Network Economics of Cyber Crime with Applications to Financial Service Organizations

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We acknowledge support from the Advanced Cyber Security Center (ACSC) for funding our project, *Cybersecurity Risk Analysis and Investment Optimization*.



The Project Synopsis:

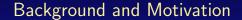
The vision of this project was to develop:

- rigorous models for cybersecurity risk,
- models for costs and benefits of various cybersecurity technologies,
- techniques for integrating these models into higher level models that account for other risks and risk management expenditures.

Our team is interdisciplinary and comprised of UMass Amherst faculty and an IT security operations professional.

Outline of Presentation

- ► Background and Motivation
 - • Internet
 - • Financial Networks
- ► Cyber Crime and Network Economics
- ► The Model
- ► Summary and Conclusions



The Internet

• The Internet has transformed the ways in which individuals, groups, and organizations communicate, obtain information, access entertainment, and conduct their economic and social activities.



The Internet

In 2012, there were over 2.4 billion users



Data source: Internet World Stats

www.pingdom.com

The advances in information technology and globalization have further shaped today's financial world into a complex network, which is characterized by distinct sectors, the proliferation of new financial instruments, and with increasing international diversification of portfolios.

As pointed out by Sheffi (2005) in his book, *The Resilient Enterprise*, one of the main characteristics of disruptions in networks is "the seemingly unrelated consequences and vulnerabilities stemming from global connectivity."

Financial service firms were heavily impacted by **the recession** and are also dealing with **increasing numbers of cyber attacks**.

In 2008 and 2009, the world reeled from the effects of the financial credit crisis; leading financial services and banks closed (including the investment bank Lehman Brothers), others merged, and the financial landscape was changed for forever.

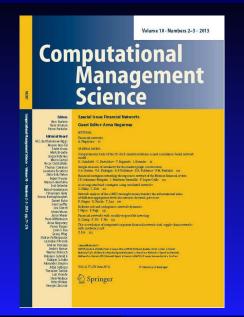
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The domino effect of the U.S. economic troubles rippled through overseas markets and pushed countries such as Iceland to the verge of bankruptcy.

It is crucial for the decision-makers in financial systems (managers, executives, and regulators) to be able **to identify a financial network's vulnerable components** to protect the functionality of the network.

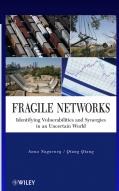
Financial networks, as extremely important infrastructure networks, have a great impact on the global economy, and their study has recently also attracted attention from researchers in the area of complex networks.

- V. Boginski, S. Butenko, and P. M. Pardalos, 2005. Statistical Analysis of Financial Networks. *Computational Statistics and Data Analysis* 48(2), 431443.
- V. Boginski, S. Butenko, and P. M. Pardalos, 2003. On Structural Properties of the Market Graph. In *Innovations in Financial and Economic Networks*, A. Nagurney (ed.), Edward Elgar Publishers, pp. 28-45.
- G. A. Bautin, V. A. Kalyagin, A. P. Koldanov, P. A. Koldanov, P. M. Pardalos, 2013. Simple measure of similarity for the market graph construction, special issue of *Computational Management Science* on Financial Networks.





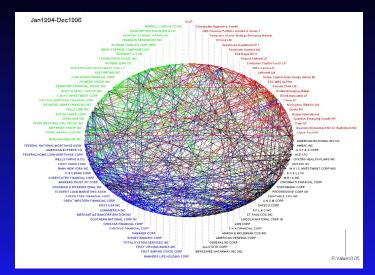




Connectivity and Vulnerability

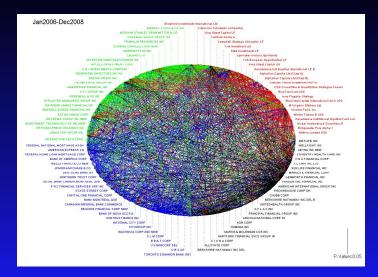
Recent empirical research has shown that connections increase before and during financial crises.

Empirical Evidence - January 1994 - December 1996



Granger Causality Results: Green Broker, Red Hedge Fund, Black Insurer, Blue Bank Source: Billio, Getmansky, Lo, and Pelizzon (2011)

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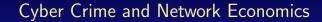


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Nevertheless, there is very little literature that addresses the vulnerability of financial networks.

Our network performance measure for financial networks captures both economic behavior as well as the underlying network/graph structure and the dynamic reallocation after disruptions.

The results are contained in the paper, "Identification of Critical Nodes and Links in Financial Networks with Intermediation and Electronic Transactions," A. Nagurney and Q. Qiang, in Computational Methods in Financial Engineering, E. J. Kontoghiorghes, B. Rustem, and P. Winker, Editors, Springer, Berlin, Germany (2008), pp 273-297.



Cyber Crime

• Cyber crimes continue to be quite costly for organizations. The Ponemon Institute (2012) determined that the average annualized cost for 56 benchmarked organizations is \$8.9 million per year, with a range from \$1.4 million to \$46 million each year per company. Last year's average cost per benchmarked organization was \$8.4 million.

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- Cyber crime cost varies by organizational size. Results reveal a positive relationship between organizational size (as measured by enterprise seats) and annualized cost. However, based on enterprise seats, the Ponemon Institute (2012) determined that small organizations incur a significantly higher per capita cost than larger organizations (\$1,324 versus \$305).

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- All industries fall victim to cyber crime, but to different degrees with defense, utilities and energy, and financial service companies experiencing higher costs than organizations in retail, hospitality, and consumer products.

Cyber Crime and Financial Institutions

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Cyber attacks are intrusive and economically costly. In addition, they may adversely affect a companys most valuable asset its reputation.

Cyber Attacks

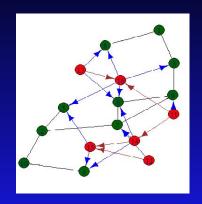
The most costly cyber crimes are those caused by denial of service, malicious insider and web-based attacks. These account for more than 58 percent of all cyber crime costs per organization on an annual basis. Mitigation of such attacks may require enabling technologies, intrusion prevention systems, applications security testing solutions and enterprise solutions.

As noted by Sarnikar and Johnson (2009), a secure financial market system is critical to our national economy, with statistics on incident reports collected and disseminated by the Computer Emergency Response Team (CERT) demonstrating that a disproportionate number of security incidents occur in the financial industry.

With financial service firms providing one of the critical infrastructure networks on which our economy and society depends, it is imperative to be able to identify their vulnerabilities to cyber attacks in a rigorous, quantifiable manner as well as to identify possible synergies associated with information sharing.

Only by capturing the complexities and the underlying behavior can one then mitigate the risk as well as identify where to invest in order to secure the financial networks on which so many of the financial transactions now depend.

Green Nodes represent Institutions Red Nodes the Attackers Red Edges between Attackers can represent collusion or transactions of stolen goods. Black Edges between Institutions can show sharing of information and mutual dependence. Blue Edges between the Attacker and Institution can represent threats and attacks.



We lay the foundation for the development of network economics based models for cyber crime in financial services.

We use, as the framework, spatial network economic models, presenting here a single commodity model.

Both financial services firms as well as hackers are economic

We assume that the firms (as well as the hackers) can be located in different regions of a country or in different countries. Financial service firms may also be interpreted as prey and the hackers as predators.

Commodities or products that the hackers seek to acquire may include: credit card numbers, password information, specific documents, etc.

The financial firms are the producers of these commodities whereas the hackers act as agents and "sell" these products, if they acquire them, at the "going" market prices. There is a "price" at which the hackers acquire the financial commodity from a financial institution and a price at which they sell the hacked product in the demand markets. The former we refer to as the supply price and the latter is the demand price.

In addition, we assume that there is a transaction cost associated between each pair of financial and demand markets for each commodity. These transaction costs can be generalized costs that also capture risk.

In the financial network cyber crime problem, we seek to determine the commodity supply prices, the demand prices, and the hacked product trade flows satisfying the equilibrium condition that, for each financial commodity, the demand price is equal to the supply price plus the transaction cost, if there is "trade" between the pair of financial and demand markets; if the demand price is less than the supply price plus the transaction cost, then there will be no (illicit) trade.

Indeed, if the cyber criminals do not find demand markets for their acquired financial commodities (since there are no consumers willing to pay the price) then there is no economic incentive for them to acquire the financial commodities.

To present another criminal network analogue – consider the market for illegal drugs, with the U.S. market being one of the largest, if not the largest one. If there is no demand for the drugs then the suppliers of illegal drugs cannot recover their costs of production and transaction and the flows of drugs will go to zero.

The framework that we utilize as the foundation for our modeling, analysis, and, ultimately, policy-making recommendations is that of spatial economics and network equilibrium. Background can be found in the books by Nagurney (1999, 2003) with analogues to financial networks made in the book by Nagurney and Siokos (1997)



Figure 1: A bipartite network of the model with financial institutions and demand markets for hacked products

Denote a typical financial institution by i and a typical demand market by j. Let s_i denote the supply of the commodity associated with i and let π_i denote the supply price of the commodity associated with i. Let d_j denote the demand associated with demand market j and let ρ_j denote the demand price associated with demand market j.

Let Q_{ij} denote the possible illicit nonnegative commodity trade flow between the firm and demand market pair (i,j) and let c_{ij} denote the nonnegative unit transaction cost associated with obtaining the product between (i,j).

The market equilibrium conditions, assuming perfect competition, take the following form: For all pairs of firms and demand markets $(i,j): i=1,\ldots,m; j=1,\ldots,n$:

$$\pi_i + c_{ij} \left\{ egin{array}{ll} =
ho_j, & ext{if} & Q_{ij}^* > 0 \ \geq
ho_j, & ext{if} & Q_{ij}^* = 0. \end{array}
ight.$$

The condition (1) states that if there is illicit trade between a market pair (i,j), then the supply price at i plus the transaction cost between the firm and demand market pair must be equal to the demand price at demand market j in equilibrium; if the supply price plus the transaction cost exceeds the demand price, then there will be no illicit trade between the market pair.

The feasibility conditions must hold for every i and j:

$$s_i = \sum_{j=1}^n Q_{ij} \tag{2}$$

and

$$d_j = \sum_{i=1}^m Q_{ij}. (3)$$

(2) and (3) state that the markets clear and that the supply at each supply market is equal to the sum of the financial commodity flows to all the demand markets. Also, the demand at a demand market must be satisfied by the sum of the commodity shipments from all the supply markets. Let K denote the closed convex set where $K \equiv \{(s, Q, d) | (2) \text{ and } (3) \text{ hold} \}$.

The supply price, demand price, and transaction cost structure is now discussed. Assume that the commodity price associated with a firm may depend upon the supply of the commodity at every firm, that is,

$$\pi = \pi(s) \tag{4}$$

where π is a known smooth function.

Similarly, the demand price associated with a demand market may depend upon, in general, the demand of the commodity at every demand market, that is,

$$\rho = \rho(d) \tag{5}$$

where ρ is a known smooth function.

The transaction cost between a pair of supply and demand markets may, in general, depend upon the shipments of the commodity between every pair of markets, that is,

$$c = c(Q) \tag{6}$$

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The Variational Inequality Formulation

We now present the variational inequality formulation of the equilibrium conditions (1).

Theorem 1. A commodity production, shipment, and consumption pattern $(s^*, Q^*, d^*) \in K$ is in equilibrium if and only if it satisfies the variational inequality problem:

$$\pi(s^*)\cdot(s-s^*)+c(Q^*)\cdot(Q-Q^*)-\rho(d^*)\cdot(d-d^*)\geq 0, \quad \forall (s,Q,d)\in K.$$
(7)

Qualitative Properties

Variational inequality (7) may be put into the standard form (1) by defining the vector $x \equiv (s, Q, d) \in R^{m+mn+n}$ and the vector $F(x)^T \equiv (\pi(s), c(Q), -\rho(d))$ which maps R^{m+mn+n} into R^{m+mn+n} .

In order to simplify the qualitative analysis, a simple calculation yields that F(x) is a partitionable function of order 3 (cf. Nagurney (1999)). Hence, immediately one can state the following result.

Theorem 2. F(x) as defined above is monotone, strictly monotone, or strongly monotone if and only if $\pi(s)$, c(Q), and $\rho(d)$ are each monotone, strictly monotone, or strongly monotone in s, Q, d, respectively.

Qualitative Properties

Since the feasible set K is not compact, existence of an equilibrium pattern (s^*, Q^*, d^*) does not immediately follow. Nevertheless, it follows from the standard theory of variational inequalities that if π , c, and ρ are strongly monotone, then existence and uniqueness of the equilibrium production, flow, and consumption pattern are guaranteed.



Figure 2: Example Network Topology

The supply price functions are:

$$\pi_1(s) = 5s_1 + s_2 + 2, \quad \pi_2(s) = 2s_2 + s_1 + 3.$$

The transaction cost functions are:

$$c_{11}(Q) = Q_{11} + .5Q_{12} + 1, \quad c_{12}(Q) = 2Q_{12} + Q_{22} + 1.5,$$

 $c_{21}(Q) = 3Q_{21} + 2Q_{11} + 15, \quad c_{22}(Q) = 2Q_{22} + Q_{12} + 10.$

The demand price functions are:

$$\rho_1(d) = -2d_1 - d_2 + 28.75, \quad \rho_2(d) = -4d_2 - d_1 + 41.$$

The equilibrium supply, shipment, and consumption pattern is then given by:

$$s_1^*=3,\quad s_2^*=2,$$
 $Q_{11}^*=1.5,\quad Q_{12}^*=1.5,\quad Q_{21}^*=0,\quad Q_{22}^*=2,$
 $d_1^*=1.5\quad d_2^*=3.5.$

The incurred equilibrium supply prices, costs, and demand prices are:

$$\pi_1=19,\quad \pi_2=10,$$
 $c_{11}=3.25,\quad c_{12}=6.5,\quad c_{21}=18,\quad c_{22}=15.5,$ $ho_1=22.25,\quad
ho_2=25.5.$

Firm 2 does not "trade" with Demand Market 1. This is due, in part, to the high fixed cost associated with trading between this market pair. Hence, one can interpret this as corresponding to a sufficiently high transaction cost (which can also capture in a generalized setting, the risk of being caught).

The above single commodity model we have generalized to multiple financial commodities.

In addition, we have included a variety of policy interventions

We have solved problems of this type using variational inequality algorithms with more than 250,000 variables.

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- The model that we developed was a spatial price equilibrium model in which producers are the financial service firms and consumers are the hackers/attackers.
- We have also developed extensions of the model to include multiple commodities (financial products) as well as policy interventions in the form of price supports to make, for example, the supply rice "high" and hence Anna Nagurney, Wayne Burleson, Mila Sherman, Senay Solak, Network Economics of Cyber Crime

THANK YOU!



For more information, see: http://supernet.isenberg.umass.edu