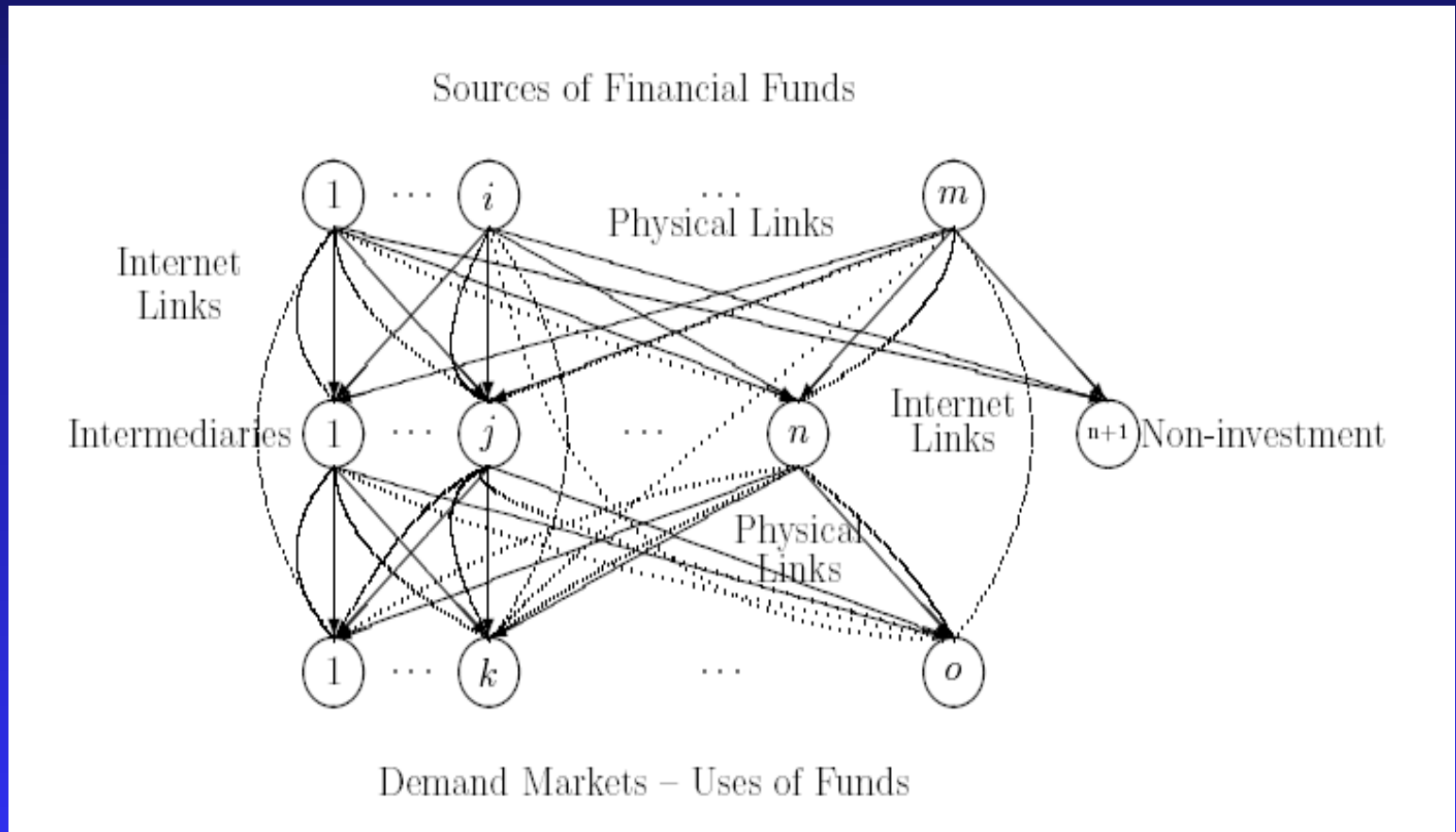
- Numerical examples

Chapter 5: Dynamics of Financial Networks with Intermediation

- Network structure
- The dynamics
 - ◆ Financial flows
 - ◆ Source agents adjust investment in various instruments
 - ◆ Intermediaries adjust transactions
 - ◆ Consumers obtain the financial products
 - ◆ Prices over time

- The projected dynamical system
- The equilibrium point (the variational inequality formulation)
- Qualitative properties
 - ◆ Existence and uniqueness
 - ◆ Stability of the system
- A discrete-time adjustment process
 - ◆ The Euler method
 - ◆ Computation of financial flows and prices at each iteration
- Numerical examples
 - ◆ Verify that the set of stationary points of PDS coincides with the set of solutions to the VI problem

Chapter 6: Dynamics of Financial Networks with Electronic Transactions



Notable Features

- Electronic transactions
- Source agents can transact:
 - ◆ With the intermediaries either physically or electronically
 - ◆ With the consumers in an electronic manner
- Intermediaries transact with the consumers
 - ◆ Physically
 - ◆ Electronically

- The behavior and optimality conditions
 - ◆ Agents with sources of funds
 - ◆ Maximize the net revenue
 - ◆ Minimize the risk
 - ◆ Intermediaries
 - ◆ Maximize the net revenue
 - ◆ Minimize the risk
 - ◆ Demand markets
- Variational inequality formulation
- The dynamics
 - ◆ The projected dynamical system

- Qualitative properties
 - ◆ Uniqueness
 - ◆ Existence
 - ◆ Lipschitz continuity
 - ◆ Stability of the system
- The algorithm
 - ◆ The Euler method
 - ◆ Computation of financial flows and prices
- Numerical examples

Numerical Examples

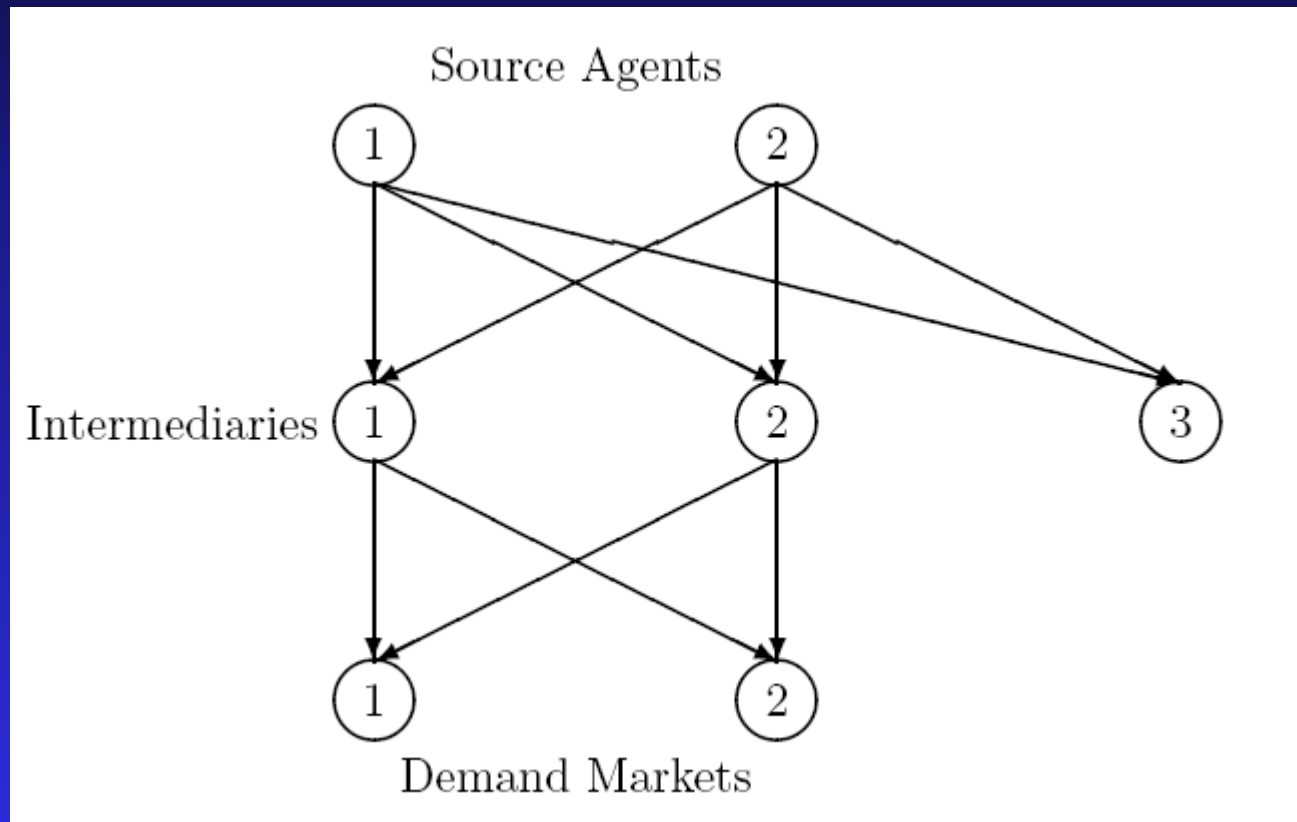


Figure: The Financial Network Structure of Example 6.1

Numerical Examples (Cont.)

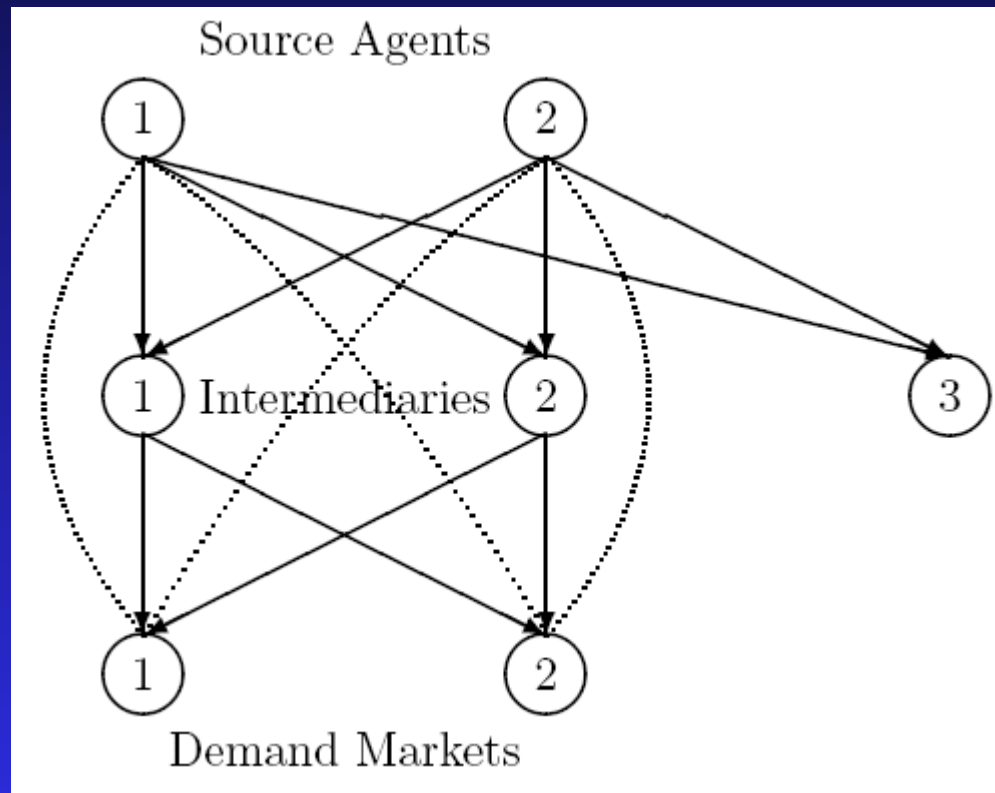


Figure: The Financial Network Structure of Example 6.2

Numerical Examples (Cont.)

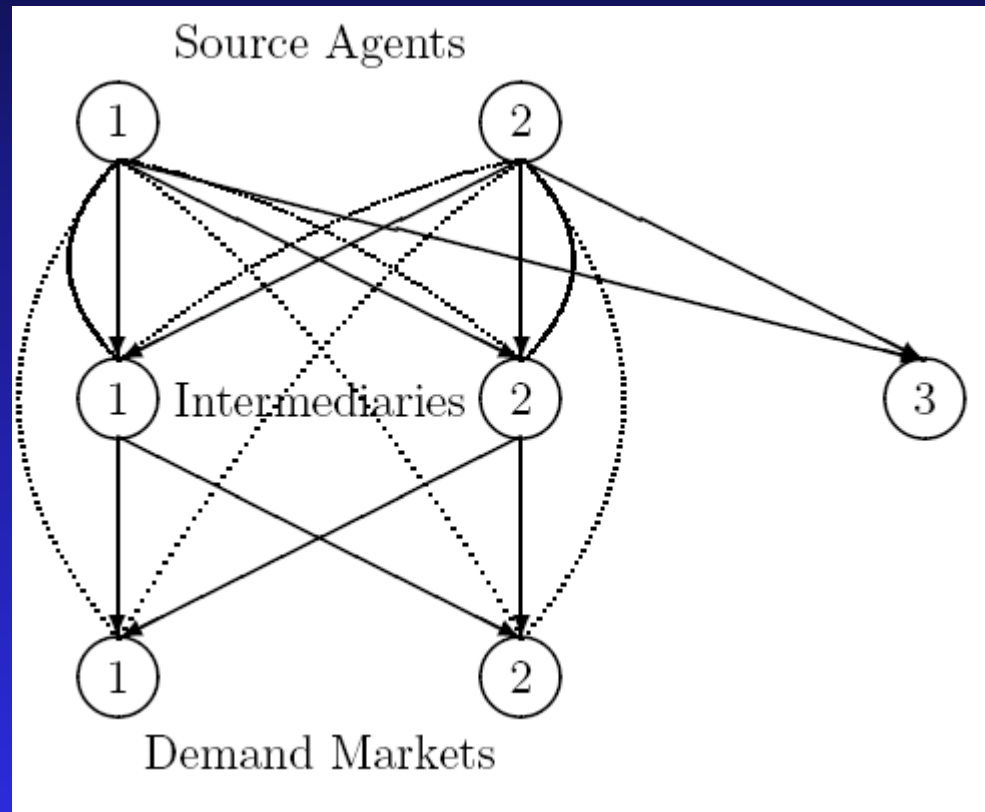


Figure: The Financial Network Structure of Example 6.3

Input Data for Examples 6.1-6.3

The transaction cost functions of the source agents	$c_{ijl}(q_{ijl}^1) = 0.5(q_{ijl}^1)^2 + 3.5q_{ijl}^1$
The handling costs of the intermediaries	$c_j(Q^1) = 0.5\left(\sum_{i=1}^2 q_{ij1}^1\right)^2$
The transaction costs of the intermediaries associated with transacting with source agents	$\hat{c}_{ijl}(q_{ijl}^1) = 1.5(q_{ijl}^1)^2 + 3q_{ijl}^1$
The transaction costs of the consumers transacting with the intermediaries	$\hat{c}_{jkl}(q_{jkl}^2) = q_{jkl}^2 + 5$
The demand functions at the demand markets	$d_1(\rho^3) = -2\rho_1^3 - 1.5\rho_2^3 + 1000$ $d_2(\rho^3) = -2\rho_2^3 - 1.5\rho_1^3 + 1000$

Additional transaction costs for Example 6.2 and 6.3:

The transaction cost functions of the source agents for dealing with demand markets:	$c_{ik}(q_{ik}^3) = 0.5(q_{ik}^3)^2 + q_{ik}^3$
Transaction cost functions from the demand markets:	$\hat{c}_{ik}(Q^2, Q^3) = q_{ik}^3 + 1$

Based on Example 6.2, the additional transaction costs for Example 6.3 are:

The transaction costs of the source agents transacting with the financial intermediaries electronically:	$c_{ij2}(q_{ij2}^1) = 0.5(q_{ij2}^1)^2 + 0.5q_{ij2}^1$
Transaction costs of the intermediaries transacting with sources electronically:	$\hat{c}_{ij2}(q_{ij2}^1) = 0.5(q_{ij2}^1)^2 + 0.5q_{ij2}^1$

Table 6.1: Equilibrium Patterns of the Numerical Examples

			Example 6.1	Example 6.2	Example 6.3
Flows Q^*	Q^{1*} (q_{ijl}^{1*})	q_{111}^{1*}	10	4.8	3.09
		q_{121}^{1*}	10	4.8	3.09
		q_{211}^{1*}	10	4.8	3.09
		q_{221}^{1*}	10	4.8	3.09
		q_{112}^{1*}			3.33
		q_{122}^{1*}			3.33
		q_{212}^{1*}			3.33
	q_{222}^{1*}			3.33	
	Q^{2*} (q_{jkl}^{2*})	q_{111}^{2*}	10	4.8	6.42
		q_{121}^{2*}	10	4.8	6.42
		q_{211}^{2*}	10	4.8	6.42
		q_{221}^{2*}	10	4.8	6.42
	Q^{3*} (q_{ik}^{3*})	q_{11}^{3*}		5.2	3.57
q_{12}^{3*}			5.2	3.57	
q_{21}^{3*}			5.2	3.57	
q_{22}^{3*}			5.2	3.57	
Lagrange Multipliers	γ_j^*	γ_1^*	245.02	260.59	255.72
		γ_2^*	245.02	260.59	255.72
Prices ρ^{3*}	ρ_k^{3*}	ρ_1^{3*}	280	280	280
		ρ_2^{3*}	280	280	280

Chapter 7: Financial Networks with Intermediation: Risk Management with Variable Weights

Why variable weights?

In decision-making under uncertainty,

Risk attitude → Decisions → Expected monetary payoffs

To reveal a sector's preference over the return and the risk, we reconstruct the objective functions to include the variable weights.

Notable Features

- Each source agent
 - ◆ Maximize net revenue z_{1i}^1
 - ◆ Minimize risk z_{2i}^1
- Each intermediary
 - ◆ Maximize net revenue z_{1j}^2
 - ◆ Minimize risk z_{2j}^2
- Essence: "How much achievement on one objective is the decision-maker willing to give up in order to improve achievement on another objective?"
- Criterion-dependent weight w_{2I}^t
 - ◆ For source agents: $I=i$; $i=1,\dots,m$, and $t=1$
 - ◆ For intermediaries: $I=j$; $j=1,\dots,n$, and $t=2$

- Risk-penalizing value function

- ◆ Source Agents

$$\text{Maximize } U^i(q_i^1) = \sum_{j=1}^n \sum_{l=1}^L (\rho_{ijl}^1 q_{ijl}^1 - c_{ijl}(q_{ijl}^1)) - w_{2i}^1(r^i(q_i^1))r^i(q_i^1)$$

- ◆ Intermediaries

$$\begin{aligned} \text{Maximize } U^j(q_j^2) = & \sum_{k=1}^o (\rho_{jk}^2 q_{jk}^2 - c_{jk}(q_{jk}^2)) - c_j(Q^1) - \sum_{i=1}^m \sum_{l=1}^L (\hat{c}_{ijl}(q_{ijl}^1) + \rho_{ijl}^1 q_{ijl}^1) \\ & - w_{2j}^2(r^j(q_j^2))r^j(q_j^2), \end{aligned} \quad (7.16)$$

Subject to:
$$\sum_{k=1}^o q_{jk}^2 \leq \sum_{i=1}^m \sum_{l=1}^L q_{ijl}^1$$

- ◆ Demand Markets

- Variational inequality formulation
- Qualitative properties
 - ◆ Uniqueness
 - ◆ Existence
- The algorithm
 - ◆ Modified projection method
 - ◆ Computation of financial flow of products and prices
- Numerical examples

Input Data for Examples 7.1-7.3

The transaction cost functions of the source agents	$c_{ijl}(q_{ijl}^1) = 0.5(q_{ijl}^1)^2 + 3.5q_{ijl}^1$
The handling costs of the intermediaries	$c_j(Q^1) = 0.5\left(\sum_{i=1}^2 q_{ij1}^1\right)^2$
The transaction costs of the intermediaries associated with transacting with source agents	$\hat{c}_{ijl}(q_{ijl}^1) = 1.5(q_{ijl}^1)^2 + 3q_{ijl}^1$
The transaction costs of the consumers associated with transacting with the intermediaries	$\hat{c}_{jkl}(q_{jkl}^2) = q_{jkl}^2 + 5$
The demand functions at the demand markets	$d_1(\rho^3) = -2\rho_1^3 - 1.5\rho_2^3 + 1000$ $d_2(\rho^3) = -2\rho_2^3 - 1.5\rho_1^3 + 1000$

Weights in Examples 7.2 and 7.3

- Example 7.2: weights associated with the source agents transacting with the first financial intermediary were doubled
- Example 7.3: $w_{2i}^1 = z_{2i}^1$ for $i = 1, 2$.

Table 7.1: Equilibrium Patterns of the Numerical Examples

			Example 7.1	Example 7.2	Example 7.3
Flows Q^*	Q^{1*}	q_{111}^{1*}	10	9.29	3.10
	(q_{ijl}^{1*})	q_{121}^{1*}	10	10.71	3.10
		q_{211}^{1*}	10	9.29	3.10
		q_{221}^{1*}	10	10.71	3.10
		Q^{2*}	q_{11}^{2*}	10	9.29
	(q_{jk}^{2*})	q_{12}^{2*}	10	9.29	3.10
		q_{21}^{2*}	10	10.71	3.10
		q_{22}^{2*}	10	10.71	3.10
Lagrange Multipliers	γ_j^*	γ_1^*	245.00	247.14	269.63
	γ^*	γ_2^*	245.00	242.86	269.63
Prices ρ^{3*}	ρ_k^{3*}	ρ_1^{3*}	280	280	283.94
		ρ_2^{3*}	280	280	283.94

Comparison of the Two Areas

■ Similarities

- ◆ Network structure
- ◆ Variables
- ◆ Cost structure
- ◆ Methodology

■ Differences

- ◆ Construction
- ◆ Flows on the links
- ◆ Direction of flows
- ◆ Behavior of top two tiers
- ◆ Role of middle tier
- ◆ Constraints

Contributions

- First dynamic multilevel supply chain model within context of network equilibrium (Nagurney, Ke, Cruz, Hancock, and Southworth (2002))
- First financial network study to explicitly include the financial intermediaries quantifiably (Nagurney and Ke (2001a))
- First financial network study to consider the impact of electronic transactions quantifiably (Nagurney and Ke (2003))
- Incorporate the dimension of the explicit dynamic behavior of the various financial agents as well as the price dynamics
- Inclusion of variable weights brings the model closer to the “reality” of financial transactions

Future Research

- Empirical study
 - ◆ Multilevel supply chain network model
 - ◆ Theoretical models of financial networks
- Informational Networks
 - ◆ Vary with respect to
 - ◆ Timelines
 - ◆ Quality of information
 - ◆ Different costs
- Introduction of variable weights into current
 - ◆ Supply chain network models
 - ◆ International financial network models
- Additional criteria

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