Exchange Rates and Multicommodity International Trade: Insights from Spatial Price Equilibrium Modeling with Policy Instruments via Variational Inequalities

Anna Nagurney¹, Dana Hassani¹, Oleg Nivievskyi², Pavlo Martyshev²

¹ Department of Operations and Information Management Isenberg School of Management University of Massachusetts Amherst, Amherst, Massachusetts ² Center for Food and Land Use Research Kyiv School of Economics, Kyiv, Ukraine

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Anna Nagurney¹ + Dana Hassani¹ · Oleg Nivievskyi² · Pavlo Martyshev²

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Abstract

In this paper, we construct a multicommodity international trade spatial price equilibrium ondel of special relevance to agriculture in which exchange rates are included along with policy instruments in the form of tariffs, subsidies as well as quetas. The model allows for imilipe trade routes between county origin nodes and county destination on tests and these trade routes can include different modes of transportation and transport through distinct counts. We capture the formation data sortational matching of the trade routes and address, which are then formational as a sortational inquiring theorem protocols and distinct, we capture the formational as a sortational inquiring three matchings and distinct, which are the formational as a sortational inquiring three protocols. The information Extension extends the stabilities of the impacts of exchange rates and sortations. The next three of the quantification of the impacts of exchange rates and various trade policies, as well as the addition or deletion of angle ymarks, down and markst and/or routes and or product trade policies. In milectations for observed the impacts of exchange rates and/or routes and services and extend markst prices in local currencies, and on the volume of product trade flows with implications for for descent.

Keywords Exchange rates · Spatial price equilibrium · International trade · Networks · Variational inequalities · Agriculture

Exchange Rates and Multicommodity International Trade

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Outline of Presentation

- Background and Motivation
- Literature Review
- The Multicommodity International Trade Spatial Price Equilibrium Model
- Illustrative Examples
- The Algorithm
- Larger Numerical Examples
- Insights and Summary

International Trade and Policies

- International trade provides us with commodities throughout the year and has benefits for producers and consumers alike.
- The increased level of world trade and competition has garnered the attention of government policy makers.
- Trade policy instruments such as tariffs, subsidies, and quotas have become highly relevant as the world continues to battle the impacts of the COVID-19 pandemic and millions on the planet suffer from hunger and growing food insecurity.



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International Trade, Policies, and Exchange Rates

Identifying quantitatively the **impacts of trade policies and exchange rates** on international trade can provide trade and regulatory bodies with valuable information on product trade volumes and producer and consumer prices.



Exchange rates represent the value (price) of one currency relative to another currency.



They are important economic parameters in international trade, with changes in the exchange rate affecting the decision-making of individuals, businesses, and governments. This work is inspired by Russia's war on Ukraine and the need to assess its impacts on agricultural trade as well as on food insecurity and the need to provide more general computable models for assessing the impacts of trade policies and exchange rates on international trade.



Literature Review

The intellectual foundations of our work lie in the contributions of Samuelson (1952) and Takayama and Judge (1964, 1971) to spatial price equilibrium (SPE) modeling with notice of the following works that utilize variational inequality theory: Florian and Los (1982), Dafermos and Nagurney (1984), Harker and Friesz (1986), Nagurney, Thore, and Pan (1996), Daniele (2004).

• Variational inequality formulations of SPE problems with trade instruments have been constructed by Nagurney, Nicholson, and Bishop (1996), Nagurney, Besik, and Dong (2019), and Nagurney, Salarpour, and Dong (2022).

• Devadoss and Sabala (2020) emphasize that no study until theirs had previously used the spatial price equilibrium model to analyze the effects of exchange rate changes. Their study focused on the yuan-dollar exchange rate and cotton markets and proposed a single commodity spatial price equilibrium model, with a single route, consisting of a single link, between countries. In this paper, we harness the powerful theory of variational inequalities to construct a model with the following features:

- Multiple commodities;
- Multiple routes from origin nodes to destination nodes in the same or different countries;
- Exchange rates and the formula for their computation along trade routes;
- Inclusion of policies in the form of tariffs, subsidies, and quotas;
- The underlying economic functions can be nonlinear and asymmetric. Hence, our transportation cost functions capture congestion.

The Multicommodity International Trade Model



The network topology is denoted by the graph G = [N, L], where N is the set of nodes, L is the set of links, and P is the set of paths. There are H commodities, with a typical one denoted by h.

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Each path p represents a trade route. Intermediate nodes in the network, which are transit points, also correspond to countries.

Let P_{ij} denote the set of paths connecting the pair of origin/destination country nodes (i, j). The paths are acyclic.

A typical link is denoted by *a* and represents transport from a country node at which the link originates to the node denoting the country at which the link terminates.

A trade route can entail transportation through multiple countries, depending on the application, and via different modes, such as rail, truck, air, or water (sea, river, etc.). Associated with each link $a \in L$ is an exchange rate e_a , reflecting the exchange rate from the country (node) that the link emanates from to the country (node) that it terminates in.

Also, associated with each pair of origin/destination countries (i, j) is the exchange rate e_{ij} for i = 1, ..., m; j = 1, ..., n.

There is a nonnegative subsidy associated with commodity h and imposed by the government in country i, which is denoted by sub_i^h for h = 1, ..., H; i = 1, ..., m.

The unit tariff levied by country j on commodity h from country i is denoted by τ_{ij}^h for h = 1, ..., H; i = 1, ..., m; j = 1, ..., n. Tariffs within a country are not imposed; hence, $\tau_{ii}^h = 0$, $\forall i, \forall h$.

In addition, there are capacities, which can represent quotas, where \bar{Q}_{p}^{h} ; $h = 1, \ldots, H$; $p \in P$, denotes the bound on the commodity shipment of commodity h on path p.

All commodity path flows, for all commodities h, and all paths p, must be nonnegative:

$$Q^h_p \ge 0, \quad \forall h, \forall p \in P.$$
 (1)

The flow on a link a of commodity h, in turn, is equal to the sum of the path flows of the commodity h that use the link:

$$f_a^h = \sum_{p \in P} Q_p^h \delta_{ap}, \quad \forall h, \forall a \in L.$$
(2)

where $\delta_{ap} = 1$, if link *a* is contained in path *p*, and is 0, otherwise.

The supply of commodity *h* produced in country *i*, s_i^h , is equal to the shipments of the commodity from the country to all destination countries:

$$s_i^h = \sum_{p \in P^i} Q_p^h, \quad h = 1, \dots, H; i = 1, \dots, m,$$
 (3)

whereas the demand for commodity h in country j, d_j^h , is equal to the shipments of the commodity from all origin countries to that country:

$$d_j^h = \sum_{\rho \in P_j} Q_{\rho}^h, \quad h = 1, \dots, H; j = 1, \dots, n.$$
 (4)

 $Q \in R_{+}^{n_{P}}$ is the vector of commodity shipments with $s \in R_{+}^{Hm}$ being the vector of commodity supplies and $d \in R_{+}^{Hn}$ being the vector of commodity demands.

The supply price function for commodity *h* of country *i* is denoted by π_i^h and we have that:

$$\pi_i^h = \pi_i^h(s), \quad h = 1, \dots, H; i = 1, \dots, m.$$
 (5a)

With notice of the conservation of flow equations (3), we may define new supply price functions $\tilde{\pi}_i^h$; h = 1, ..., H; i = 1, ..., m, such that

$$\tilde{\pi}_i^h(Q) \equiv \pi_i^h(s). \tag{5b}$$

The demand price functions, in turn, are:

$$\rho_j^h = \rho_j^h(d), \quad h = 1, \dots, H; j = 1, \dots, n,$$
(6a)

where ρ_j^h denotes the demand price for commodity h in country j. Making use now of conservation of flow equations (4), we construct equivalent demand price functions $\tilde{\rho}_j^h$; $h = 1, \ldots, H$; $j = 1, \ldots, n$, as follows:

$$\tilde{\rho}_j^h(Q) \equiv \rho_j^h(d). \tag{6b}$$

With each link $a \in L$, and commodity h, we associate a unit transportation cost c_a^h such that

$$c_a^h = c_a^h(f), \quad \forall h, \forall a \in L.$$
 (7a)

Because of the conservation of flow equations (2), we can define link unit transportation cost functions $\tilde{c}_a^h(Q)$, $\forall a \in L$, $\forall h$, as:

$$\tilde{c}^h_a(Q) \equiv c^h_a(f). \tag{7b}$$

Observe that, in order to appropriately quantify the effective transportation cost on a link *a* for a commodity *h*, if a commodity makes use of the link on a path from an origin country node to a destination country node, one needs to calculate the effective exchange rate associated with the commodity on link *a* being transported onward on path *p*, which is denoted by e_a^p . Note that e_a^p is the product of the exchange rates on the links on path *p* that include and follow link *a* on that path, and is given by:

$$e_{a}^{p} \equiv \begin{cases} \prod_{b \in \{a' \ge a\}_{p}} e_{b}, & \text{if } \{a' \ge a\}_{p} \neq \emptyset, \\ 0, & \text{if } \{a' \ge a\}_{p} = \emptyset, \end{cases}$$

$$(8)$$

where $\{a' \ge a\}_p$ denotes the set of the links including and following link *a* in path *p*, and Ø denotes the null set.

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The true transportation cost then on link $a, a \in L$, for commodity h; h = 1, ..., H, when it is used in a path p, is given by the expression:

$$\tilde{c}_a^{hp} = \tilde{c}_a^h(Q) e_a^p. \tag{9}$$

The effective transportation cost on a path, \tilde{C}_{p}^{h} , $\forall p \in P$, for commodity h; $h = 1, \ldots, H$, is then calculated as:

$$\tilde{C}^{h}_{p} = \sum_{a \in L} \tilde{c}^{hp}_{a} \delta_{ap}; \tag{10}$$

that is, the effective transportation cost on a path, which represents a trade route, is equal to the sum of the effective transportation costs for the commodity on links that make up the path.

Definition 1: The Multicommodity International Trade Equilibrium Conditions

A multicommodity path trade flow pattern $Q^* \in R_+^{n_p}$ is an international trade spatial price network equilibrium pattern under subsidies and tariffs with explicit exchange rates and capacities if the following conditions hold: For all pairs of country origin and destination nodes: (i,j); i = 1, ..., m; j = 1, ..., n, and all paths $p \in P_{ij}$ as well as all commodities h; h = 1, ..., H:

$$(\tilde{\pi}_{i}^{h}(Q^{*}) - sub_{i}^{h} + \tau_{ij}^{h})e_{ij} + \tilde{C}_{p}^{h}(Q^{*}) \begin{cases} \leq \tilde{\rho}_{j}^{h}(Q^{*}), & \text{if } Q_{p}^{h*} = \bar{Q}_{p}^{h}, \\ = \tilde{\rho}_{j}^{h}(Q^{*}), & \text{if } 0 < Q_{p}^{h*} < \bar{Q}_{p}^{h}, \\ \geq \tilde{\rho}_{j}^{h}(Q^{*}), & \text{if } Q_{p}^{h*} = 0. \end{cases}$$

$$(11)$$

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Variational Inequality Formulation and Existence

Theorem 1: Variational Inequality Formulation of the Multicommodity International Trade Equilibrium Conditions

A multicommodity path trade flow pattern $Q^* \in K$, where $K \equiv \{Q|0 \le Q \le \overline{Q}\}$ is a multicommodity international trade spatial price network equilibrium pattern with exchange rates and under subsidies and tariffs and capacities, according to Definition 1, if and only if it satisfies the variational inequality:

$$\sum_{h=1}^{H} \sum_{i=1}^{m} \sum_{j=1}^{n} \sum_{p \in P_{ij}} \left[(\tilde{\pi}_{i}^{h}(Q^{*}) - sub_{i}^{h} + \tau_{ij}^{h}) e_{ij} + \tilde{C}_{p}^{h}(Q^{*}) - \tilde{\rho}_{j}^{h}(Q^{*}) \right]$$

$$\times \left[Q_{\rho}^{h} - Q_{\rho}^{h*} \right] \ge 0, \quad \forall Q \in K.$$
(12)

Existence of an equilibrium solution Q^* is guaranteed since the feasible set K is compact.

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Standard Form

Variational inequality (12) is now put into standard form (cf. Nagurney (1999)), VI(F, \mathcal{K}), where one seeks to determine a vector $X^* \in \mathcal{K} \subset R^{\mathcal{N}}$, such that

$$\langle F(X^*), X - X^* \rangle \ge 0, \quad \forall X \in \mathcal{K},$$
 (13)

where F is a given continuous function from \mathcal{K} to $\mathbb{R}^{\mathcal{N}}$, \mathcal{K} is a given closed, convex set, and $\langle \cdot, \cdot \rangle$ denotes the inner product in \mathcal{N} -dimensional Euclidean space.

Specifically, we define $X \equiv Q$, $\mathcal{K} \equiv K$, and $\mathcal{N} = Hn_P$. Plus, F(X) consists of the elements $F_p^h(X) \equiv \left[(\tilde{\pi}_i^h(Q) - sub_i^h + \tau_{ij}^h)e_{ij} + \tilde{C}_p^h(Q) - \tilde{\rho}_j^h(Q) \right]$, $\forall h$, $\forall i, j, \forall p \in P_{ij}$. Clearly, VI (12) can be put into standard form (13).

Illustrative Examples

The examples focus on wheat commodity flows from Ukraine to Lebanon before and after the invasion of Ukraine by Russia on February 24, 2022.

The unit of flow is a ton of wheat, and, in these examples, there are no commodity path flow capacities.



USDA Foreign Agricultural Service

Source: State Statistics Service of Ukraine (Rosstat for Crimea Oblast) Average Wheat Production 2016-2020

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Example 1 - Pre-Invasion Scenario



The network topology for Illustrative Example 1 with nodes 1 and 2 representing Ukraine and node 3 corresponding to Lebanon. There is a single path $p_1 = (a, b)$, where link *a* corresponds to transport to the Black Sea ports via rail inside Ukraine, and link *b* represents maritime transport from the Black Sea ports to Lebanon.

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Example 1 - Pre-Invasion Scenario

Applying the international trade spatial price equilibrium conditions (11), under the assumption of no tariff, subsidy, and no quota, and assuming that $Q_{p_1}^* > 0$, we have that:

$$Q_{p_1}^* = 553,962.4370.$$

The 553,962.4370 tons of wheat flow is quite reasonable, since, in 2021, Lebanon imported 520,000 tons of wheat from Ukraine, and an even greater harvest was expected in 2022.

The supply and demand prices are:

$$\pi_1(s_1^*) = \tilde{\pi}_1(Q_{\rho_1}^*) = 7,076.9388 \text{ UAH} = \$257.7002,$$

 $\rho_3(d_3^*) = \tilde{\rho}_3(Q_{\rho_1}^*) = 519,249.6344 \text{ LBP} = \$343.4190.$

The supply price of \$257.7002 per ton of wheat in Ukraine (at the farmer level) and the demand price of \$343.4190 in Lebanon are close to the reported prices in 2021. Farmers in Ukraine could get about \$270 per ton of wheat before the invasion.

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Example 2 - Invasion Scenario



In Example 2, we consider the invasion scenario after February 24, 2022, but before the Black Sea Grain Initiative, which took effect in late July. During this period, essentially no grain was shipped from Ukraine using a Black Sea route as in Example 1. There is a single path $p_2 = (c, d, e)$. Nodes 1, 3, 4, and 5 denote Ukraine, Lebanon, Moldova, and Romania, respectively.

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Example 2 - Invasion Scenario

According to the international trade spatial price equilibrium conditions (11), and assuming that $Q_{p_2}^* > 0$, we have that:

 $Q_{p_2}^* = 25,780.2589.$

The wheat flow of 25,780.2589 tons is reasonable since, without access to deep-sea ports on the Black Sea, Ukraine can, at most, export around 10% of what it used to.

Supply and demand prices are:

 $\pi_1(s_1^*) = \tilde{\pi}_1(Q^*) = 2,875.2106 \text{ UAH} = \$98.2813,$ $\rho_3(d_3^*) = \tilde{\rho}_3(Q^*) = 789,364.8559 \text{ LBP} = \$522.0667.$

Because of the ongoing war, Ukrainian farmers are earning approximately \$100 per ton of wheat, which is similar to the supply price of \$98.2813 in this example. Moreover, with the continuing food crisis in Lebanon, and, as a result of the war, the price of wheat in Lebanon has gone up to more than \$500 per ton.

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Example 3 - Black Sea Grain Initiative in Place



The network topology for Example 3, where we consider the post-July 22 Black Sea Grain Initiative scenario with maritime transportation from several of the Ukrainian Black Sea ports being, again, possible. In the network above, the nodes and the links correspond to the same countries and modes of transportation as in Examples 1 and 2

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Example 3 - Black Sea Grain Initiative in Place

The equilibrium conditions (11), for this example, result in:

 $Q_{p_1}^* = 506, 566.8120, \quad Q_{p_2}^* = 0.0000.$

With the availability of maritime transportation from Ukraine on the Black Sea, the wheat flow on path p_2 is at 0.0000, which is due to the inefficiency of transporting the grain by such a route and composition of modes.

The supply and demand prices per ton now are:

$$\pi_1(s_1^*) = \tilde{\pi}_1(Q^*) = 3,449.1966 \text{ UAH} = \$94.3212,$$

 $\rho_3(d_3^*) = \tilde{\rho}_3(Q^*) = 754,624.0214 \text{ LBP} = \$499.0899.$

Although the initiative has facilitated the transportation of wheat, the war, and nearly full storage have kept the prices high. The supply price at \$94.3212 and the demand price at \$499.0899, along with around \$205 transportation cost on link *b*, reflect these issues and are preventing the demand market prices from falling, =, = = = =

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Example 4 - Example 3 Data with Subsidy

In Example 4, we, again, consider the post-July 22 Black Sea Grain Initiative scenario. Additionally, we consider the effect of the subsidy $sub_1 = 1,000.00$ in hryvnia on Ukrainian wheat shipped to Lebanon.

In the solution of this example, again, only path p_1 is used, and one has that: $Q_{p_1}^* = 889,408.4787$ and $Q_{p_2}^* = 0.0000$.

The resultant supply and demand prices are:

 $\pi_1(s_1^*) = \tilde{\pi}_1(Q^*) = 3,513.1312 \text{ UAH} = \$96.0696,$ $\rho_3(d_3^*) = \tilde{\rho}_3(Q^*) = 723,231.0047 \text{ LBP} = \$478.3273.$

The subsidy increases the quantity of wheat shipment, and increases the price that farmers can expect to get for a ton of wheat to \$96.0696, which can increase farmers' ability to buy seed and equipment. The subsidy also helps to reduce the demand price to \$478.3273, which can be of significant importance in countering the food crisis in Lebanon.

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The Algorithm

Modified Projection Method (Korpelevich (1977))

Step 0: Initialization

Initialize with $X^0 \in \mathcal{K}$. Set the iteration counter t := 1 and let β be a scalar such that $0 < \beta \leq \frac{1}{n}$, where η is the Lipschitz constant.

Step 1: Computation

Compute \bar{X}^t by solving the variational inequality subproblem:

$$\langle \hat{X}^t + \beta F(X^{t-1}) - X^{t-1}, X - \hat{X}^t \rangle \ge 0, \quad \forall X \in \mathcal{K}.$$
 (14)

Step 2: Adaptation

Compute X^t by solving the variational inequality subproblem:

$$\langle X^t + (\beta F(\hat{X}^t) - X^{t-1}), X - X^t \rangle \ge 0, \quad \forall X \in \mathcal{K}.$$
 (15)

Step 3: Convergence Verification

If $|X^t - X^{t-1}| \le \epsilon$, with $\epsilon > 0$, a pre-specified tolerance, then stop; otherwise, set t := t + 1 and go to Step 1.

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Explicit Formulae at Iteration t for the Multicommodity Product Path Flows in Step 1

The algorithm results in the following closed form expressions for (14) for the multicommodity product path flows in Step 1 for the solution of variational inequality (12):

$$\bar{Q}_{\rho}^{ht} = \max\{0, \min\{\bar{Q}_{\rho}^{h}, Q_{\rho}^{ht-1} + \beta(\tilde{\rho}_{j}^{h}(Q^{t-1}) - (\tilde{\pi}_{i}^{h}(Q^{t-1}) + sub_{i}^{h} - \tau_{ij}^{h})e_{ij} - \tilde{C}_{\rho}^{h}(Q^{t-1}))\}\},$$

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$$h, \forall p.$$
 (16)

The explicit formulae for (15) in Step 2 readily follow.

Larger Numerical Examples

The examples focus on commodity flows from Ukraine to Lebanon and Egypt, after the Black Sea Grain Initiative of July 22, 2022.



The figure above represents the network topology for the numerical Examples. Nodes 1 and 2 correspond to Ukraine, node 3 represents Lebanon, node 4 represents Moldova, node 5 is Romania, and node 6 denotes Egypt.

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Example 5 - Brokered Agreement - Two Demand Markets

In this example, the commodity is, again, that of wheat. The modified projection method computes the following commodity path flow pattern in tons of wheat:

 $Q_{p_1}^* = 302, 029.3750, \quad Q_{p_2}^* = 0.0000, \quad Q_{p_3}^* = 1, 390, 388.5000, \quad Q_{p_4}^* = 0.0000.$

One can see, from this solution, how important having an unblocked maritime route on the Black Sea is.

The demand market prices at equilibrium in the local currencies are:

 $\rho_3(d^*) = 771,396.0912 \text{ LBP} = \$510.1826, \quad \rho_6(d^*) = 9,700.2754 \text{ EGP} = \$506.5417.$

The lower wheat commodity flow as compared to that in Example 3 shows that Egypt essentially "competes" with Lebanon for wheat. This result also supports the negative effects of war-induced higher prices compared to the pre-war prices (e.g., around \$343 for Lebanon, as shown in Example 1). The demand price of wheat in Egypt is in accord with the post-war reported prices of more than \$470 as compared to less than \$300 pre-war.

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In order to support farmers, we assume that the Ukrainian government is now subsidizing farmers so that $sub_1 = 1000$ in hryvnia.

The modified projection method now yields the following equilibrium commodity path flow pattern of the wheat in tons:

$$Q_{p_1}^* = 557,759.6250, \quad Q_{p_2}^* = 0.0000,$$

 $Q_{p_3}^* = 2,254,257.0000, \quad Q_{p_4}^* = 0.0000.$

The most efficient paths only are, again, used, and we see a big increase in the wheat flow on paths p_1 and p_3 , almost similar to the pre-war import levels.

The demand market prices at equilibrium in the local currencies are:

$$\rho_3(d^*) = 750,426.1875 \text{ LBP} = \$496.3136,$$
 $\rho_6(d^*) = 9,513.6797 \text{ EGP} = \$496.7978.$

The demand market price of wheat decreases in both countries under the subsidy, which benefits consumers. The farmers in Ukraine now sell the wheat at a lower price (i.e., under \$105) relative to the pre-war supply price of \$257.7002 in Example 1, but now export a greater volume as compared to Example 5. The greater volume of wheat can assist in reducing food insecurity in Lebanon and Egypt, which rely heavily on Ukrainian wheat.

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Example 7 - Two Demand Markets and Two Commodities

The network topology remains as in Example 6, but now we have two commodities: wheat and corn. Here, the subscript h = 1 refers to wheat and the subscript h = 2 corresponds to corn.

The modified projection method yields the following multicommodity equilibrium flow pattern in tons of wheat and corn, respectively:

$$Q_{\rho_1}^{1*} = 285, 284.5625, \quad Q_{\rho_2}^{1*} = 0.0000, \quad Q_{\rho_3}^{1*} = 1, 288, 246.2500, \quad Q_{\rho_4}^{1*} = 0.0000.$$

$$Q_{p_1}^{2*} = 19,948.1738, \quad Q_{p_2}^{2*} = 0.0000, \quad Q_{p_3}^{2*} = 630,883.1250, \quad Q_{p_4}^{2*} = 0.0000.$$

The results for Example 7 further substantiate the importance of maritime routes over the Black Sea for exporting agricultural products from Ukraine, which would even be more the case if maritime freight rates are to decrease. The more efficient paths p_1 and p_3 are, again, in use for wheat shipments; however, one can see that the flows have decreased compared to Example 5, which is the impact of having another type of grain in the trade network.

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Example 7 - Two Demand Markets and Two Commodities

The prices at equilibrium in the local currencies for a ton of wheat in Lebanon and Egypt are:

 $\rho_3^1(d^*) = 772,769.1875 \text{ LBP} = \$511.0907, \quad \rho_6^1(d^*) = 9,722.3388 \text{ EGP} = \$507.6939,$

and for corn:

 $\rho_3^2(d^*) = 772,678.6875 \text{ LBP} = \$511.0308, \quad \rho_6^2(d^*) = 9,706.1885 \text{ EGP} = \$506.8505.$

The demand prices for wheat are nearly similar to those in Example 5, as both countries highly depend on Ukrainian wheat imports. Furthermore, one can observe the similarly war-induced higher demand prices for corn, although less than wheat. It is also worth noting that even at an increased supply price of around \$114 at the farm's gate, Ukraine remains the supplier providing the cheapest corn in the world.

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Example 8 - Example 7 with Quotas on Commodity Flows

This scenario is inspired by slowdowns in the processing of shipments of agricultural products even after the passage of the Black Sea Grain Initiative. As such, commodity path flow quotas are imposed.

The modified projection method now converges to the following equilibrium multicommodity flow pattern:

$$Q_{\rho_1}^{1*} = 200,000.0000, \quad Q_{\rho_2}^{1*} = 0.0000, \quad Q_{\rho_3}^{1*} = 100,000.0000, \quad Q_{\rho_4}^{1*} = 14,006.8184,$$

$$Q_{p_1}^{2*} = 15,000.0000, \quad Q_{p_2}^{2*} = 0.0000, \quad Q_{p_3}^{2*} = 600,000.0000, \quad Q_{p_4}^{2*} = 0.0000.$$

Both wheat and corn flows are at their capacities on paths: p_1 and p_3 . In the case of wheat, we now have positive flow on path p_4 , which was not the case in Example 7, but can be compared to Example 2. Clearly, the demand is sufficiently high that an alternative route is now being used. It can also be observed that the alternative route is not used for corn, which, again, is in accord with the high dependence of Lebanon and Egypt on Ukrainian wheat compared to corn.

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Example 8 - Example 7 with Quotas on Commodity Flows

The demand market prices at equilibrium in the local currencies for a ton of wheat and corn in Lebanon and Egypt are:

 $\rho_3^1(d^*) = 779,762.5000 \text{ LBP} = \$515.7159, \quad \rho_6^1(d^*) = 9,975.9746 \text{ EGP} = \520.9386

 $\rho_3^2(d^*) = 774,806.3750 \text{ LBP} = \$512.4380, \quad \rho_6^2(d^*) = 9,715.7002 \text{ EGP} = \$507.3472.$

The demand market prices of both wheat and corn rise in both Lebanon and Egypt under the quota regime as compared to the respective prices in Example 7. However, note that the increase in the price of wheat is greater than that of corn.

The supply price of wheat is at around \$95 relative to the respective supply price of about \$100 in Example 7. Similarly, the supply price of corn decreases from around \$114 in Example 7 to about \$112 in this example. A reduction in capacity on routes has a negative impact on farmers as well as on consumers in terms of prices and commodity availability.

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• The importance of having alternative routes in countering disruptions and congestion is evident in the examples.

• The results strongly confirm the need for efficient transportation routes for trade, as, for example, for the export of grain via maritime transport from the Black Sea ports in the case of Ukraine.

• The examples show the benefits of subsidies for agricultural trade for both farmers and consumers.

• The impact of the exchange rates on the grain commodity flows and on producer and consumer prices are revealed in the examples for different periods: pre-invasion, following the invasion, and after the Black Sea Grain Initiative.

• The examples demonstrate the importance of the Ukrainian grain, and its relevance to global food security.

• International trade of commodities is essential to both producers and consumers. Various recent disasters have demonstrated the criticality of trade for the availability of various commodities.

• Our model allows for multiple routes from origin to destination countries, and these routes can consist of multiple transportation links through different countries. We show how exchange rates affect costs, and formalize the definition of the multicommodity spatial price equilibrium with exchange rates and under policies.

• The numerical examples, for which complete input and output data are reported, are drawn from Russia's war on Ukraine.

• The flexibility of the modeling and algorithmic framework allows for quantitatively investigating the impacts of different scenarios with features of exchange rates plus various policies and the addition/deletion of markets and trade routes.

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This presentation is dedicated to all Ukrainian farmers who have sacrificed so much as the war continues in Ukraine.



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Exchange Rates and Multicommodity International Trade

INFORMS 2023

The Virtual Center for Supernetworks



Supernetworks for Optimal Decision-Making and Improving the Global Quality of Life

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