Labor and Supply Chain Networks: It's All About People

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Thanks also to the Local Organizing and the Program Committees!

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This talk is dedicated to essential workers, who have sustained us in the COVID-19 pandemic.



I also acknowledge all the freedom-loving people on the planet, including those fighting for their freedom in Ukraine.

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Outline of Presentation

- Background and Motivation
- Optimization and Supply Chain Network Models with Labor
 - Food
 - Medical Supplies
- Methodology The Variational Inequality Problem
- Game Theory and Supply Chain Network Models with Labor
 - Food and Labor Disruptions
- Resilience of Supply Chain Networks
- Dealing with the Media and Impacting Policy

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Background and Motivation

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I Work on the Modeling of Network Systems



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Much of My Recent Research Has Been on Supply Chains



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A Multidisciplinary Approach

In our research on perishable and time-sensitive product supply chains, we utilize results from physics, chemistry, biology, and medicine in order to capture the perishability of various products over time from healthcare products such as blood, medical nucleotides, vaccines and pharmaceuticals to food.

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It's All About People

A major research theme of ours in the COVID-19 pandemic is the inclusion of labor in supply chains, using optimization and game theory. This research is also very relevant with Russia's war against Ukraine.



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Optimization and Supply Chain Network Models with Labor

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Research and Publications

"Perishable Food Supply Chain Networks with Labor in the Covid-19 Pandemic," A. Nagurney, in: *Dynamics of Disasters -Impact, Risk, Resilience, and Solutions*, I.S. Kotsireas, A. Nagurney, P.M. Pardalos, and A. Tsokas, Editors, Springer Nature Switzerland AG, 2021, pp 173-193.



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Perishable Food Supply Chain Network Model with Labor



Our findings include:

- The lack of labor on a single link, even a freight one, may significantly negatively impact a food firm.
- Preserving productivity in all utilized supply chain network economic activities is critical since the impact of a drastic reduction can severely reduce profits.
- Adding more direct sales, whether at farmers' markets or nearby farm stands, may help a food firm in a pandemic.
- Also, if a firm enhances its marketing so as to have consumers be willing to pay a higher price for its fresh produce, major profit increases can occur.

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This Research Is Highly Relevant to the War On Ukraine

On February 24, 2022, Russia began a major invasion of Ukraine, a sovereign, democratic nation.

• Ukraine is the breadbasket of the world with major exports of wheat, corn, barley, and sunflower oil. Many countries, including MENA ones (Middle Eastern and North African countries) depend on agricultural products from Ukraine.

• The war has disrupted trade due to blockages of ports on the Black Sea and the Azov Sea and the mining of seas and has affected shipping options.

• The price of seeds has risen, plus the prices of fuel and fertilizer.

• Having enough labor to plant and harvest will also be challenging and getting the products to market and points of demand.

• The World Food Programme used to buy 50% of its wheat from Ukraine.

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A. Nagurney, "Optimization of Supply Chain Networks with Inclusion of Labor: Applications to Covid-19 Pandemic Disruptions," International Journal of Production Economics 235 (2021), 108074.

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Optimization of supply thirds resoration of thirds Applications.
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The modeling framework considers first elastic demands for a product and then fixed demands, coupled with distinct types of labor capacities in order to capture the availability of this valuable resource in a pandemic, as well as possible flexibility.

The supply chain network framework includes electronic commerce and is relevant to many different supply chain applications including protective personal and medical equipment.

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The model considers three sets of labor constraints, of increasing flexibility of movement.

- In the first set, each supply chain link has an upper bound of available labor. Labor is is not free to move to other production sites, nor to other distribution centers, or assist in freight service provision.
- In the second set, labor is free to move across a supply chain set of network economic activities (such as production, or transportation, or storage, and, finally, distribution). There is a capacity of labor associated with each such "tier" of supply chain links. Those who have skills in production, or in distribution, etc., may be reallocated. This has been happening in freight service provision, for example, during the Covid-19 pandemic.
- In the third set, labor is free to move across all the supply chain network economic activities, and there is a single capacity. McKinsey & Company noted this is a means towards resilience and returning the supply chain to effectiveness while reenvisioning and reforming.

Our findings include:

- Having appropriate healthcare pandemic mitigation processes and procedures in place is essential to continuing operations. With even one of the two manufacturing plants closed, the can prices rise at the demand markets.
- Reduction in labor availability can result in a significant increase in product prices at the consumer level.
- Even in the case of reduced labor availability, electronic commerce can result in increased profits.
- Having the flexibility of labor being able to be reallocated across supply chain network activities can enable enhanced profits.

Methodology - The VI Problem

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We utilize the theory of variational inequalities for the formulation, analysis, and solution of both centralized and decentralized supply chain network problems.

Definition: The Variational Inequality Problem

The finite-dimensional variational inequality problem, $VI(F, \mathcal{K})$, is to determine a vector $X^* \in \mathcal{K}$, such that:

$$\langle F(X^*), X - X^* \rangle \geq 0, \quad \forall X \in \mathcal{K},$$

where F is a given continuous function from \mathcal{K} to \mathbb{R}^N , \mathcal{K} is a given closed convex set, and $\langle \cdot, \cdot \rangle$ denotes the inner product in \mathbb{R}^N .

The vector X consists of **the decision variables** – typically, the flows (products, prices, etc.).

 \mathcal{K} is the **feasible set representing how the decision variables are constrained** – for example, the flows may have to be nonnegative; budget constraints may have to be satisfied; similarly, quality and/or time constraints may have to be satisfied.

The function F that enters the variational inequality represents functions that capture the behavior in the form of the functions such as costs, profits, risk, etc.

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The variational inequality problem contains, as special cases, such mathematical programming problems as:

- systems of equations,
- optimization problems,
- complementarity problems,
- game theory problems, operating under Nash equilibrium,
- and is related to the fixed point problem.

Hence, it is a natural methodology for a spectrum of supply chain network problems from centralized to decentralized ones. Geometric Interpretation of $VI(F, \mathcal{K})$ and a Projected Dynamical System (Dupuis and Nagurney, Nagurney and Zhang)

In particular, $F(X^*)$ is "orthogonal" to the feasible set \mathcal{K} at the point X^* .



Associated with a VI is a Projected Dynamical System, which provides the natural underlying dynamics.

To model the **dynamic behavior of complex networks**, including supply chains, we utilize *projected dynamical systems* (PDSs) advanced by Dupuis and Nagurney (1993) in *Annals of Operations Research* and by Nagurney and Zhang (1996) in our book *Projected Dynamical Systems and Variational Inequalities with Applications*.

Such nonclassical dynamical systems are now being used in: evolutionary games (Sandholm (2005, 2011)),

ecological predator-prey networks (Nagurney and Nagurney (2011a, b)),

even neuroscience (Girard et al. (2008),

dynamic spectrum model for cognitive radio networks (Setoodeh, Haykin, and Moghadam (2012)),

Future Internet Architectures (Saberi, Nagurney, Wolf (2014); see also Nagurney et al. (2015), Marentes et al. (2016)).

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This part of the presentation is based on the paper, "Supply Chain Game Theory Network Modeling Under Labor Constraints: Applications to the Covid-19 Pandemic," A. Nagurney, *European Journal of Operational Research* 293(3) (2021), pp 880-891, in which a game theory model for supply chains with labor was constructed, under three different sets of constraints, building on our previous work.



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Two sets of constraints have labor being shared among the competing supply chain networks of firms/organizations, in which case the governing concept is that of a **Generalized Nash Equilibrium** (rather than a Nash Equilibrium).

The research adds to modeling methodology as well as applications.

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Figure: The Supply Chain Network Topology of the Game Theory Model with Labor

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Game Theory Supply Chain Network Model Notation

Table: Game Theory Supply Chain Network Model Notation

Notation	Definition
L ⁱ	The set of links in firm i 's supply chain network, with L being all the links.
G = [N, L]	the graph of the supply chain network consisting of all nodes N and all links L .
P_k^i	set of paths in firm i 's supply chain network terminating in demand market $k;$ $\forall i,k.$
P ⁱ	set of all n_{pi} paths of firm $i; i = 1,, I$.
Р	set of all n_P paths in the supply chain network economy.
$x_p; p \in P_k^i$	nonnegative flow on path p originating at firm node i and terminating at k ; $\forall i, k$.
	Group firm i's path flows into vector $x^i \in R_{\perp}^{''P^i}$. Then group all firms' path flows
	into vector $x \in R^{np}_+$.
f _a	nonnegative flow of the product on link $a, \forall a \in L$. Group all link flows into vector
	$f \in R_+^{n_L}$.
la	labor on link a (usually denoted in person hours).
α_a	positive factor relating input of labor to output of product flow on link a , $\forall a \in L$.
Īa	bound on the availability of labor on link a under Scenario 1, $orall a \in L$
7 ^t	bound on labor availability for tier t activities under Scenario 2. $T + 1$ is electronic commerce tier.
7	bound on labor availability under Scenario 3.
d _{ik}	demand for the product of firm <i>i</i> at demand market <i>k</i> ; $\forall i, k$. Group $\{d_{ik}\}$ elements
	for firm <i>i</i> into vector $d^i \in R^{n_R}_+$ and all demands into vector $d \in R^{l \times n_R}_+$.
$\hat{c}_a(f)$	total operational cost associated with link $a, \forall a \in L$.
π_a	cost of a unit of labor on link a , $\forall a$.
$\rho_{ik}(d)$	demand price function for the product of firm <i>i</i> at demand market k ; $\forall i, k$.
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For each firm i; i = 1, ..., I, we must have that:

$$\sum_{p\in P_k^i} x_p = d_{ik}, \quad k = 1, \dots, n_R.$$
(1)

The path flows must be nonnegative; that is, for each firm i; i = 1, ..., I:

$$x_p \ge 0, \quad \forall p \in P^i.$$
 (2)

The link flows of each firm i; i = 1, ..., I, are related to the path flows as:

$$f_{a} = \sum_{p \in P} x_{p} \delta_{ap}, \quad \forall a \in L^{i},$$
(3)

where $\delta_{ap} = 1$, if link *a* is contained in path *p*, and 0, otherwise. We now discuss how labor is related to product flow.

$$f_{a} = \alpha_{a}I_{a}, \quad \forall a \in L^{i}, \quad i = 1, \dots, I.$$
(4)

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The utility function of firm *i*, U^i ; i = 1, ..., I, is the profit, given by the difference between its revenue and its total costs:

$$U^{i} = \sum_{k=1}^{n_{R}} \rho_{ik}(d) d_{ik} - \sum_{a \in L^{i}} \hat{c}_{a}(f) - \sum_{a \in L^{i}} \pi_{a} I_{a}.$$
 (5a)

The functions U_i ; i = 1, ..., I, are assumed to be concave, with the demand price functions being monotone decreasing and continuously differentiable and the total link cost functions being convex and also continuously differentiable.

The Optimization Problem of Each Firm

The optimization problem of each firm i; i = 1, ..., I, is:

Maximize
$$\sum_{k=1}^{n_R} \rho_{ik}(d) d_{ik} - \sum_{a \in L^i} \hat{c}_a(f) - \sum_{a \in L^i} \pi_a I_a, \quad (5b)$$

subject to: (1), (2), (3), and (4).

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Labor Scenario 1 – A Bound on Labor on Each Supply Chain Network Link

In Scenario 1, the additional constraints on the fundamental model are:

$$J_a \leq \overline{J}_a, \quad \forall a \in L.$$
 (6)

Labor Scenario 2 – A Bound on Labor on Each Tier of Links in the Supply Chain Network

In Scenario 2, firms are faced with the ff. additional constraints:

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$$\sum_{a \in l^1} l_a \le \bar{l}^1, \tag{7,1}$$

$$\sum_{a \in L^2} I_a \le \overline{I}^2, \tag{7,2}$$

and so on, until

$$\sum_{\in L^{T+1}} I_a \le I^{T+1}.$$
 (7, T+1)

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Labor Scenario 3 – A Single Labor Bound on Labor for All the Links in the Supply Chain Network

Scenario 3 may be interpreted as being the least restrictive of the scenarios considered here in that labor can be transferable across different activities of production, transportation, storage, and distribution. In Scenario 3, in addition to constraints (1) through (4), the firms are now faced with the following single constraint:

$$\sum_{a\in L} l_a \le \overline{l}.$$
 (8)

Recall that x^i denotes the vector of strategies, which are the path flows, for each firm i; i = 1, ..., I. We can redefine the utility/profit functions $\tilde{U}^i(x) \equiv U^i$; i = 1..., I and group the profits of all the firms into an *I*-dimensional vector \tilde{U} , such that

$$\tilde{U} = \tilde{U}(x).$$
 (9)

Objective function (5b), in lieu of the above, can now be expressed as:

Maximize
$$\tilde{U}^{i}(x) = \sum_{k=1}^{n_{R}} \tilde{\rho}_{ik}(x) \sum_{p \in P_{k}^{i}} x_{p} - \sum_{a \in L^{i}} \tilde{c}_{a}(x) - \sum_{a \in L^{i}} \frac{\pi_{a}}{\alpha_{a}} \sum_{p \in P} x_{p} \delta_{ap}.$$

$$(10)$$
Governing Equilibrium Conditions

Scenario 1 Nash Equilibrium Conditions We define the feasible set K_i for firm *i*: $K_i \equiv \{x^i | x^i \in R^{n_{pi}}_+, \frac{\sum_{p \in P^i} x_p \delta_{ap}}{\alpha_a} \leq \overline{l}_a, \forall a \in L^i\}$, for i = 1, ..., I. Also, we define $K \equiv \prod_{i=1}^{I} K_i$.

In Scenario 1, each firm competes noncooperatively until the following equilibrium is achieved.

Definition: Supply Chain Network Nash Equilibrium for Scenario 1

A path flow pattern $x^* \in K$ is a supply chain network Nash Equilibrium if for each firm i; i = 1, ..., I:

$$ilde{U}^i(x^{i*}, \hat{x}^{i*}) \geq ilde{U}^i(x^i, \hat{x}^{i*}), \quad \forall x^i \in K_i,$$
(11)

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where $\hat{x}^{i*} \equiv (x^{1*}, \dots, x^{i-1*}, x^{i+1*}, \dots, x^{l*}).$

Variational Inequality Formulations

Applying the classical theory of Nash equilibria and variational inequalities, under our imposed assumptions on the underlying functions, it follows that (cf. Gabay and Moulin (1980) and Nagurney (1999)) the solution to the above Nash Equilibrium problem (see Nash (1950, 1951)) coincides with the solution of the variational inequality problem: determine $x^* \in K$, such that

$$-\sum_{i=1}^{l} \langle \nabla_{x^{i}} \tilde{U}^{i}(x^{*}), x^{i} - x^{i*} \rangle \geq 0, \quad \forall x \in K,$$
(12)

where $\langle \cdot, \cdot \rangle$ represents the inner product in the corresponding Euclidean space, which here is of dimension n_P , and $\nabla_{x^i} \tilde{U}^i(x)$ is the gradient of $\tilde{U}^i(x)$ with respect to x^i .

We introduce Lagrange multipliers λ_a associated with constraint (6), $\forall a \in L$ and group the Lagrange multipliers for each firm *i*'s network L^i into the vector λ^i . Group all such vectors for firms into vector $\lambda \in R_+^{n_L}$. Define feasible sets: $K_i^1 \equiv \{(x^i, \lambda^i) | (x^i, \lambda^i) \in R_+^{n_{pi} + n_{Li}}\}; i = 1, ..., I$, and $K^1 \equiv \prod_{i=1}^{l} K_i^1$.

Theorem: Alternative VI of Nash Equilibrium for Scenario 1

The supply chain network Nash Equilibrium satisfying the Definition 3.1 is equivalent to the solution of the variational inequality: determine vectors of path flows and Lagrange multipliers, $(x^*, \lambda^*) \in K^1$, where:

$$\sum_{i=1}^{m} \sum_{k=1}^{n_R} \sum_{p \in P_k^i} \left[\frac{\partial \tilde{\mathcal{C}}_p(x^*)}{\partial x_p} + \sum_{a \in L^i} \frac{\lambda_a^*}{\alpha_a} \delta_{ap} + \sum_{a \in L^i} \frac{\pi_a}{\alpha_a} \delta_{ap} - \tilde{\rho}_{ik}(x^*) - \sum_{l=1}^{n_R} \frac{\partial \tilde{\rho}_{il}(x^*)}{\partial x_p} \sum_{q \in P_l^i} x_q^* \right] \times [x_p - x_p^*]$$

$$+\sum_{a\in L} \left[\bar{l}_a - \frac{\sum_{p\in P} x_p^* \delta_{ap}}{\alpha_a} \right] \times \left[\lambda_a - \lambda_a^* \right] \ge 0, \quad \forall (x,\lambda) \in \mathcal{K}^1;$$
(13)

where for each path p; $p \in P_k^i$; $i = 1, \ldots, m$; $k = 1, \ldots, n_R$:

$$\frac{\partial \tilde{\mathcal{C}}_{\mathcal{P}}(x)}{\partial x_{p}} \equiv \sum_{a \in L^{i}} \sum_{b \in L^{i}} \frac{\partial \hat{c}_{b}(f)}{\partial f_{a}} \delta_{ap}, \tag{14}$$

$$\frac{\partial \hat{\rho}_{ik}(x)}{\partial x_{\rho}} \equiv \frac{\partial \rho_{il}(d)}{\partial d_{ik}}.$$
(15)

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Scenarios 2 and 3

For both Scenarios 2 and 3, we use a refinement of the Generalized Nash Equilibrium, known as a Variational Equilibrium to construct variational inequality formulations.

Hence, the labor supply chain network equilibrium models, under three different scenarios of constraints, can be uniformly qualitatively studied and solution to numerical problems, quantitatively computed using rigorous algorithms!

All the variational inequalities can be put into standard form; $VI(F, \mathcal{K})$, where one seeks to determine a vector $X^* \in \mathcal{K} \subset R^N$, such that

$$\langle F(X^*), X - X^* \rangle \ge 0, \quad \forall X \in \mathcal{K},$$
 (16)

where F is a given continuous function from \mathcal{K} to \mathbb{R}^N , \mathcal{K} is a given closed, convex set, and $\langle \cdot, \cdot \rangle$ denotes the inner product in N-dimensional Euclidean space.

The Algorithm

The Modified Projection Method

Step 0: Initialization

Initialize with $X^0 \in \mathcal{K}$. Set the iteration counter $\tau := 1$ and let β be a scalar such that $0 < \beta \leq \frac{1}{L}$, where L is the Lipschitz constant.

Step 1: Computation

Compute \bar{X}^{τ} by solving the variational inequality subproblem:

$$\langle \bar{X}^{\tau} + \beta F(X^{\tau-1}) - X^{\tau-1}, X - \bar{X}^{\tau} \rangle \ge 0, \quad \forall X \in \mathcal{K}.$$
 (17)

Step 2: Adaptation

Compute X^{τ} by solving the variational inequality subproblem:

$$\langle X^{\tau} + \beta F(\bar{X}^{\tau}) - X^{\tau-1}, X - X^{\tau} \rangle \ge 0, \quad \forall X \in \mathcal{K}.$$
 (18)

Step 3: Convergence Verification If $|X^{\tau} - X^{\tau-1}| \leq \epsilon$, with $\epsilon > 0$, a pre-specified tolerance, then stop; otherwise, set $\tau := \tau + 1$ and go to Step_1. The set of the

Application of the Modified Projection Method

Realization of the Modified Projection Method Computation Step for VI (13)

Specifically, at iteration τ , we compute each of the path flows \bar{x}_{p}^{τ} , $\forall P_{k}^{i}$, $\forall i, \forall k, \text{ according to:}$

$$\tilde{x}_{\rho}^{\tau} = \max\{0, x_{\rho}^{\tau-1} - \beta(\frac{\partial \tilde{\mathcal{C}}_{\rho}(x^{\tau-1})}{\partial x_{\rho}} + \sum_{a \in L^{i}} \frac{\lambda_{a}^{\tau-1}}{\alpha_{a}} \delta_{a\rho} + \sum_{a \in L^{i}} \frac{\pi_{a}}{\alpha_{a}} \delta_{a\rho} - \tilde{\rho}_{ik}(x^{\tau-1}) - \sum_{l=1}^{n_{R}} \frac{\partial \tilde{\rho}_{il}(x^{\tau-1})}{\partial x_{\rho}} \sum_{q \in P^{i}} x_{q}^{\tau-1})\}$$
(19)

and each of the Lagrange multipliers $\bar{\lambda}_{a}^{\tau}$, $\forall a \in L$, according to:

l = 1

$$\bar{\lambda}_{a}^{\tau} = \max\{0, \lambda_{a}^{\tau-1} - \beta(\bar{l}_{a} - \frac{\sum_{p \in P} x_{p}^{\tau-1} \delta_{ap}}{\alpha_{a}})\}.$$
 (20)

 $a \in P_i^i$

Application of the Modified Projection Method

Realization of the Modified Projection Method Adaptation Step for VI (13)

At iteration τ , we compute each of the path flows x_p^{τ} , $\forall P_k^i$, $\forall i$, $\forall k$, according to:

$$x_{p}^{\tau} = \max\{0, x_{p}^{\tau-1} - \beta(\frac{\partial \tilde{C}_{p}(\bar{x}^{\tau})}{\partial x_{p}} + \sum_{a \in L^{i}} \frac{\bar{\lambda}_{a}^{\tau}}{\alpha_{a}} \delta_{ap} + \sum_{a \in L^{i}} \frac{\pi_{a}}{\alpha_{a}} \delta_{ap} - \tilde{\rho}_{ik}(\bar{x}^{\tau}) - \sum_{l=1}^{n_{R}} \frac{\partial \tilde{\rho}_{il}(\bar{x}^{\tau})}{\partial x_{p}} \sum_{q \in P_{l}^{i}} \bar{x}_{q}^{\tau})\}$$
(21)

and each of the Lagrange multipliers λ_a^{τ} , $\forall a \in L$, according to:

$$\lambda_a^{\tau} = \max\{0, \lambda_a^{\tau-1} - \beta(\bar{l}_a - \frac{\sum_{p \in P} \bar{x}_p^{\tau} \delta_{ap}}{\alpha_a})\}.$$
 (22)

Our numerical examples are based on disruptions in migrant labor in the blueberry supply chain in the Northeast of the US in the summer of 2020.



The numerical examples investigate:

- Modifications in demand price functions;
- Disruptions in labor on a supply chain network link, with additional numerical examples presented in the EJOR paper.

Numerical Examples

Examples 1, 2, and 3 have the supply chain network topology given below. There are two competing food firms (blueberry farms), each with two production locations, and with a single distribution center. There are two demand markets. We consider Scenario 1.



Figure: The Supply Chain Network Topology for the Numerical Examples

Example 1 - Baseline Example

The total operational cost functions for Food Firm 1 on its supply chain network L^1 are:

$$\hat{c}_{a}(f) = .0006f_{a}^{2}, \quad \hat{c}_{b}(f) = .0007f_{b}^{2}, \quad \hat{c}_{c}(f) = .001f_{c}^{2}, \quad \hat{c}_{d}(f) = .001f_{d}^{2},$$
$$\hat{c}_{e}(f) = .002f_{e}^{2}, \quad \hat{c}_{f}(f) = .005f_{f}^{2}, \quad \hat{c}_{g}(f) = .005f_{g}^{2}.$$

Also, the total operational costs associated with Food Firm 2's supply chain network L^2 are:

$$\hat{c}_h(f) = .00075f_h^2, \quad \hat{c}_i(f) = .0008f_i^2, \quad \hat{c}_j(f) = .0005f_j^2, \quad \hat{c}_k(f) = .0005f_k^2, \\ \hat{c}_l(f) = .0015f_l^2, \quad \hat{c}_m(f) = .01f_m^2, \quad \hat{c}_n(f) = .01f_n^2.$$
The costs for labor (wages) for Food Firm 1 are:

 $\pi_a = 10, \quad \pi_b = 10, \quad \pi_c = 15, \quad \pi_d = 15, \quad \pi_e = 20, \quad \pi_f = 17, \quad \pi_g = 18,$ and for Food Firm 2:

$$\pi_h = 11, \quad \pi_i = 22, \quad \pi_j = 15, \quad \pi_k = 15, \quad \pi_l = 18, \quad \pi_m = 18, \quad \pi_n = 18.$$

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Example 1 - Baseline Example

The link labor productivity factors for the first firm are:

 $\alpha_{\textit{a}}=24,\,\alpha_{\textit{b}}=25,\,\alpha_{\textit{c}}=100,\,\alpha_{\textit{d}}=100,\,\alpha_{\textit{e}}=50,\,\alpha_{\textit{f}}=100,\,\alpha_{\textit{g}}=100,$

and for the second firm:

$$\alpha_h = 23, \, \alpha_i = 24, \, \alpha_j = 100, \, \alpha_k = 100, \, \alpha_l = 70, \, \alpha_m = 100, \, \alpha_n = 100.$$

The bounds on labor for the first firm are:

 $\bar{l}_a = 10, \quad \bar{l}_b = 200, \quad \bar{l}_c = 300, \quad \bar{l}_d = 300, \quad \bar{l}_e = 100, \quad \bar{l}_f = 120, \quad \bar{l}_g = 120,$

and for the second firm:

 $\bar{l}_h = 800, \quad \bar{l}_i = 90, \quad \bar{l}_j = 200, \quad \bar{l}_k = 200, \quad \bar{l}_l = 300, \quad \bar{l}_m = 100, \quad \bar{l}_n = 100.$

Observe that the labor availability on link *a* is low. This is done in order to capture a disruption to labor in the pandemic.

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The demand price functions for Food Firm 1 are:

$$\rho_{11}(d) = -.0001d_{11} - .00005d_{21} + 6, \quad \rho_{12}(d) = -.0002d_{12} - .0001d_{22} + 8.$$

The demand price functions for Food Firm 2 are:

$$\rho_{21}(d) = -.0003d_{21} + 7, \quad \rho_{22}(d) = -.0002d_{22} + 7.$$

The paths are: $p_1 = (a, c, e, f)$, $p_2 = (b, d, e, f)$, $p_3 = (a, c, e, g)$, path $p_4 = (b, d, e, g)$, $p_5 = (h, j, l, m)$, $p_6 = (i, k, l, m)$, $p_7 = (h, j, l, n)$, and $p_8 = (i, k, l, n)$.

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All the Lagrange multipliers are equal to 0.00 except for $\lambda_a^* = 4.925$ with the labor equilibrium value on link *a* equal to its upper bound of 10.00.

The product prices at equilibrium are:

$$\rho_{11} = 5.97, \quad \rho_{12} = 7.91, \quad \rho_{21} = 6.94, \quad \rho_{22} = 6.96,$$

with equilibrium demands of:

 $d_{11}^* = 172.07, \quad d_{12}^* = 359.15, \quad \rho_{21} = 195.94, \quad \rho_{22} = 197.86.$

The profit of Food Firm 1 is: 1,671.80 and the profit of Food Firm 2 is: 1,145.06.

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Example 2 has the same data as Example 1 except that we modify the demand price functions for the second firm to include a cross term, so that:

 $\rho_{21}(d) = -.0003d_{21} - .0001d_{11} + 6, \quad \rho_{22}(d) = -.0002d_{22} - .0001d_{12} + 7.$

The Lagrange multipliers are all equal to 0.00 except for $\lambda_a^* = 4.93$.

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The product prices at equilibrium are now:

 $\rho_{11} = 5.97, \quad \rho_{12} = 7.91, \quad \rho_{21} = 6.92, \quad \rho_{22} = 6.92,$

with the equilibrium demands:

$$d_{11}^* = 172.07, \quad d_{12}^* = 359.16, \quad d_{21}^* = 195.48, \quad d_{22}^* = 196.48.$$

The profit for Food Firm 1 is: 1,671.86 and the profit for Food Firm 2 is: 1,134.61. The profit for Food Firm 1 rises ever so slightly, whereas that for Food Firm 2 decreases.

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Example 3 – Disruptions in Storage Facilities

Example 3 has the same data as Example 2 except that we now consider a sizable disruption in terms of the spread of COVID-19 at the distribution centers of both food firms with the bounds on labor corresponding to the associated respective links being reduced to:

$$\overline{l}_e = 5, \quad \overline{l}_l = 5.$$

All computed equilibrium Lagrange multipliers are now equal to 0 except for those associated with the distribution center links, since the equilibrium labor values attain the imposed upper bounds on links *e* and *I*, with the respective equilibrium Lagrange multiplier values being:

$$\lambda_e^* = 157.2138, \quad \lambda_I^* = 43.6537.$$

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The product prices at equilibrium are now:

$$\rho_{11} = 5.99, \quad \rho_{12} = 7.94, \quad \rho_{21} = 6.94, \quad \rho_{22} = 6.94,$$

with the equilibrium demands:

$$d_{11}^* = 30.03, \quad d_{12}^* = 219.96, \quad d_{21}^* = 174.61, \quad d_{22}^* = 175.39.$$

The profit for Food Firm 1 is now dramatically reduced to 1,218.74 and the profit for Food Firm 2 also declines, but by a much smaller amount, to 1,126.73.

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Table: Equilibrium Product Path Flows for Examples 1 Through 3

Equilibrium Product Path Flows	Ex. 1	Ex. 2	Ex. 3
X [*] _{p1}	73.23	73.22	15.65
$X_{p_2}^*$	98.85	98.85	14.38
x [*] _{p3}	166.77	166.78	110.60
$X_{p_4}^*$	192.38	192.38	109.35
$X_{\rho_5}^*$	142.85	142.62	131.97
$X_{p_6}^*$	53.08	52.86	42.63
X [*] _{p7}	143.81	143.12	132.36
×* p8	54.04	53.36	43.02

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Table: Equilibrium Link Labor Values for Examples 1 Through 3

Equilibrium Link Labor Values	Ex. 1	Ex. 2	Ex. 3
/ <u>*</u>	10.00	10.00	5.26
/ <u>*</u>	11.65	11.65	4.95
I_c*	2.40	2.40	1.26
I_d^*	2.91	2.91	1.24
/ <u>*</u>	10.62	10.62	5.00
I_f^*	1.72	1.72	0.30
I_g^*	3.59	3.59	2.20
I_h^*	12.46	12.42	11.49
I_i^*	4.46	4.43	3.57
I_i^*	2.87	2.86	2.64
Ĩ,*	1.07	1.06	0.86
I <u>*</u>	5.63	5.60	5.00
/ <u>*</u>	1.96	1.95	1.75
/ <u>*</u>	1.98	1.96	1.75

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Farmers should do everything possible to secure the health of workers at their production/harvesting and other facilities, so that the blueberries can be harvested in a timely manner and so that profits do not suffer. Keeping workers healthy, through appropriate measures, impacts the bottom line! A. Nagurney, "Attracting International Migrant Labor: Investment Optimization to Alleviate Supply Chain Labor Shortages," Operations Research Perspectives 9 (2022), 100233.

A. Nagurney, "Optimization of Investments in Labor Productivity in Supply Chain Networks," International Transactions in Operational Research 29(4), (2022), pp 2116-2144. This article was recognized with an Editor's Choice Award.

A. Nagurney, "Supply Chain Networks, Wages, and Labor Productivity: Insights from Lagrange Analysis and Computations," *Journal of Global Optimization* 83 (2022), pp 615-638.

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The numerical results in our papers clearly reveal the importance of a holistic approach to supply chain network modeling since decisions made by a specific firm can have unexpected impacts on other competing firms in the supply chain network economy.

Our results also strongly suggest that having wages and labor equilibrate without any wage ceilings can be beneficial for an individual firm and also for firms engaged in competition.

And, most importantly, taking care of workers is critical in times of peace and war!

Resilience of Supply Chain Networks

Anna Nagurney Labor and Supply Chain Networks

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Resilience of Supply Chain Networks with Labor



How to quantify the resilience of a supply chain network in general and, specifically, with respect to disruptions in labor availability and productivity.

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Resilience of Supply Chain Networks with Labor



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Efficiency/Performance of a Supply Chain Network

The efficiency/performance of a defense supply chain network, denoted by *efficiency*, \mathcal{E} , is defined as:

$$\mathcal{E} = \mathcal{E}(G, \hat{c}, \rho, \pi, \alpha, \overline{I}) \equiv \sum_{i=1}^{I} \sum_{k=1}^{n_R} \frac{\frac{d_{ik}^*}{\rho_{ik}(d^*)}}{\ln_R}, \qquad (23)$$

with the demands, d^* , and the incurred demand market prices in (23), evaluated at the solution to the VI problem.

Given a supply chain network economy, and the various parameters and functions, the corresponding multi-firm supply chain network is considered as performing better if, on the average, it can handle higher demands at lower prices.

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Importance of a Supply Chain Network Component

Following then Nagurney and Qiang (2009), one can then define the importance of a component g (node, link, or a combination of nodes and links), I(g), which represents the efficiency drop when gis removed from the defense supply chain network, as:

$$I(g) = \frac{\Delta \mathcal{E}}{\mathcal{E}} = \frac{\mathcal{E}(G, \hat{c}, \rho, \pi, \alpha, \overline{I}) - \mathcal{E}(G - g, \hat{c}, \rho, \pi, \alpha, \overline{I})}{\mathcal{E}(G, \hat{c}, \rho, \pi, \alpha, \overline{I})}.$$
 (24)

One can then rank the importance of nodes or links using (24).

Resilience of Supply Chain Networks with Labor

I adapt the measure proposed in Nagurney and Ermagun (2022) for the supply chain network game theory model. As therein, let $\bar{I}\gamma$ denote the reduction of labor availability with $\gamma \in (0, 1]$ so if $\gamma = .8$ this means that the labor availability associated with the labor constraints is now 80% of the original labor availability as in \mathcal{E} .

Resilience Measure Capturing Labor Availability

One can define the resilience measure with respect to labor availability, $\mathcal{R}^{\bar{l}\gamma}$, as

$$\mathcal{R}^{\bar{l}\gamma} \equiv \mathcal{R}^{\bar{l}\gamma}(G,\hat{c},\rho,\pi,\alpha,\bar{l}) = \frac{\mathcal{E}^{\bar{l}\gamma}}{\mathcal{E}} \times 100\%,$$
(25)

with \mathcal{E} as in (22).

The closer the value is to 100%, the greater the resilience.

I constructed a similar resilience measure for labor productivity.

Solving multiple distinct supply chain network examples, we find:

(1). a free movement of labor across the supply chain network results in a higher efficiency of the supply chain as well as a higher resilience;

(2). a reduction in labor productivity can impact the supply chain network efficiency and the corresponding resilience, and

(3). the presence of electronic commerce escalates the efficiency of the supply chain network but diminishes resilience.

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Dealing with the Media and Impacting Policy

Anna Nagurney Labor and Supply Chain Networks

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Coverage by the Media



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On March 11, 2020 the WHO declared the pandemic. On March 12 my article on blood supply chains in *The Conversation* appeared and, on March 24 my article in INFORMS *Analytics Coronavirus Chronicles*.



How coronavirus is upsetting the blood supply chain



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The coronavirus, which causes the disease COVID-19, has created enormous

anxiety, uncertainty, and disruption to our lives. Much has already been written about potential shortages of medicines and face masks, but little has been said

about something only you and I can provide - lifesaving blood.

Our nation's blood supply is essential to our health care security. Blood transfusions are integral parts of major superfiss. Blood is used in the treatment of diseases, particularly siddle cell anemia and some cancers. Blood is needed for victims who have injuries sauced by succidense or natural diseases. Egercydag, the U.S. needs 80,000 units of red blood cells. 7,000 units of platteles, and 10,000 units of platms.

Lama professor and director of the Virtual Center for Supernetworks at the University of Massachusettis Amherst: Become of the exclusing commutinus. health care crisis, I am deeply concerned the USA, blood supply chain is under stress. The timing could Intrily be worse, the COVID-19 outbreak coincides with our seasonal Bus and colds.

Patients need blood in many states

Many states, including Washington, Galifornia Kansas, Pennaylvania, the Carolinas, Massachusetti and Rhode Island, are now calling for blood domitons. At the same time, some states are closing schools and other sites that typically host mobile blood drives; even prior to the coronarina, some events had been concelled to Macendeneut, the Berl Coron memory by Foremost branches in sead for a field coronal based on the state of the sead of the site state of the sead of

Anna Nagurnev

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arch 24, 2020 in Coronaurus Chronicses

The COVID-19 Pandemic and the Stressed Blood Supply Chain



Bood is seenfall to our motion healthcare security. It is a life-serving product that cannot be manufactured and comes assing from volumes downs. No exact that the form the product metal sector and the motion are integral parts of major supplets. Bood is a must for saving volume of acceleration of natural disasters. Bood is video useful to be volumes of comes and acceleration of acceleration of the volume of acceleration of one part, which can be meeted daily as are 7.250 uset of plantets and 150,000 units of plasma. A typical donation of one part, which can be used or diverse for one of \$2, planten and there is an advected to the first end \$2, \$2, \$50,000 units of blood.

Even in the best of times, the complex blocd supply chain in the United States is under stress. Although 38% of the U.S. population in eligible to domine blood, lists than 10% establig does as or a year. Furthermore, issues of sessonality core into pay with it and oriolic outing disordisor, the some for waither-elevide vertex that obliotisys. To further complicate matters, blood is perishable, planlets list five days and red blood cells have a shift life of 42 days.

The local basis is indexity, an whether with measurements and uncertainty of block, it has been a basis of the one sharp with block 000 his generation. The binary basis of the sharp with height block of basis and of the signal block basis block of the binary basis of the sharp with the signal block conserts and of basis and the binary block of the binary block of the binary block of the binary block of the binary of the control of the binary block of the binary block of the binary block of the binary of the control of the binary block of the binary block of the binary block of the binary of the control of the binary block of the binary mediad places. This has a subder in singular binary block of the binary block of t

The ottoil billod supply chain survices from others that we study is operations research (0.8%) is causes it hugess advanced contence, or lengt operating and distribution to heapsthal and media centers. The blodd supply chain can be visualized, modeled and studied as a network [4]. The convanisus can disrupt the links in the biodic augely chain interech "trong's avaiding of means. If charms and 8, they cannot down! If the util fit is, they connect celest, test, process and distribute blood. If our healthcare workers are compromised, they cannot transfrage.

China, specifically Wuhan where the coronavirus is generally thought to have originated, blood donations have

Labor and Supply Chain Networks

On August 4, 2020, I published an article in The Conversation,

"The Raging Competition for Medical Supplies is not a Game, but Game Theory Can Help."



On September 18, 2020, I published another article in *The Conversation*,

"Keeping Coronavirus Vaccines at Subzero Temperatures During Distribution Will Be Hard, but Likely Key to Ending Pandemic."

On January 8, 2021, my article,

"Vaccine Delays Reveal Unexpected Weak Link in Supply Chains: A Shortage of Workers," appeared in *The Conversation*.



On April 5, 2021, I published the article,

"Today's Global Economy Runs on Standardized Containers, as the Ever Given Fiasco Illustrates," also in *The Conversation*.

On September 21, 2021, my article,

"Global Shortage of Shipping Containers Highlights Their Importance in Getting Goods to Amazon Warehouses, Store Shelves and Your Door in Time for Christmas," appeared in *The Conversation.* It has had over 330,000 reads.



On February 3, 2022, my article,

"Heading into the Third Year of the Pandemic, the US Blood Supply is at a 10-Year Low," was published in *The Conversation*.
Some of My Media Interviews in the Pandemic



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Some of the Media Interviews on the War on Ukraine

Economic dangers from Russia's invasion ripple across globe







Published: Feb. 28, 2022, 5:55 p.m.



Anna Nagurney with John Moore

The John Batchelor Show

1/2: #Ukraine: The Kyiv School of Economics is open for business under fire. Paul Gregory @HooverInst @PaulR_Gregory. Anna Nagurney @Supernetworks University of Massachusetts. Paul Becker, Duke University

Russian war in world's 'breadbasket' threatens food supply

By JOSEPH WILSON, SAMY MAGDY, AVA BATRAWY and CHINEDU ASADU March 6, 2022

Threat of Russian cyber attacks likely for not just Ukraine, but also in the US

No Ikea Shelves, No Levis: The Retail Exodus From Russia Is On

Since the invasion of Ukraine began, the increasing financial and reputational risks of doing business in Russia are leading Western brands to halt operations.

Russian Sanctions Snarl Shipping Even as Pandemic Pressure Eases

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March 11, 2022 Liz Alderman and Jenny Gross On April 22, 2020, a letter from California Attorney General Xavier Becerra to the Admiral Brett Giroir, the Assistant Secretary of the US Department of Health & Human Services, and signed by US Attorney Generals of 21 other states, requested updates, because of the pandemic blood shortages, to blood donation policies that discriminate.

My March 2020 article in *The Conversation*, which was reprinted in LiveScience, was the first reference and was cited on the first page.

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Impacting Policy



State of California Office of the Attorney General Xavier Becerra Artonsmus Ginnasi

April 22, 2020

Via Electronic Mail

The Honorable Admiral Brett Giroir, MD Assistant Secretary for Health U.S. Department of Health & Human Services Mary E. Switzer Building 330 C Street SW, Room 1.600 Washington, DC 20024 Attr: ACDTSA-PAHPALA Sec. 209 ACBTSA@bhx.gov

RE: "Solicitation for Public Comments on Section 209 of the Pandemic and All-Hazards Preparedness and Advancing Innovation Act," 85 Fed. Reg. 16.372 (March 23, 2020)

Dear Assistant Secretary Giroir:

The undersigned State Attomneys General from California, Colerada, Connection, Dohreney, the Diversity of Columbia, Harves, Millowi, Jone, Maney, Mare, Martin, Michigan, Martin, Yuguisa ubanit this letter in response to the foderal government * "Solicitation for Public Commerton so-Societor 2007 of the Pandemin and JAII Lanzeh Prependenses and Advancing Innovation, Aut," (SS Fed. Reg. LA72). We support the Office of the Assistant Societary for minimizing an advance minimum term of the Assistant Societary for minimizing and subsequence minimum term of the Assistant Societary for minimizing and subsequence minimum term of participation of the Assistant Societary for Martin and Societary and So

An adequate blood supply is critical to the nation's healthcare. Blood transfusions and blood products are needed for major surgeries, to treat diseases such as sickle cell anemia and some cancers, and to treat victims who have injuries caused by accidents or natural disasters.¹ Every day, the United States needs approximately 36,000 units of red blood cells, nearly 7,000

1300 I STREET * SUITE 1740 * SACRAMENTO, CALIFORNIA 95814 * (916) 210-6029

Anna Nagurney Labor and Supply Chain Networks

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¹ Anna Nagurney, How Coronavirus is Upsetting the Blood Supply Chain, Live Science (Mar. 13, 2020), https://www.livescience.com/coronavirus-blood-supply-chain.html/.

Impacting Policy

Hos. Beett Giscir Auril 22, 2020 Pare 7 - Ling Knother Anno WILLIAMTONO CATCH FOR HERMINGS Comecticut Attomev General Delaware Attorney General CARLA RACINI District of Columbia Attoms y General Hawaii Attoms y General Ton Millor OM MULER Illinois Attomey General Iows Attorney General I Hack Jour M. Frey MAURA HEALEY Maine Attomey General Massachusetts Attoms y General inthe Alis ane Wares Michigan Attomey General Minne sota Attorne y General and AARON D. FORD HIRBIRS OREWAL Neveda Attomey General New Jessey Attorney General Letitia James CENTRAL LA MES New York Attomey General New Mexico Attome v General

Xavier Becerra, previously California's Attorney General, has now been confirmed as President Joe Biden's Health and Human Services Secretary!

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It's All About People!



Anna Nagurney

Labor and Supply Chain Networks



More information on our work can be found on the Supernetwork Center site: https://supernet.isenberg.umass.edu/

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