

Sustainable Supply Chain Networks for Sustainable Cities

Anna Nagurney

Isenberg School of Management
University of Massachusetts
Amherst, Massachusetts 01003

47th Session of the International Seminars on
Planetary Emergencies
Energy, Cities, and the Control of Complex Systems
ETTORE MAJORANA FOUNDATION AND CENTRE FOR
SCIENTIFIC CULTURE
May 11-15, 2014, Erice, Italy

Acknowledgments

I would like to thank Dr. Antonino Zichichi, Dr. Adilson E. Motter, and Dr. Robert Schock for the invitation to speak at this workshop.



Support for Our Research Has Been Provided by:



National Science Foundation

THE ROCKEFELLER FOUNDATION

Fulbright Scholar Program **FULBRIGHT**



RADCLIFFE INSTITUTE FOR ADVANCED STUDY
HARVARD UNIVERSITY



AT&T AT&T Foundation



John F. Smith Memorial Fund
University of Massachusetts
Amherst



UNIVERSITY OF GOTHENBURG
SCHOOL OF BUSINESS, ECONOMICS AND LAW

Outline

- ▶ Background and Motivation
- ▶ Supply Chains
- ▶ Methodology
- ▶ Applied Supply Chain Network Game Theory Models of Relevance to Sustainable Cities
- ▶ The Sustainable Supply Chain Network Model with Frequency of Activities
- ▶ Numerical Examples
- ▶ An Extension to Capture Competition
- ▶ Summary and Conclusions

This presentation is based on the following papers:

- “Design of Sustainable Supply Chains for Sustainable Cities,” A. Nagurney, in press in *Environment & Planning B*;

<http://supernet.isenberg.umass.edu/articles/SustainableCities.pdf>

- “Supply Chain Network Sustainability Under Competition and Frequencies of Activities from Production to Distribution,” A. Nagurney, M. Yu, and J. Floden, *Computational Management Science* **10(4)** (2013) pp 397-422;

<http://supernet.isenberg.umass.edu/articles/SustainableSupplyChainManagement.pdf>

Additional References

- “Sustainable Supply Chain Network Design: A Multicriteria Perspective,” A. Nagurney and L. S. Nagurney, *International Journal of Sustainable Engineering* **3** (2010) pp 189-197;

<http://supernet.isenberg.umass.edu/articles/SustainableSupplyChainNetworkDesign-nagurney-nagurney.pdf>

- “Environmental Impact Assessment of Transportation Networks with Degradable Links in an Era of Climate Change,” A. Nagurney, Q. Qiang, and L. S. Nagurney, *International Journal of Sustainable Transportation* **4** (2010) pp 154-171;

<http://supernet.isenberg.umass.edu/articles/nagurney-qiang-nagurney-environmental-robustness.pdf>

- “Environmental and Cost Synergy in Supply Chain Network Integration in Mergers and Acquisitions,” A. Nagurney and T. Woolley, in *Sustainable Energy and Transportation Systems, Lecture Notes in Economics and Mathematical Systems*, M. Ehrgott et al., Editors, Springer, Berlin, Germany (2010) pp 51-78;

<http://supernet.isenberg.umass.edu/articles/S-OMergerEnvironmentalWeights.pdf>



Background and Motivation

What is Sustainability?

The general definition of sustainability is development that meets the needs of the present without compromising the ability of future generations to meet their own needs (World Commission Environment and Development (WCED) (1987)).

The Debates Continue

There are, nevertheless, debates as to the correct methods to operationalize sustainability, as questions arise such as:

The Debates Continue

There are, nevertheless, debates as to the correct methods to operationalize sustainability, as questions arise such as:

- What *resources* will future generations require?

The Debates Continue

There are, nevertheless, debates as to the correct methods to operationalize sustainability, as questions arise such as:

- What *resources* will future generations require?
- What *level of emissions* can be released without negatively affecting future generations?

The Debates Continue

There are, nevertheless, debates as to the correct methods to operationalize sustainability, as questions arise such as:

- What *resources* will future generations require?
- What *level of emissions* can be released without negatively affecting future generations?
- What *policies* are required to achieve sustainability?

The Debates Continue

There are, nevertheless, debates as to the correct methods to operationalize sustainability, as questions arise such as:

- What *resources* will future generations require?
- What *level of emissions* can be released without negatively affecting future generations?
- What *policies* are required to achieve sustainability?
- What are the effects of *market forces*, etc.?



Pollution and Environmental Impacts

The release of CO₂ into the atmosphere, through the combustion of fossil fuels (coal, oil, and natural gas), has risen 30% in the 200 years since the industrial revolution (Burruss (2004)).

Pollution and Environmental Impacts

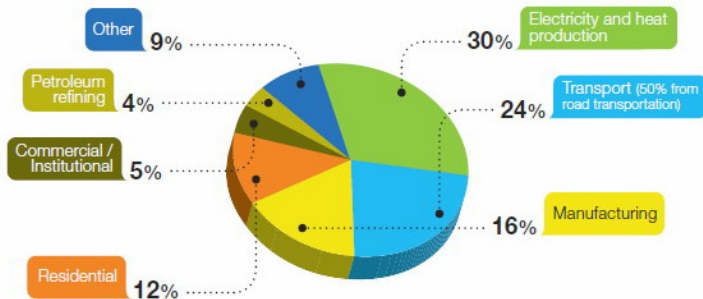
The release of CO₂ into the atmosphere, through the combustion of fossil fuels (coal, oil, and natural gas), has risen 30% in the 200 years since the industrial revolution (Burruss (2004)).

The average surface temperature of the earth, expressed as a global average, has increased by about 0.74C over the past hundred years (between 1906 and 2005) with 11 of the 12 warmest years occurring between 1995 and 2006 (IPCC (2007)).

Pollution and Environmental Impacts

In the US alone, greenhouse gas emissions are projected to rise 35% between 2005 and 2030 due to fewer forests and agricultural land to absorb the carbon, an increasing population, expansion of the economy, and an increased use of fossil fuel powered power plants to generate energy (Creyts et al. (2007)).

European CO₂ emissions by sector



Source: EEA (European Environment Agency)
Technical Report 6/2006

Cities and Sustainability

Cities, *as dynamic complex networks, are the systems in which more people now live than don't* and which represent the economic engines for commerce, research and development, education, health care, and even culture.

Cities have evolved over space and time on built infrastructure from transportation networks to telecommunication and electric power networks.

At the same time, cities are *the centers of resource usage* from electricity and other forms of energy and fuel, to food, water, and a plethora of other products.

Some Examples of Cities



Cities and Sustainability

Cities are also *the repositories and generators of waste output and other environmental pollutants, such as carbon and other emissions, sewage, noise, etc.*

Some Negative Externalities Associated with Cities



Cities and Sustainability

The term *Sustainable Cities* has come into increasing use in the past two decades, with a focus of making cities more livable, with an eye not only on the present generation but towards future ones, as well (cf. Nijkamp and Perrels (1994), Capello, Nijkamp, and Pepping (1999), Knickerbocker (2007), Grant Thornton (2011)).

Cities and Sustainability

A recent World Bank report (see Suzuki et al. (2009)) noted that the world is shrinking with cheaper air travel, large-scale commercial shipping, and expanding road networks. Today, only 10% of the globe's land area is considered to be remote, that is, more than 48 hours from a large city.

Our world is becoming a network of interconnected cities or a supernetwork of cities.

Cities and Sustainability

According to Alusi et al. (2011), *urbanization is one of the most pressing and complex challenges of the 21st century*, with the citizenry characterized by a growing awareness of a threat to the sustainability of the earth's natural environment, coupled with the increase in the number of people moving into and living in cities.

Cities and Supply Chains

Cities are supplied by a complex array of supply chains servicing an immense spectrum of economic activities from food stores and restaurants, office supplies and high tech equipment, apparel, construction materials, as well as raw materials, to name just a few.

Supply Chains

Supply Chains

Supply chains are the *critical infrastructure and backbones* for the production, distribution, and consumption of goods as well as services in our globalized *Network Economy*.

Supply chains, in their most fundamental realization, *consist of manufacturers and suppliers, distributors, retailers, and consumers at the demand markets*.

Supply Chains

Supply chains are the *critical infrastructure and backbones* for the production, distribution, and consumption of goods as well as services in our globalized *Network Economy*.

Supply chains, in their most fundamental realization, *consist of manufacturers and suppliers, distributors, retailers, and consumers at the demand markets*.

Today, supply chains may span thousands of miles across the globe, involve numerous suppliers, retailers, and consumers, and be underpinned by multimodal transportation and telecommunication networks.

Characteristics of Supply Chains and Networks Today

- ▶ *large-scale nature* and complexity of network topology;
- ▶ *congestion*, which leads to nonlinearities;
- ▶ *alternative behavior of users of the networks*, which may lead to paradoxical phenomena (Braess paradox);
- ▶ *possibly conflicting criteria associated with optimization*;
- ▶ *interactions among the underlying networks themselves*, such as the Internet with electric power networks, financial networks, and transportation and logistical networks;
- ▶ recognition of *their fragility and vulnerability*;
- ▶ policies surrounding networks today may have major impacts not only economically, but also *environmentally, socially, politically, and security-wise*.

Supply Chains Are Network Systems

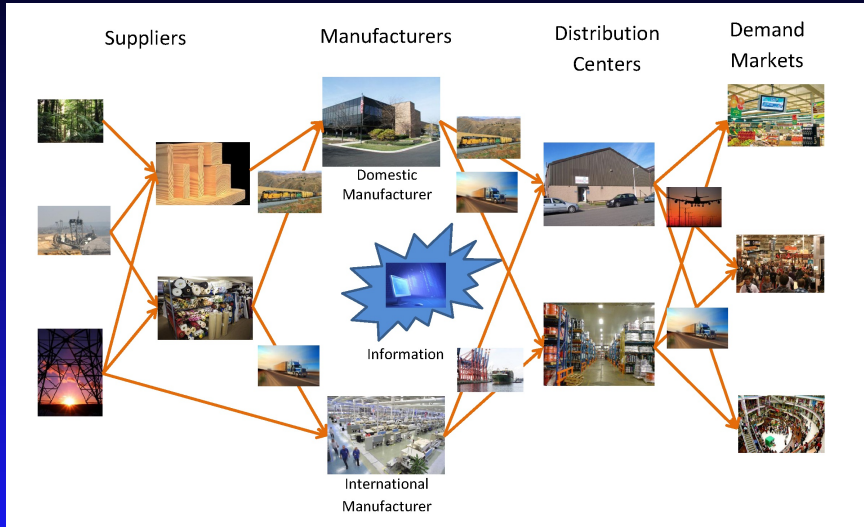
Supply chains are, in fact, *Complex Network Systems*.

Hence, *any formalism that seeks to model supply chains and to provide quantifiable insights and measures must be a system-wide one and network-based.*

Such crucial issues as the stability and resiliency of supply chains, as well as their adaptability and responsiveness to events in *a global environment of increasing risk and uncertainty* can only be rigorously examined from the view of supply chains as network systems.

Supply chains may be characterized by *decentralized decision-making* associated with the different economic agents or by *centralized* decision-making.

A General Supply Chain



Examples of Supply Chains

- ▶ food and food products
- ▶ high tech products
- ▶ automotive
- ▶ energy (oil, electric power, etc.)
- ▶ clothing and toys
- ▶ humanitarian relief
- ▶ healthcare supply chains.

Examples of Supply Chains

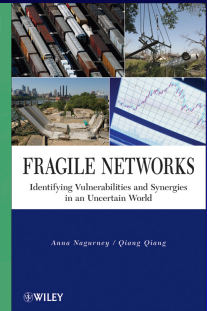
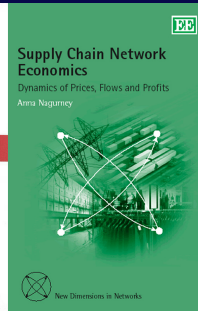
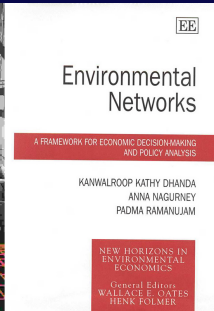
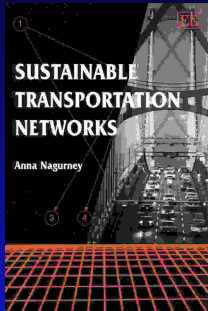


Sustainability of supply chains is, hence, a precursor to the sustainability of our cities. According to a Business for Social Responsibility (2009) paper, it is now widely acknowledged that making significant progress on mitigating the impact of climate change depends on reducing the negative environmental impacts of supply chains through their redesign and enhanced management (see also McKinsey Quarterly (2008)).

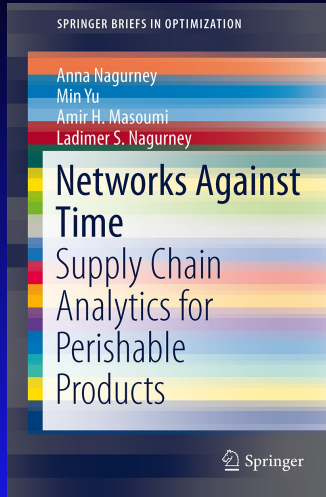
Sustainability of supply chains is, hence, a precursor to the sustainability of our cities. According to a Business for Social Responsibility (2009) paper, it is now widely acknowledged that making significant progress on mitigating the impact of climate change depends on reducing the negative environmental impacts of supply chains through their redesign and enhanced management (see also McKinsey Quarterly (2008)).

As noted by Capgemini in its 2008 report: *2016: Future Supply Chain*, *"Preserving energy and raw materials and other resources like water will become a crucial aspect in future supply chains, as costs will likely remain volatile and supplies will continue to dwindle."* These conditions may well create substantial pressure on current supply chain models.

Our Approach to Sustainability



Our Most Recent Book



Why More Research is Needed

Although the importance of sustainable supply chains to the sustainability of cities is being increasingly recognized (cf. Grant Thornton (2011)), in terms of not only the enhancement of business processes in terms of efficiency and cost reduction but also the reduction of negative environmental externalities as well as waste *there have been only limited modeling efforts that capture supply chains within a cities framework.*

Why More Research is Needed

Although the importance of sustainable supply chains to the sustainability of cities is being increasingly recognized (cf. Grant Thornton (2011)), in terms of not only the enhancement of business processes in terms of efficiency and cost reduction but also the reduction of negative environmental externalities as well as waste *there have been only limited modeling efforts that capture supply chains within a cities framework.*

Models of sustainable supply chains are important since *they enable the evaluation (before expensive investments are actually made) as to alternative network designs, technologies, as well as sensitivities to cost and demand structures.*

Why More Research is Needed

The edited volume of Taniguchi and Thompson (2004), which focuses on logistics systems for sustainable cities, *emphasized the unique features of urban logistical systems, which may include more frequent freight shipments and deliveries, with the concomitant negative externalities.*



Why More Research is Needed

Geroliminis and Daganzo (2005) further emphasize that the environmental impacts of logistical activities are most severe where population densities are highest, that is, in cities.

They have identified *innovative practices of cities around the globe in terms of their logistics systems and sustainability*, including the use of alternative modes of transportation, such as, for example, even bicycles for deliveries in Amsterdam and electric trams in Gothenburg.

Methodology

Methodology - The Variational Inequality Problem

We utilize the theory of variational inequalities for the formulation, analysis, and solution of both centralized and decentralized supply chain network problems.

Definition: The Variational Inequality Problem

The finite-dimensional variational inequality problem, $VI(F, \mathcal{K})$, is to determine a vector $X^ \in \mathcal{K}$, such that:*

$$\langle F(X^*), X - X^* \rangle \geq 0, \quad \forall X \in \mathcal{K},$$

where F is a given continuous function from \mathcal{K} to R^N , \mathcal{K} is a given closed convex set, and $\langle \cdot, \cdot \rangle$ denotes the inner product in R^N .

Methodology - The Variational Inequality Problem

The vector X consists of the decision variables – typically, the flows (products, prices, etc.).

\mathcal{K} is the feasible set representing how the decision variables are constrained – for example, the flows may have to be nonnegative; budget constraints may have to be satisfied; similarly, quality and/or time constraints may have to be satisfied.

The function F that enters the variational inequality represents functions that capture the behavior in the form of the functions such as costs, profits, risk, etc.

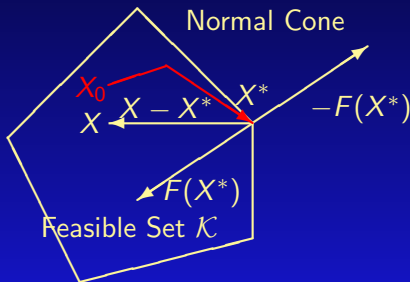
The variational inequality problem contains, as special cases, such mathematical programming problems as:

- systems of equations,
- optimization problems,
- complementarity problems,
- game theory problems, operating under Nash equilibrium,
- and is related to the fixed point problem.

Hence, it is a natural methodology for a spectrum of supply chain network problems from centralized to decentralized ones as well as to design problems.

Geometric Interpretation of $\text{VI}(F, \mathcal{K})$ and a Projected Dynamical System (Dupuis and Nagurney (1993), Nagurney and Zhang (1996))

In particular, $F(X^*)$ is “orthogonal” to the feasible set \mathcal{K} at the point X^* .



Associated with a VI is a Projected Dynamical System, which provides natural underlying dynamics associated with travel (and other) behavior to the equilibrium.

To model the *dynamic behavior of complex networks*, including supply chains, we utilize *projected dynamical systems* (PDSs) advanced by Dupuis and Nagurney (1993) in *Annals of Operations Research* and by Nagurney and Zhang (1996) in our book *Projected Dynamical Systems and Variational Inequalities with Applications*.

Such nonclassical dynamical systems are now being used in *evolutionary games* (Sandholm (2005, 2011)), *ecological predator-prey networks* (Nagurney and Nagurney (2011a, b)), and even *neuroscience* (Girard et al. (2008)).

Applied Supply Chain Network Game Theory Models of Relevance to Sustainable Cities

Electric Power Supply Chains

We developed *an empirical, large-scale electric supply chain network equilibrium model*, formulated it as a VI problem, and were able to solve it by *exploiting the connection between electric power supply chain networks and transportation networks* using our proof of a hypothesis posed in the classic book, *Studies in the Economics of Transportation*, by Beckmann, McGuire, and Winsten (1956).

The paper, “An Integrated Electric Power Supply Chain and Fuel Market Network Framework: Theoretical Modeling with Empirical Analysis for New England,” by Z. Liu and A. Nagurney was published in *Naval Research Logistics* **56** (2009) pp 600-624;

<http://supernet.isenberg.umass.edu/articles/LiuNagurneyNRL.pdf>

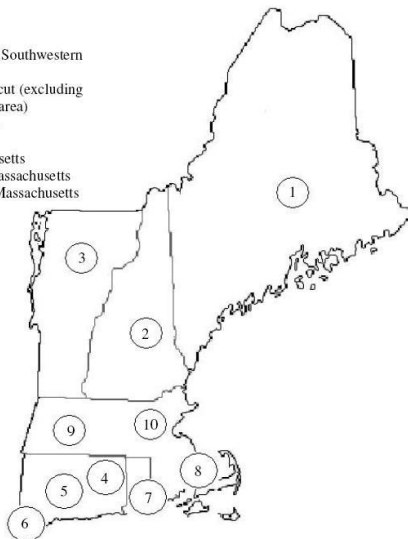
An Empirical Example of an Electric Power Supply Chain for New England

There are 82 generating companies who own and operate 573 generating units. We considered 5 types of fuels: natural gas, residual fuel oil, distillate fuel oil, jet fuel, and coal. The whole area was divided into 10 regions:

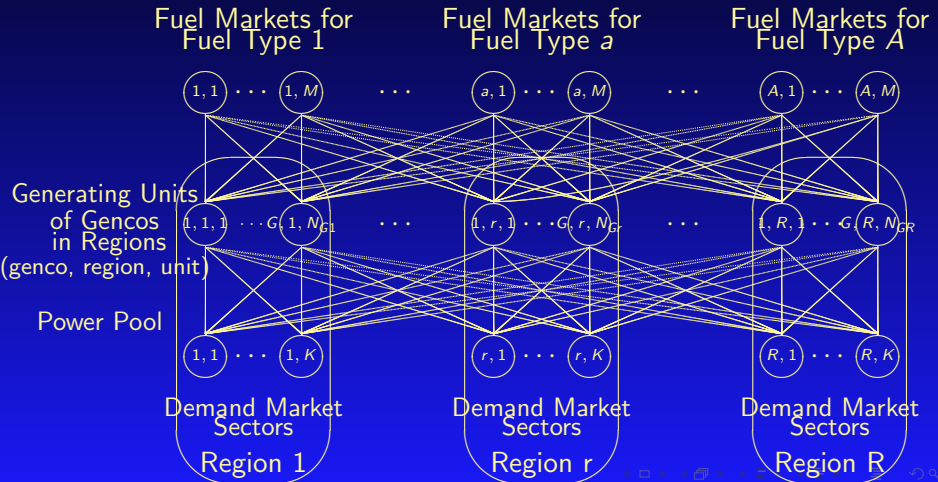
1. Maine,
2. New Hampshire,
3. Vermont,
4. Connecticut (excluding Southwest Connecticut),
5. Southwestern Connecticut (excluding the Norwalk-Stamford area),
6. Norwalk-Stamford area,
7. Rhode Island,
8. Southeastern Massachusetts,
9. Western and Central Massachusetts,
10. Boston/Northeast Massachusetts.

Graphic of New England

1. Maine
2. New Hampshire
3. Vermont
4. Connecticut (excluding Southwestern Connecticut)
5. Southwestern Connecticut (excluding the Norwalk-Stamford area)
6. Norwalk-Stamford area
7. Rhode Island
8. Southeastern Massachusetts
9. Western and Central Massachusetts
10. Boston/Northeastern Massachusetts



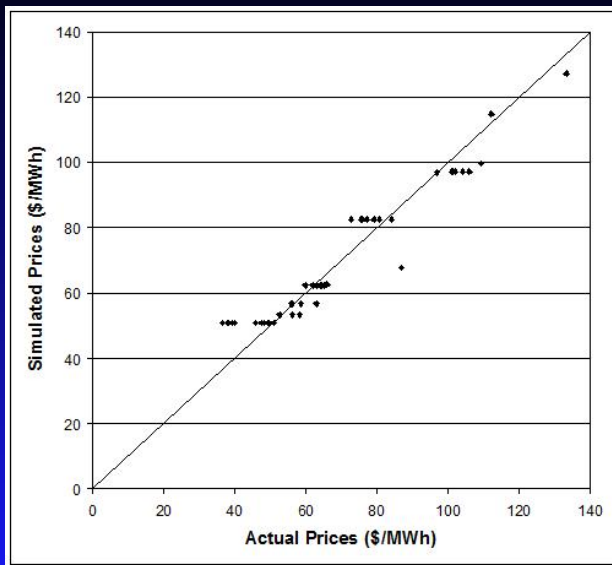
The Electric Power Supply Chain Network with Fuel Supply Markets



We tested the model on the data of July 2006 which included $24 \times 31 = 744$ hourly demand/price scenarios. We sorted the scenarios based on the total hourly demand, and constructed the load duration curve. We divided the duration curve into 6 blocks ($L_1 = 94$ hours, and $L_w = 130$ hours; $w = 2, \dots, 6$) and calculated the average regional demands and the average weighted regional prices for each block.

The empirical model had on the order of 20,000 variables.

Actual Prices Vs. Simulated Prices (\$/Mwh)



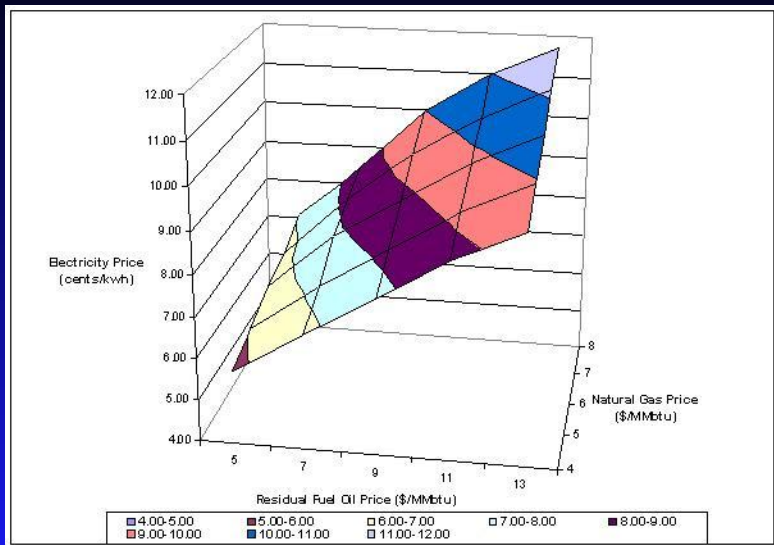
Sensitivity Analysis

We used the same demand data, and then varied the prices of natural gas and residual fuel oil. We assumed that the percentage change of distillate fuel oil and jet fuel prices were the same as that of the residual fuel oil price.

The next figure presents the average electricity price for the two peak blocks under oil/gas price variations.

The surface in the figure represents the average peak electricity prices under different natural gas and oil price combinations.

Sensitivity Analysis











Food Supply Chains

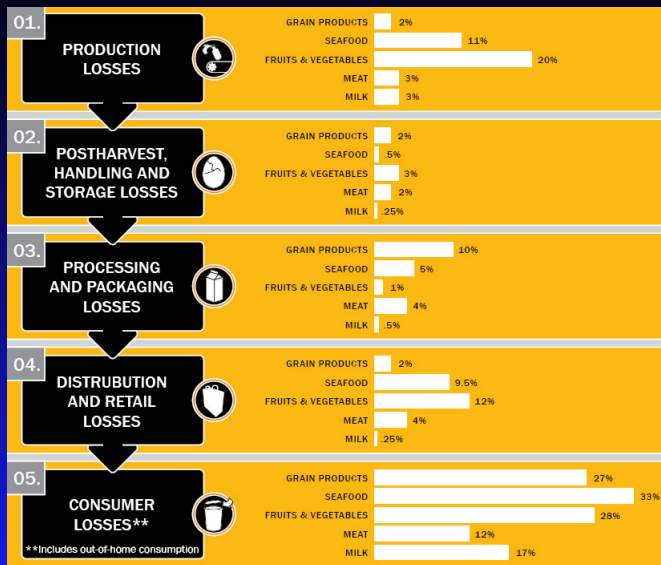
Food is something anyone can relate to.



Fascinating Facts About Food Perishability

THE SHELF LIFE OF FOOD			
Foods unopened, uncut or uncooked unless stated otherwise	COUNTER/PANTRY	REFRIGERATOR	FREEZER
	1 DAY ← → 1 MONTH	1 DAY ← → 3 MONTHS	1 MONTH ← → 1 YEAR
 APPLES	2-4 weeks	1-2 months	8-12 months
 BANANAS	2-7 days	5-9 days	2-3 months
 CANTALOUPE	Until ripe	1 week	8-12 months
 CARROTS	Up to 4 days	4-5 weeks	8-12 months
 CUCUMBERS	1-3 days	1 week	8-12 months
 EGGS	Few hours	3-4 weeks	Do not freeze
 MILK	Few hours	5-7 days	1 month
 VEGETABLES	Few hours	2-3 weeks	1-2 months

Fascinating Facts About Food Perishability



Source: Food and Agriculture Organization 2011

Fascinating Facts About Food Perishability

**ABOUT 10 PERCENT OF THE
U.S. ENERGY BUDGET GOES TO
BRINGING FOOD TO OUR TABLES.**

Source: Webber, Michael, "How to Make the Food System More Energy Efficient," *Scientific American*, December 29, 2011.



**ONE INDUSTRY CONSULTANT
ESTIMATES THAT UP TO ONE
IN SEVEN TRUCKLOADS OF
PERISHABLES DELIVERED TO
SUPERMARKETS IS THROWN AWAY.**

Source: Beswick, P. et al, "A Retailer's Recipe for Fresher Food and Far Less Shrink," Oliver Wyman, Boston. [ergpeditorial.biz/worksamples/OW%20grocery%20shrinkage.pdf](http://www.ergpeditorial.biz/worksamples/OW%20grocery%20shrinkage.pdf).

**FOR THE AVERAGE U.S. HOUSEHOLD OF
FOUR, FOOD WASTE TRANSLATES INTO
AN ESTIMATED \$1,350 TO \$2,275 IN
ANNUAL LOSSES.**



Source: Bloom, American Household, 187. Another report using updated USDA consumer loss numbers and 2011 prices estimates \$1,600 in annual losses per household of four. Clean Metrics, "The Climate Change and Economic Impacts of Food Waste in the United States," <http://www.cleanmetrics.com/wp-content/uploads/2012/04/foodwaste.pdf>

Source: Food and Agriculture Organization 2011



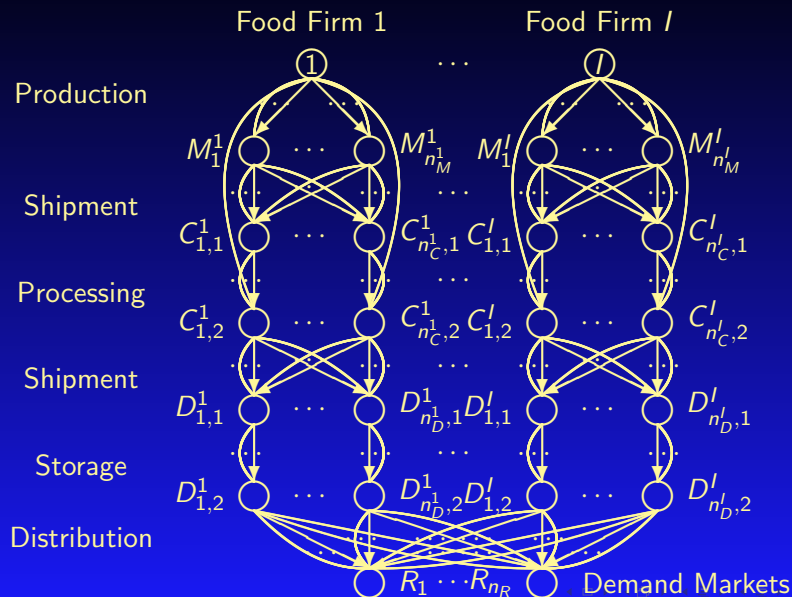
Fresh Produce Food Supply Chains

We developed a fresh produce supply chain network oligopoly model that

1. captures the deterioration of fresh food along the entire supply chain from a network perspective;
2. handles the exponential time decay through the introduction of arc multipliers;
3. formulates oligopolistic competition with product differentiation;
4. includes the disposal of the spoiled food products, along with the associated costs;
5. allows for the assessment of alternative technologies involved in each supply chain activity.

Reference: “Competitive Food Supply Chain Networks with Application to Fresh Produce,” M. Yu and A. Nagurney, *European Journal of Operational Research* **224(2)** (2013) pp 273-282.

Fresh Produce Food Supply Chains



The Sustainable Supply Chain Network Model with Frequency of Activities

The Sustainable Supply Chain Network Model with Frequency of Activities

- We present the model for sustainable supply chain networks with a focus of the frequency of the various supply chain activities.

The Sustainable Supply Chain Network Model with Frequency of Activities

- We present the model for sustainable supply chain networks with a focus of the frequency of the various supply chain activities.
- Logistics in cities are often characterized by more frequent shipments, especially using primarily freight vehicles such as trucks.

The Sustainable Supply Chain Network Model with Frequency of Activities

- We present the model for sustainable supply chain networks with a focus of the frequency of the various supply chain activities.
- Logistics in cities are often characterized by more frequent shipments, especially using primarily freight vehicles such as trucks.
- However, the scope of our model is broader and we also capture the optimal frequencies of the other activities, that is, those of manufacturing, storage, etc.

The Sustainable Supply Chain Network Model with Frequency of Activities

This paper is inspired, in part, by paper presented by Martin J. Beckmann: "Vehicle and Passenger Flows in Mass Transportation: Optimal Routing of Buses and Planes," at the Symposium on Transportation Network Design and Economics, Northwestern University, Evanston, Illinois, January 29, 2010.



The Sustainable Supply Chain Network Model with Frequencies

We consider the supply chain network topology depicted in the Figure but note that this network is simply representative and more disaggregation can be included, depending on the application.

The Sustainable Supply Chain Network Model with Frequencies

We consider the supply chain network topology depicted in the Figure but note that this network is simply representative and more disaggregation can be included, depending on the application.

The top level (origin) node 0 corresponds to the firm and the bottom level (destination) nodes correspond to the demand sites, which can denote, for example, retailers or consumers, that the firm wishes to supply.

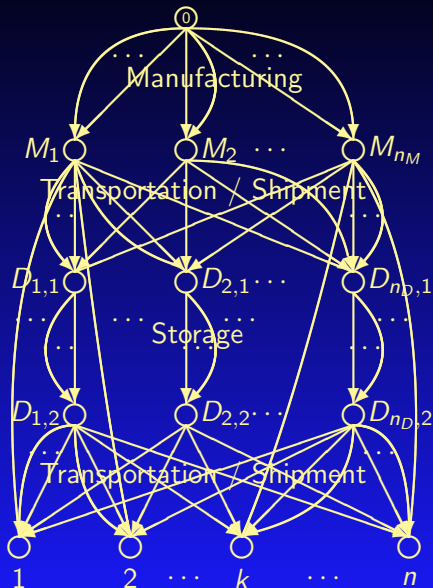
The Sustainable Supply Chain Network Model with Frequencies

We consider the supply chain network topology depicted in the Figure but note that this network is simply representative and more disaggregation can be included, depending on the application.

The top level (origin) node 0 corresponds to the firm and the bottom level (destination) nodes correspond to the demand sites, which can denote, for example, retailers or consumers, that the firm wishes to supply.

The paths joining the origin node to the destination nodes depict sequences of supply chain network activities that guarantee that the product is produced and is delivered to the demand sites.

The Supply Chain Network Topology



The Sustainable Supply Chain Network Model with Frequencies

Implicit in our framework is a time horizon, as, for example, a week, over which the relevant decisions are made and the activities conducted.

The Sustainable Supply Chain Network Model with Frequencies

Implicit in our framework is a time horizon, as, for example, a week, over which the relevant decisions are made and the activities conducted.

The supply chain network consisting of the graph $G = [N, L]$, with N denoting the set of nodes and L the set of directed links.

The Sustainable Supply Chain Network Model with Frequencies

Implicit in our framework is a time horizon, as, for example, a week, over which the relevant decisions are made and the activities conducted.

The supply chain network consisting of the graph $G = [N, L]$, with N denoting the set of nodes and L the set of directed links.

The firm seeks to minimize the total costs associated with its production, storage, and transportation/distribution activities, along with the total cost of link operation frequencies, plus the total cost of environmental impact and waste, which we elaborate upon below, subject to the demand being satisfied at the demand sites.

The Sustainable Supply Chain Network Model with Frequencies

We denote the links by a, b , etc., and the total cost on a link a by \hat{c}_a . For the sake of generality, we note that the total costs are generalized costs and may include, for example, risk, time, etc. (see also Nagurney (2010)).

The Sustainable Supply Chain Network Model with Frequencies

We denote the links by a, b , etc., and the total cost on a link a by \hat{c}_a . For the sake of generality, we note that the total costs are generalized costs and may include, for example, risk, time, etc. (see also Nagurney (2010)).

A path p in the network (see, e.g., Figure 1) joining node 0, which is the origin node, to a demand node, which is a destination node, represents the activities and their sequence associated with producing the product and having it, ultimately, delivered. Let w_k denote the pair of origin/destination (O/D) nodes $(0, k)$ and let P_{w_k} denote the set of paths, which represent alternative associated possible supply chain network processes, joining $(0, k)$. P is the set of all paths joining node 0 to the demand nodes. n_P denotes the number of paths from the organization to the demand markets.

The Sustainable Supply Chain Network Model with Frequencies

Let x_p represent the nonnegative flow of the product on path p joining (origin) node 0 with a (destination) demand node. Let d_k denote the demand, which is assumed to be known and fixed, for the product at demand location k .

The Sustainable Supply Chain Network Model with Frequencies

Let x_p represent the nonnegative flow of the product on path p joining (origin) node 0 with a (destination) demand node. Let d_k denote the demand, which is assumed to be known and fixed, for the product at demand location k .

The following conservation of flow equation must hold:

$$d_k \equiv \sum_{p \in P_{w_k}} x_p, \quad k = 1, \dots, n, \quad (1)$$

that is, the demand must be satisfied at each demand site.

The Sustainable Supply Chain Network Model with Frequencies

Let x_p represent the nonnegative flow of the product on path p joining (origin) node 0 with a (destination) demand node. Let d_k denote the demand, which is assumed to be known and fixed, for the product at demand location k .


The following conservation of flow equation must hold:

$$d_k \equiv \sum_{p \in P_{w_k}} x_p, \quad k = 1, \dots, n, \quad (1)$$

that is, the demand must be satisfied at each demand site.

Let f_a denote the flow of the product on link a . The following conservation of flow equations satisfied:

$$f_a = \sum_{p \in P} x_p \delta_{ap}, \quad \forall a \in L, \quad (2)$$

where $\delta_{ap} = 1$, if link a is contained in path p , and $\delta_{ap} = 0$, 

The Sustainable Supply Chain Network Model with Frequencies

The path flows must be nonnegative, that is,

$$x_p \geq 0, \quad \forall p \in P, \quad (3)$$

since the product will be produced in nonnegative quantities.

The Sustainable Supply Chain Network Model with Frequencies

The path flows must be nonnegative, that is,

$$x_p \geq 0, \quad \forall p \in P, \quad (3)$$

since the product will be produced in nonnegative quantities.

The total operational cost on a link, be it a manufacturing / production link, a transportation / shipment link, or a storage link is assumed to be a function of the flow of the product on the link; see, for example, Nagurney and Nagurney (2010) and Nagurney (2006) and the references therein. We have, thus, that

$$\hat{c}_a = \hat{c}_a(f_a), \quad \forall a \in L. \quad (4)$$

The Sustainable Supply Chain Network Model with Frequencies

We assume that the total cost on each link is convex and is continuously differentiable.

We denote the total cost of operating link a at a frequency γ_a by $\hat{\pi}_a$, $\forall a \in L$, and assume that

$$\hat{\pi}_a = \hat{\pi}_a(\gamma_a), \quad \forall a \in L. \quad (5)$$

These frequency operational cost functions are assumed to be convex and continuously differentiable and to have bounded second order partial derivatives.

The Sustainable Supply Chain Network Model with Frequencies

The firm seeks to determine the optimal levels of product processed on each supply chain network link coupled with the optimal levels of frequency link operation subject to the minimization of the total cost.

The Sustainable Supply Chain Network Model with Frequencies

The firm seeks to determine the optimal levels of product processed on each supply chain network link coupled with the optimal levels of frequency link operation subject to the minimization of the total cost.

The firm is faced with the following objective function:

$$\text{Minimize } \sum_{a \in L} \hat{c}_a(f_a) + \hat{\pi}_a(\gamma_a). \quad (6)$$

The Sustainable Supply Chain Network Model with Frequencies

The firm is concerned with the environmental impact of its activities, which can include not only the emissions generated but also noise pollution, as well as other types of pollution and infrastructure deterioration.

Let $\hat{e}_a(f_a, \gamma_a)$, $\forall a \in L$, denote the environmental impact function associated with link a . Let $\hat{z}_a(f_a)$, $a \in L$, denote the waste management cost associated with link a , $a \in L$. They are assumed to be convex and continuously differentiable and to have bounded second order partial derivatives, as are the ones above.

The Sustainable Supply Chain Network Model with Frequencies

The firm is concerned with the environmental impact of its activities, which can include not only the emissions generated but also noise pollution, as well as other types of pollution and infrastructure deterioration.

Let $\hat{e}_a(f_a, \gamma_a)$, $\forall a \in L$, denote the environmental impact function associated with link a . Let $\hat{z}_a(f_a)$, $a \in L$, denote the waste management cost associated with link a , $a \in L$. They are assumed to be convex and continuously differentiable and to have bounded second order partial derivatives, as are the ones above.

The second objective of the firm is then given by:

$$\text{Minimize} \quad \sum_{a \in L} \hat{e}_a(f_a, \gamma_a) + \hat{z}_a(f_a). \quad (7)$$

The Sustainable Supply Chain Network Model with Frequencies

The Multicriteria Optimization Problem for Sustainable Supply Chain Network Design with Frequency of Activities

A nonnegative constant ω is now assigned to the environmental criterion (7). The constant ω is a weight that the firm assigns. Of course, ω can also be interpreted as a “tax” imposed by the governmental/environmental authority (see, e.g., Wu et al. (2006)).

The Sustainable Supply Chain Network Model with Frequencies

We assume, as given, a parameter $\bar{u}_a, \forall a \in L$. These parameters denote the existing capacities of the links.

For example, for a manufacturing link \bar{u}_a would denote the capacity of production, that is, the volume of the product that could be produced on the link; for a storage link a , the capacity would denote how much of the product could be stored there, and, similarly, for a transportation/shipment link, \bar{u}_a would represent the amount that could be shipped (could denote a truckload, for example).

The Sustainable Supply Chain Network Model with Frequencies

Using results from multicriteria optimization (see, e.g., Nagurney and Dong (2002)), one can then construct the following:

$$\text{Minimize} \quad \sum_{a \in L} \hat{c}_a(f_a) + \hat{\pi}_a(\gamma_a) + \omega \left(\sum_{a \in L} \hat{e}_a(f_a, \gamma_a) + \hat{z}_a(f_a) \right). \quad (8)$$

The firm seeks to solve (8), subject to the constraints: (1), (2), (3), and

$$f_a \leq \bar{u}_a \gamma_a, \quad \forall a \in L. \quad (9)$$

$$0 \leq \gamma_a, \quad \forall a \in L. \quad (10)$$

Constraint (9) guarantees that the product flow on a link does not exceed that link's capacity times the frequency of replenishment.

The Sustainable Supply Chain Network Model with Frequencies

We associate the Lagrange multiplier μ_a with constraint (9) for each link $a \in L$ and denote the associated optimal Lagrange multiplier by μ_a^* . These terms may also be interpreted as the price or value of an additional unit of “capacity” on link a . We group these Lagrange multipliers into the respective vectors μ and μ^* .

The Variational Inequality Formulation

Theorem 1

The optimization problem (8), subject to the constraints (1) – (3), (9), and (10), is equivalent to the variational inequality problem: determine the vectors of link flows, link operation frequencies, and Lagrange multipliers $(f^, \gamma^*, \mu^*) \in K$, such that:*

$$\begin{aligned} & \sum_{a \in L} \left[\frac{\partial \hat{c}_a(f_a^*)}{\partial f_a} + \omega \frac{\partial \hat{e}_a(f_a^*, \gamma_a^*)}{\partial f_a} + \omega \frac{\partial \hat{z}_a(f_a^*)}{\partial f_a} + \mu_a^* \right] \times [f_a - f_a^*] \\ & + \sum_{a \in L} \left[\frac{\partial \hat{\pi}_a(\gamma_a^*)}{\partial \gamma_a} + \omega \frac{\partial \hat{e}_a(f_a^*, \gamma_a^*)}{\partial \gamma_a} - \bar{u}_a \mu_a^* \right] \times [\gamma_a - \gamma_a^*] \\ & + \sum_{a \in L} [\bar{u}_a \gamma_a^* - f_a^*] \times [\mu_a - \mu_a^*] \geq 0, \quad \forall (f, \gamma, \mu) \in K, \end{aligned} \quad (11)$$

$K \equiv \{(f, \gamma, \mu) | \exists x \geq 0, \text{ and (1), (2), and (10) hold, and } \mu \geq 0\}$, where f is the vector of link flows, γ is the vector of link operation frequencies, and μ is the vector of Lagrange multipliers.

The Variational Inequality Formulation

Variational inequality (11) can be put into standard form (see Nagurney (1999)): determine $X^* \in \mathcal{K}$ such that:

$$\langle F(X^*), X - X^* \rangle \geq 0, \quad \forall X \in \mathcal{K}, \quad (12)$$

where $\langle \cdot, \cdot \rangle$ denotes the inner product in \mathcal{N} -dimensional Euclidean space. If we define the column vectors: $X \equiv (f, \gamma, \mu)$ and $F(X) \equiv (F_1(X), F_2(X), F_3(X))$, such that

$$F_1(X) \equiv \left[\frac{\partial \hat{c}_a(f_a)}{\partial f_a} + \omega \frac{\partial \hat{e}_a(f_a, \gamma_a)}{\partial f_a} + \omega \frac{\partial \hat{z}_a(f_a)}{\partial f_a} + \mu_a; \quad a \in L \right], \quad (13)$$

$$F_2(X) \equiv \left[\frac{\partial \hat{\pi}_a(\gamma_a)}{\partial \gamma_a} + \omega \frac{\partial \hat{e}_a(f_a, \gamma_a)}{\partial \gamma_a} - \bar{u}_a \mu_a; \quad a \in L \right], \quad (14)$$

$$F_3(X) \equiv [\bar{u}_a \gamma_a - f_a; \quad a \in L], \quad (15)$$

and define $\mathcal{K} \equiv K$, then (11) can be re-expressed as (12).

Special Case of the Model

Let $\bar{u}_a = 1$ and let $\hat{\pi}_a$ now denote the total cost associated with investment to a level of operation γ_a on link a , for $a \in L$.

Special Case of the Model

Corollary 1

Under the preceding assumptions, the optimality conditions for the sustainable supply chain network model take on the following variational inequality form: determine the vectors of link flows, link capacity investments, and Lagrange multipliers $(f^, \gamma^*, \mu^*) \in K^1$:*

$$\begin{aligned} & \sum_{a \in L} \left[\frac{\partial \hat{c}_a(f_a^*)}{\partial f_a} + \omega \frac{\partial \hat{e}_a(f_a^*, \gamma_a^*)}{\partial f_a} + \omega \frac{\partial \hat{z}_a(f_a^*)}{\partial f_a} + \mu_a^* \right] \times [f_a - f_a^*] \\ & + \sum_{a \in L} \left[\frac{\partial \hat{\pi}_a(\gamma_a^*)}{\partial \gamma_a} + \omega \frac{\partial \hat{e}_a(f_a^*, \gamma_a^*)}{\partial \gamma_a} - \mu_a^* \right] \times [\gamma_a - \gamma_a^*] \\ & + \sum_{a \in L} [\gamma_a^* - f_a^*] \times [\mu_a - \mu_a^*] \geq 0, \quad \forall (f, \gamma, \mu) \in K^1, \end{aligned} \quad (16)$$

$K^1 \equiv \{(f, \gamma, \mu) | \exists x \geq 0, (1), (2), \text{ and } (10) \text{ hold with } \bar{u}_a = 1, \forall a, \mu \geq 0\}.$

Qualitative Properties

Theorem 2

The function $F(X)$ as defined following (12) (see (13) – (15)), under the assumptions above, is monotone, that is,

$$\langle (F(X^1) - F(X^2)), X^1 - X^2 \rangle \geq 0, \quad \forall X^1, X^2 \in \mathcal{K}. \quad (17)$$

Qualitative Properties

Theorem 2

The function $F(X)$ as defined following (12) (see (13) – (15)), under the assumptions above, is monotone, that is,

$$\langle (F(X^1) - F(X^2)), X^1 - X^2 \rangle \geq 0, \quad \forall X^1, X^2 \in \mathcal{K}. \quad (17)$$

Theorem 3

The function $F(X)$ as defined following (12) is Lipschitz continuous, that is,

$$\|F(X^1) - F(X^2)\| \leq \|X^1 - X^2\|, \quad \forall X^1, X^2 \in \mathcal{K}. \quad (18)$$

It is important to realize that linear functions are convex and continuously differentiable. Hence, our model can be applied (and solved) under many different not unreasonable cost settings.

Convergence of the Algorithmic Scheme

Theorem 4: Convergence

Assume that the function that enters the variational inequality (11) (or (12)) has at least one solution and satisfies the conditions in Theorem 2 and in Theorem 3. Then the modified projection method converges to the solution of variational inequality (11) (or (12)) and, similarly, due to Corollary 1, to the solution of (16).

Numerical Examples

Numerical Examples

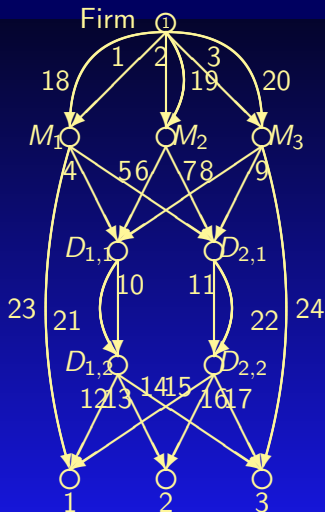
The modified projected method was implemented and a Unix system at the University of Massachusetts Amherst was used for all the computations.

We initialized the algorithm by equally distributing the demand at each demand site among all the paths joining the firm node 0 to the demand node.

All other variables (the link frequencies and the Lagrange multipliers) were initialized to zero. We used the equilibration algorithm (cf. Dafermos and Sparrow (1969) and Nagurney (1999)) for the solution of the embedded quadratic programming network optimization problems.

The numerical examples were solved to a high degree of accuracy since the imposed convergence criterion guaranteed that the absolute value of successive iterates differed by no more than 10^{-5} .

The Supply Chain Network Topology $G = [N, L]$ for the Examples



Numerical Examples

The numerical examples consisted of a firm faced with 3 possible manufacturing plants, each of which had 2 possible technologies, 2 distribution centers, each of which also had 2 distinct technologies, and the firm had to supply the 3 demand points.

Numerical Examples

The numerical examples consisted of a firm faced with 3 possible manufacturing plants, each of which had 2 possible technologies, 2 distribution centers, each of which also had 2 distinct technologies, and the firm had to supply the 3 demand points.

Demand points 1 and 3 had direct shipments from the respective manufacturing plants permitted, as depicted in the Figure.

Numerical Examples

The numerical examples consisted of a firm faced with 3 possible manufacturing plants, each of which had 2 possible technologies, 2 distribution centers, each of which also had 2 distinct technologies, and the firm had to supply the 3 demand points.

Demand points 1 and 3 had direct shipments from the respective manufacturing plants permitted, as depicted in the Figure.

The common input data for the first two examples are reported in Table 1.

Numerical Examples

The numerical examples consisted of a firm faced with 3 possible manufacturing plants, each of which had 2 possible technologies, 2 distribution centers, each of which also had 2 distinct technologies, and the firm had to supply the 3 demand points.

Demand points 1 and 3 had direct shipments from the respective manufacturing plants permitted, as depicted in the Figure.

The common input data for the first two examples are reported in Table 1.

The first two examples had link capacities as reported in Table 1. The third numerical example (since it was a supply chain network design example) had $\bar{u}_a = 1$ for all links a , with the interpretation that the optimal values for the γ_a^* , for all links $a \in L$, would reflect the effective optimal capacities of the corresponding links (see, e.g., Nagurney (2010)).

The Input Data

Table 1: Total Operating and Frequency Cost Functions, Environmental Impact Cost and Waste Cost Functions, and Link Capacities for Numerical Examples 1 and 2

Link	$\hat{c}_a(f_a)$	$\hat{\pi}_a(\gamma_a)$	$\hat{e}_a(f_a, \gamma_a)$	$\hat{z}_a(f_a)$	\bar{u}_a
1	$.5f_1^2 + 2f_1$	$.5\gamma_1^2 + \gamma_1$	$.05f_1^2 + f_1 + 1.5\gamma_1^2 + 2\gamma_1$	$.05f_1^2 + f_1$	100.
2	$.5f_2^2 + f_2$	$2.5\gamma_2^2 + \gamma_2$	$.1f_2^2 + f_2 + 2\gamma_2^2 + 2\gamma_2$	$.1f_2^2 + 2f_2$	100.
3	$.5f_3^2 + f_3$	$\gamma_3^2 + 2\gamma_3$	$.15f_3^2 + 2f_3 + 2.5\gamma_3^2 + \gamma_3$	$.25f_3^2 + 5f_3$	200.
4	$1.5f_4^2 + 2f_4$	$\gamma_4^2 + \gamma_4$	$.05f_4^2 + .1f_4 + .1\gamma_4^2 + .2\gamma_4$	$.05f_4^2 + 2f_4$	20.
5	$f_5^2 + 3f_5$	$2.5\gamma_5^2 + 2\gamma_5$	$.05f_5^2 + .1f_5 + .05\gamma_5^2 + .1\gamma_5$	$.1f_5^2 + 3f_5$	20.
6	$f_6^2 + 2f_6$	$.5\gamma_6^2 + \gamma_6$	$.1f_6^2 + .1f_6 + .05\gamma_6^2 + .1\gamma_6$	$.05f_6^2 + f_6$	20.
7	$.5f_7^2 + 2f_7$	$.5\gamma_7^2 + \gamma_7$	$.05f_7^2 + .2f_7 + .1\gamma_7^2 + .2\gamma_7$	$.25f_7^2 + f_7$	20.
8	$.5f_8^2 + 2f_8$	$1.5\gamma_8^2 + \gamma_8$	$.05f_8^2 + .1f_8 + .1\gamma_8^2 + .3\gamma_8$	$.2f_8^2 + 2f_8$	10.
9	$f_9^2 + 5f_9$	$2\gamma_9^2 + 3\gamma_9$	$.05f_9^2 + .1f_9 + .1\gamma_9^2 + .2\gamma_9$	$.1f_9^2 + 5f_9$	10.
10	$.5f_{10}^2 + 2f_{10}$	$\gamma_{10}^2 + 5\gamma_{10}$	$.2f_{10}^2 + f_{10} + 1.5\gamma_{10}^2 + 3\gamma_{10}$	$.05f_{10}^2 + 5f_{10}$	50.
11	$f_{11}^2 + f_{11}$	$.5\gamma_{11}^2 + 3\gamma_{11}$	$.25f_{11}^2 + 3f_{11} + 2\gamma_{11}^2 + 3\gamma_{11}$	$.1f_{11}^2 + 2f_{11}$	50.
12	$.5f_{12}^2 + 2f_{12}$	$.5\gamma_{12}^2 + \gamma_{12}$	$.05f_{12}^2 + .1f_{12} + .1\gamma_{12}^2 + .2\gamma_{12}$	$.05f_{12}^2 + 3f_{12}$	15.
13	$.5f_{13}^2 + 5f_{13}$	$.5\gamma_{13}^2 + \gamma_{13}$	$.1f_{13}^2 + .1f_{13} + .05\gamma_{13}^2 + .1\gamma_{13}$	$.05f_{13}^2 + 5f_{13}$	15.
14	$f_{14}^2 + 7f_{14}$	$2\gamma_{14}^2 + 5\gamma_{14}$	$.15f_{14}^2 + .2f_{14} + .1\gamma_{14}^2 + .1\gamma_{14}$	$.05f_{14}^2 + 3f_{14}$	15.
15	$f_{15}^2 + 2f_{15}$	$.5\gamma_{15}^2 + \gamma_{15}$	$.05f_{15}^2 + .3f_{15} + .1\gamma_{15}^2 + .2\gamma_{15}$	$.1f_{15}^2 + 5f_{15}$	20.

The Input Data

Table 2: Total Operating and Frequency Cost Functions, Environmental Impact Cost and Waste Cost Functions, and Link Capacities for Numerical Examples 1 and 2

16	$.5f_{16}^2 + 3f_{16}$	$\gamma_{16}^2 + \gamma_{16}$	$.05f_{16}^2 + .1f_{16} + .1\gamma_{16}^2 + .1\gamma_{16}$	$.15f_{16}^2 + 3f_{16}$	20.
17	$.5f_{17}^2 + 2f_{17}$	$.5\gamma_{17}^2 + \gamma_{17}$	$.15f_{17}^2 + .3f_{17} + .05\gamma_{17}^2 + .1\gamma_{17}$	$.1f_{17}^2 + 5f_{17}$	20.
18	$.5f_{18}^2 + f_{18}$	$\gamma_{18}^2 + 2\gamma_{18}$	$.2f_{18}^2 + 2f_{18} + 2\gamma_{18}^2 + 3\gamma_{18}$	$.05f_{18}^2 + f_{18}$	100.
19	$.5f_{19}^2 + 2f_{19}$	$\gamma_{19}^2 + \gamma_{19}$	$.25f_{19}^2 + 3f_{19} + 3\gamma_{19}^2 + 4\gamma_{19}$	$.1f_{19}^2 + 2f_{19}$	200.
20	$1.5f_{20}^2 + f_{20}$	$\gamma_{20}^2 + \gamma_{20}$	$.3f_{20}^2 + 3f_{20} + 2.5\gamma_{20}^2 + 5\gamma_{20}$	$.15f_{20}^2 + f_{20}$	100.
21	$.5f_{21}^2 + 2f_{21}$	$\gamma_{21}^2 + 3\gamma_{21}$	$.1f_{21}^2 + 3f_{21} + 1.5\gamma_{21}^2 + 4\gamma_{21}$	$.15f_{21}^2 + 3f_{21}$	100.
22	$f_{22}^2 + 3f_{22}$	$.5\gamma_{22}^2 + 2\gamma_{22}$	$.05f_{22}^2 + 4f_{22} + 2.5\gamma_{22}^2 + 4\gamma_{22}$	$.25f_{22}^2 + 5f_{22}$	100.
23	$.5f_{23}^2 + f_{23}$	$.25\gamma_{23}^2 + \gamma_{23}$	$.2f_{23}^2 + f_{23} + \gamma_{23}^2 + 2\gamma_{23}$	$.2f_{23}^2 + 4f_{23}$	150.
24	$f_{24}^2 + f_{24}$	$.25\gamma_{24}^2 + \gamma_{24}$	$.1f_{24}^2 + 3f_{24} + .05\gamma_{24}^2 + 2\gamma_{24}$	$.1f_{24}^2 + 2f_{24}$	150.

Example 1

In Example 1 the demands were:

$$d_1 = 100, \quad d_2 = 200, \quad d_3 = 100.$$

Example 1

In Example 1 the demands were:

$$d_1 = 100, \quad d_2 = 200, \quad d_3 = 100.$$

In Example 1 we assumed that the firm did not care about the environmental impact and the waste generated in its supply chain and, hence, $\omega = 0$. The computed solution is reported in Table 2.

Example 1 Solution

Table 3: Example 1 Optimal Solution

Link	f_a^*	γ_a^*	μ_a^*
1	74.61	.7461	.0175
2	58.08	.5808	.0390
3	100.71	.5035	.0150
4	25.30	1.2651	.1765
5	24.89	1.2443	.4111
6	46.75	2.3373	.1669
7	68.45	3.4228	.2211
8	49.52	4.9520	1.5856
9	11.20	1.1202	.7481
10	60.73	1.2146	.1486
11	52.76	1.0551	.0811
12	0.00	.0000	.0000
13	108.47	7.2307	.5481
14	13.10	.83733	.5662
15	0.00	.0000	.0000

Example 1 Solution

Table 4: Example 1 Optimal Solution

Link a	f_a^*	γ_a^*	μ_a^*
16	91.53	4.5766	.5076
17	13.01	.6506	.0826
18	75.58	.7558	.0351
19	57.12	.2856	.0079
20	33.90	.3390	.0168
21	60.84	.6084	.0422
22	51.79	.5179	.0252
23	100.00	.6667	.0089
24	73.89	.4926	.0083

Example 1 Solution

The total cost (see objective function (6)) was: 55,920.97. The total environmental impact cost (see objective function (7)) was: 11,966.57, and the total waste costs were: 15,551.25. The value of the objective function (8) was, hence, 55.920.97.

Example 1 Solution

The total cost (see objective function (6)) was: 55,920.97. The total environmental impact cost (see objective function (7)) was: 11,966.57, and the total waste costs were: 15,551.25. The value of the objective function (8) was, hence, 55.920.97.

All the demand for demand market 1 is fulfilled through link 23 since links 12 and 15 have zero product flow on them. Of course, the corresponding frequencies of operating these links is also zero.

Example 1 Solution

The total cost (see objective function (6)) was: 55,920.97. The total environmental impact cost (see objective function (7)) was: 11,966.57, and the total waste costs were: 15,551.25. The value of the objective function (8) was, hence, 55.920.97.

All the demand for demand market 1 is fulfilled through link 23 since links 12 and 15 have zero product flow on them. Of course, the corresponding frequencies of operating these links is also zero.

Also, since, in this example, the firm is not at all concerned about its environmental impact and wastes generated, the value of the objective function corresponds to the total operational and frequency costs.

Example 2

Example 2 had the identical data as in Example 1 except that the firm was now concerned about the environment with $\omega = 1$. The new computed solution is given in Table 3.

Example 2 Solution

Table 5: Example 2 Optimal Solution

Link a	f_a^*	γ_a^*	μ_a^*
1	90.32	.9032	.0661
2	62.87	.6287	.0866
3	84.87	.4223	.0298
4	31.83	1.5913	.2351
5	30.93	1.5471	.4994
6	53.64	2.6821	.2026
7	59.35	2.9677	.2381
8	35.89	3.5892	1.2784
9	8.70	.8703	.6857
10	60.29	1.2057	.2806
11	52.30	1.0461	.2246
12	0.00	.0000	.0000
13	109.41	7.2947	.6089
14	11.95	.7966	.5630
15	0.00	.0000	.0000

Example 2 Solution

Table 6: Example 2 Optimal Solution

Link a	f_a^*	γ_a^*	μ_a^*
16	90.59	4.5294	.5533
17	8.41	.4204	.0781
18	72.45	.7245	.0935
19	50.13	.2506	.0350
20	39.77	.3977	.0878
21	61.07	.6107	.1005
22	46.69	.4669	.0880
23	100.00	.6667	.0311
24	79.64	.5310	.0085

Example 2 Solution

The total cost (see objective function (6)) was now: 56,632.07. The environmental impact cost (see objective function (7)) was now: 11,468.64. The waste cost was: 14,326.37. The value of the objective function (8) was, hence, 82,427.09. Due to the higher weight on the environmental and waste costs, the impact on the environment was reduced. However, as a consequence, the total cost is now higher than in Example 1 although not substantially so.

Example 2 Solution

The total cost (see objective function (6)) was now: 56,632.07. The environmental impact cost (see objective function (7)) was now: 11,468.64. The waste cost was: 14,326.37. The value of the objective function (8) was, hence, 82,427.09. Due to the higher weight on the environmental and waste costs, the impact on the environment was reduced. However, as a consequence, the total cost is now higher than in Example 1 although not substantially so.

Links 12 and 15, which are transportation/shipment links, are not used/operated, as was also the case in Example 1.

Example 2 Solution

The total cost (see objective function (6)) was now: 56,632.07. The environmental impact cost (see objective function (7)) was now: 11,468.64. The waste cost was: 14,326.37. The value of the objective function (8) was, hence, 82,427.09. Due to the higher weight on the environmental and waste costs, the impact on the environment was reduced. However, as a consequence, the total cost is now higher than in Example 1 although not substantially so.

Links 12 and 15, which are transportation/shipment links, are not used/operated, as was also the case in Example 1.

As expected, there is a transfer of production to the more environmentally-friendly manufacturing plants, with the associated technologies of production.

Example 3

Example 3 had the same data as Example 2 except that the $\bar{u}_1 = 1$ for all links $a = 1, \dots, 24$. hence, the firm, in Example 1, was interested in designing a sustainable supply chain network for the product, with concern for the environment.

Example 3

Example 3 had the same data as Example 2 except that the $\bar{u}_1 = 1$ for all links $a = 1, \dots, 24$. hence, the firm, in Example 1, was interested in designing a sustainable supply chain network for the product, with concern for the environment.

We kept the cost data for Example 3 as in Example 2 for comparison purposes. For actual design purposes one would need to increase the values of the $\hat{\pi}_a$ functions for all links $a \in L$, since these would then reflect actual construction/investment costs in the links (cf. Nagurney (2010)).

Here our goal was to demonstrate the flexibility of the modeling and computational framework.

The computed solution is reported in Table 4.

Example 3 Solution

Table 7: Example 3 Optimal Solution

Link a	f_a^*	γ_a^*	μ_a^*
1	97.25	97.25	391.9421
2	52.05	52.05	471.3385
3	70.95	70.95	499.5281
4	39.78	39.78	88.7147
5	24.65	24.65	127.7666
6	53.33	53.33	59.7681
7	54.01	4.01	66.0133
8	19.80	19.80	64.6667
9	8.43	8.43	38.5899
10	56.30	56.30	289.4470
11	47.05	47.05	241.1960
12	0.00	.0000	.0000
13	112.92	112.92	125.3066
14	0.00	.0000	5.1009
15	0.00	.0000	.3203

Example 3 Solution

Table 8: Example 3 Optimal Solution

Link a	f_a^*	γ_a^*	μ_a^*
16	87.08	87.08	192.6962
17	0.00	.0000	.0000
18	67.18	67.18	407.9846
19	55.29	55.29	447.2140
20	57.28	57.28	406.8561
21	56.61	56.61	289.9844
22	40.04	40.04	246.2007
23	100.00	100.00	252.9854
24	100.00	100.00	51.0052

Example 3 Solution

The total cost was: 122,625.56. The environmental impact was now: 102,133.26. The waste cost was: 13,464.07. The value of the objective function (8) was 238,222.89.

Example 3 Solution

The total cost was: 122,625.56. The environmental impact was now: 102,133.26. The waste cost was: 13,464.07. The value of the objective function (8) was 238,222.89.

Since links 12, 14, 15, and 17, have zero flows and zero effective capacities on those links, the optimal sustainable supply chain network design topology is given by the topology in the next Figure.

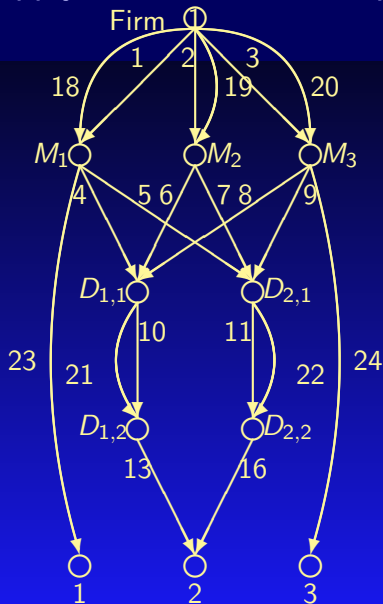
Example 3 Solution

The total cost was: 122,625.56. The environmental impact was now: 102,133.26. The waste cost was: 13,464.07. The value of the objective function (8) was 238,222.89.

Since links 12, 14, 15, and 17, have zero flows and zero effective capacities on those links, the optimal sustainable supply chain network design topology is given by the topology in the next Figure.

Demand points 1 and 3 are now served exclusively through direct shipments following the manufacture of the product.

The Optimal Supply Chain Network Topology for Example 3



One can conduct additional sensitivity analysis exercises to evaluate, for example, the effects of increases in population and, hence, the demand for the product.

One can conduct additional sensitivity analysis exercises to evaluate, for example, the effects of increases in population and, hence, the demand for the product.

When we doubled the demands at each of the three demand points in Examples 1 through 3, the same links had zero flows as under the original demands. This kind of information is useful for a firm. One can also explore increases in the weight ω and improvements in environmental technologies.

One can conduct additional sensitivity analysis exercises to evaluate, for example, the effects of increases in population and, hence, the demand for the product.

When we doubled the demands at each of the three demand points in Examples 1 through 3, the same links had zero flows as under the original demands. This kind of information is useful for a firm. One can also explore increases in the weight ω and improvements in environmental technologies.

The above examples, although stylized, illustrate the practicality and flexibility of the sustainable supply chain network modeling approach and algorithm.

An Extension to Capture Competition

An Extension to Capture Competition

In the paper, “Supply Chain Network Sustainability Under Competition and Frequencies of Activities from Production to Distribution,” A. Nagurney, M. Yu, and J. Floden, *Computational Management Science* **10(4)** (2013) pp 397-422, we extended the model to include competition and product differentiation.

Now the firms are profit-maximizers and control both their product flows and the frequencies associated with the supply chain network activities.

An Extension to Capture Competition

We utilize game theory and the Nash equilibrium concept and formulate the governing equilibrium conditions as a variational inequality problem.

We construct a weighted utility function associated with the two criteria faced by each firm. The term ω_i is assumed to be the price that firm i would be willing to pay for each unit of emission on each of its links and it is nonnegative.

The multicriteria decision-making problem faced by firm i ; $i = 1, \dots, I$, is:

$$U_i = \sum_{k=1}^{n_R} \hat{p}_{ik}(x) \sum_{p \in P_k^i} x_p - \sum_{a \in L^i} \hat{c}_a(f) - \sum_{a \in L^i} \hat{g}_a(\gamma_a) - \omega_i \sum_{a \in L^i} \hat{e}_a(f_a, \gamma_a). \quad (19)$$

An Extension to Capture Competition

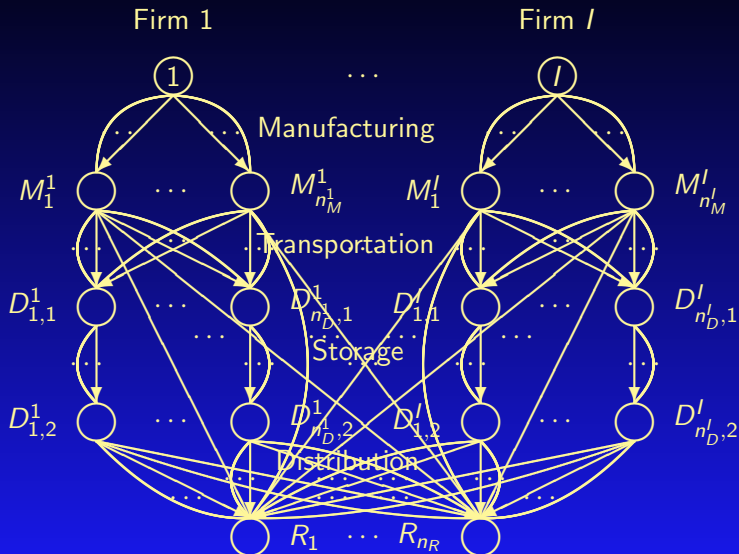


Figure 2: The Sustainable Supply Chain Network Topology that Captures

Definition: Supply Chain Network Cournot-Nash Equilibrium

A path flow and link frequency pattern $Y^* \in K = \prod_{i=1}^l K_i$ is said to constitute a supply chain network Cournot-Nash equilibrium if for each firm i ; $i = 1, \dots, l$:

$$\hat{U}_i(Y_i^*, \hat{Y}_i^*) \geq \hat{U}_i(Y_i, \hat{Y}_i^*), \quad \forall Y_i \in K_i, \quad (20)$$

where $\hat{Y}_i^* \equiv (Y_1^*, \dots, Y_{i-1}^*, Y_{i+1}^*, \dots, Y_l^*)$ and $K_i \equiv \{Y_i | Y_i \in R_+^{n_{Pi} + n_{Li}}\}$.

According to (20), an equilibrium is established if no firm can individually improve its utility, by changing its production path flows and its activity frequencies, given the decisions of the other firms.

Theorem 5

Assume that for each firm i ; $i = 1, \dots, I$, the utility function $\hat{U}_i(Y)$ is concave with respect to the variables in Y_i , and is continuously differentiable. Then $Y^ \in K$ is a sustainable supply chain network Cournot-Nash equilibrium according to Definition 1 if and only if it satisfies the variational inequality:*

$$-\sum_{i=1}^I \langle \nabla_{Y_i} \hat{U}_i(Y^*), Y_i - Y_i^* \rangle \geq 0, \quad \forall Y \in K, \quad (21)$$

where $\langle \cdot, \cdot \rangle$ denotes the inner product in the corresponding Euclidean space and $\nabla_{Y_i} \hat{U}_i(Y)$ denotes the gradient of $\hat{U}_i(Y)$ with respect to Y_i .

Summary and Conclusions

Summary and Conclusions

- ▶ We provided background and foundations for sustainable supply chains for sustainable cities and highlighted several applications of ours.

Summary and Conclusions

- ▶ We provided background and foundations for sustainable supply chains for sustainable cities and highlighted several applications of ours.
- ▶ We discussed a model for sustainable supply chains for sustainable cities that captures the frequencies of supply chain activities.

Summary and Conclusions

- ▶ We provided background and foundations for sustainable supply chains for sustainable cities and highlighted several applications of ours.
- ▶ We discussed a model for sustainable supply chains for sustainable cities that captures the frequencies of supply chain activities.
- ▶ The framework handles both sustainable operations and the design of a sustainable supply chain from scratch.

Summary and Conclusions

- ▶ We provided background and foundations for sustainable supply chains for sustainable cities and highlighted several applications of ours.
- ▶ We discussed a model for sustainable supply chains for sustainable cities that captures the frequencies of supply chain activities.
- ▶ The framework handles both sustainable operations and the design of a sustainable supply chain from scratch.
- ▶ Qualitative properties of the model were presented.


Summary and Conclusions

- ▶ We provided background and foundations for sustainable supply chains for sustainable cities and highlighted several applications of ours.
- ▶ We discussed a model for sustainable supply chains for sustainable cities that captures the frequencies of supply chain activities.
- ▶ The framework handles both sustainable operations and the design of a sustainable supply chain from scratch.
- ▶ Qualitative properties of the model were presented.
- ▶ Numerical examples illustrated the relevance and scope of the theoretical and computational approach.


Summary and Conclusions

- ▶ We provided background and foundations for sustainable supply chains for sustainable cities and highlighted several applications of ours.
- ▶ We discussed a model for sustainable supply chains for sustainable cities that captures the frequencies of supply chain activities.
- ▶ The framework handles both sustainable operations and the design of a sustainable supply chain from scratch.
- ▶ Qualitative properties of the model were presented.
- ▶ Numerical examples illustrated the relevance and scope of the theoretical and computational approach.
- ▶ We also noted recent work in game theory and sustainable supply chain network competition.

THANK YOU!




The Virtual Center for Supernetworks



Supernetworks for Optimal Decision-Making and Improving the Global Quality of Life

Director's Welcome	About the Director	Projects	Supernetworks Laboratory	Center Associates	Media Coverage	What's New
Downloadable Articles	Visuals	Audio/Video	Books	Commentaries & OpEds	The Supernetwork Sentinel	Congratulations & Kudos



New INFORMS Fellows
October 2013

The Virtual Center for Supernetworks is an interdisciplinary center at the Isenberg School of Management that advances knowledge on large-scale networks and integrates operations research and management science, engineering, and economics. Its Director is Dr. Anna Nagurney, the John F. Smith Memorial Professor of Operations Management.

Mission: The Virtual Center for Supernetworks fosters the study and application of supernetworks and serves as a resource on networks ranging from transportation and logistics, including supply chains, and the Internet, to a spectrum of economic networks.


The Applications of Supernetworks Include: decision-making, optimization, and game theory; supply chain management; critical infrastructure from transportation to electric power networks; financial networks; knowledge and social networks; energy, the environment, and sustainability; risk management; network vulnerability, resiliency, and performance metrics; humanitarian logistics and healthcare.

Announcements and Notes	Photos of Center Activities	Photos of Network Innovators	Friends of the Center	Course Lectures	Fulbright Lectures	UMass Amherst INFORMS Student Chapter
Professor Anna Nagurney's Blog	Network Classics	Doctoral Dissertations	Conferences	Journals	Societies	Archive

Announcements and Notes from the Center Director

Professor Anna Nagurney

Updated: February 13, 2014

 Follow

Professor Anna Nagurney's Blog

RENeW

Research, Education, Networks, and the World: A Female Professor Speaks


Sustaining the Supply Chain

Mathematical Moments Podcast

It's often a challenge to get from Point A to Point B in a normal way. But what if you could? In a new podcast, Professor Anna Nagurney discusses the challenges of sustainable supply chain management and the role of mathematics in solving these problems.


PBS VIDEO

America Revealed




New Book

Networks Against Time



Photos of Center Activities



The Braess Paradox Translation

Information Photos



Publications

On a Paradox of Traffic Planning

Environmental Impact Assessment of Transportation Networks with Degradable Links in an Era of Climate Change

Anna Nagurney, "Qing Qiang," and Lorraine S. Nagurney

For more information, see: <http://supernet.isenberg.umass.edu>
 Additional references provided upon request.